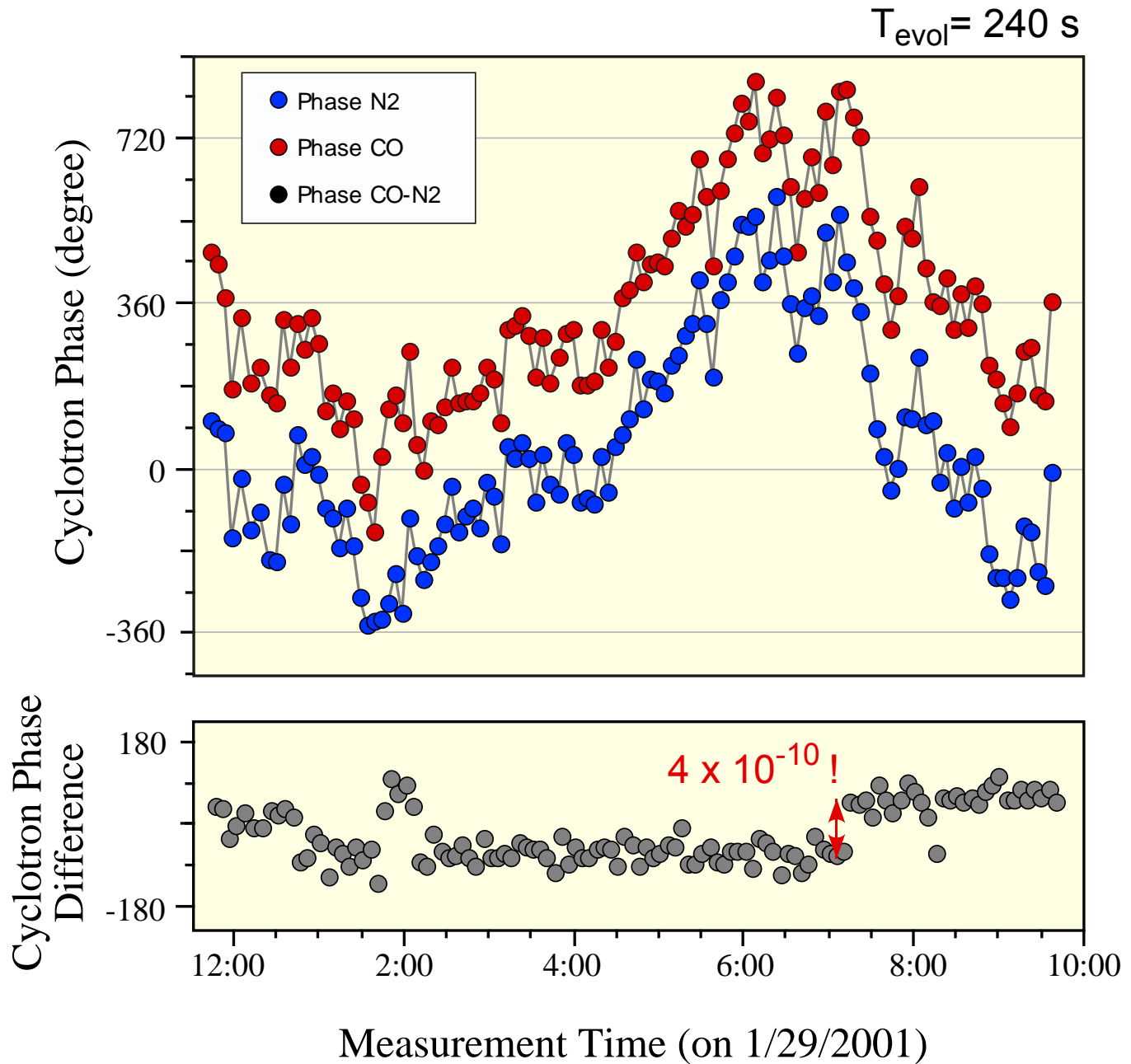
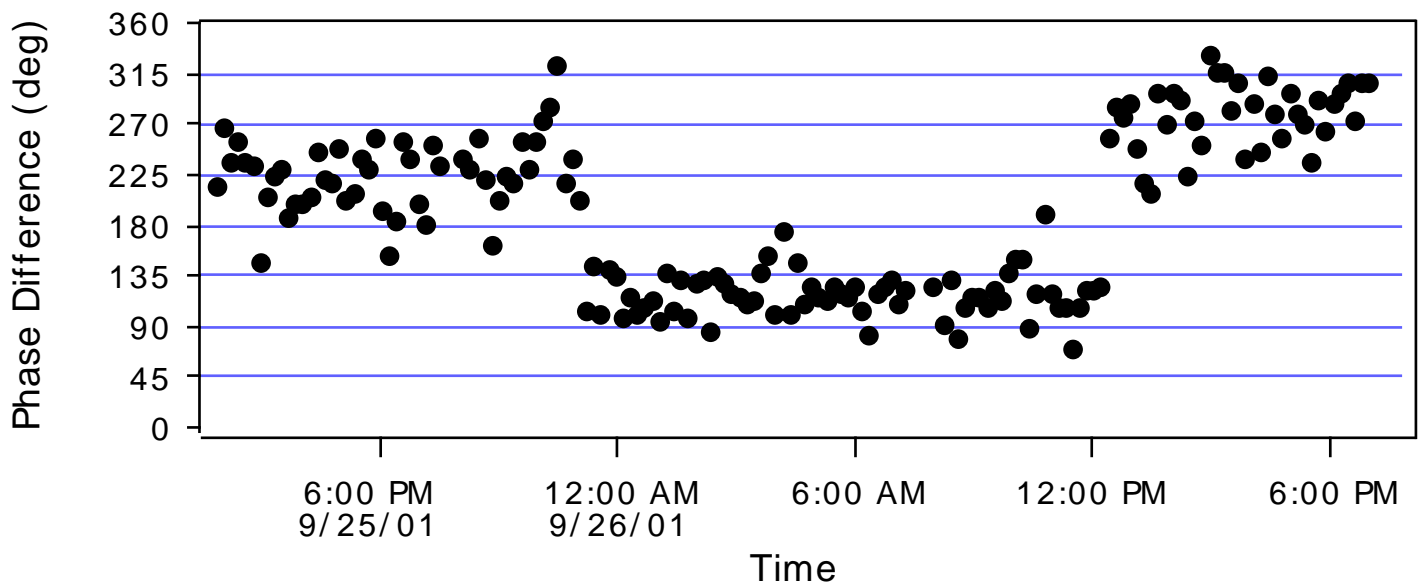
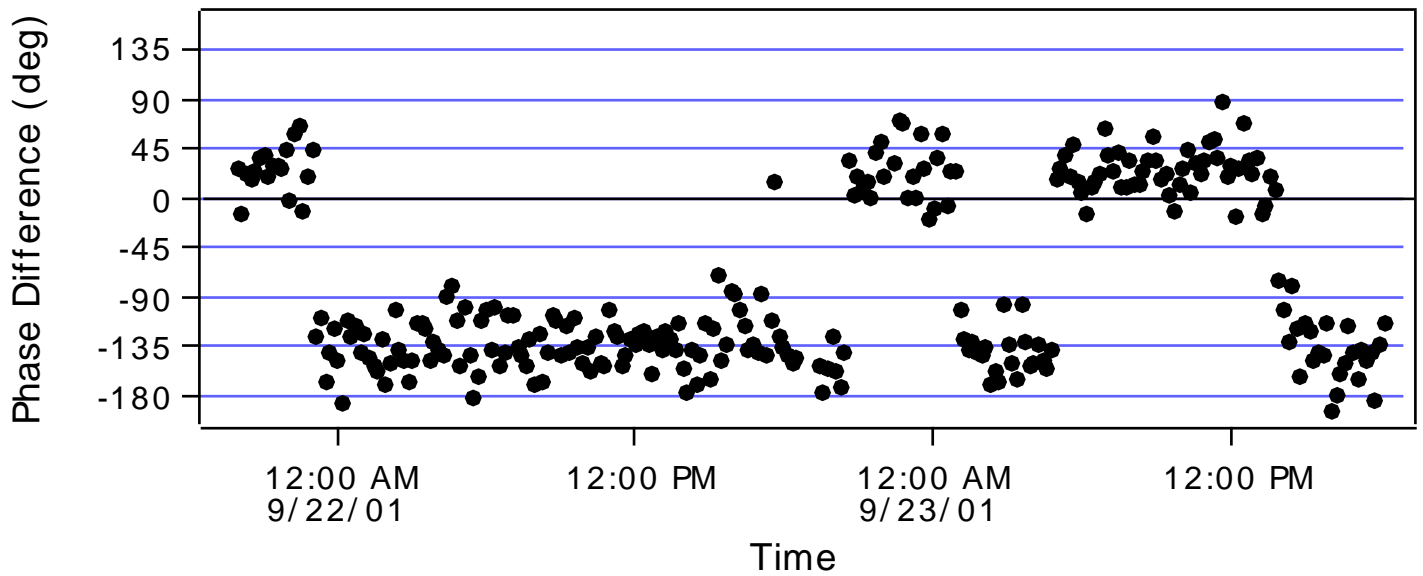
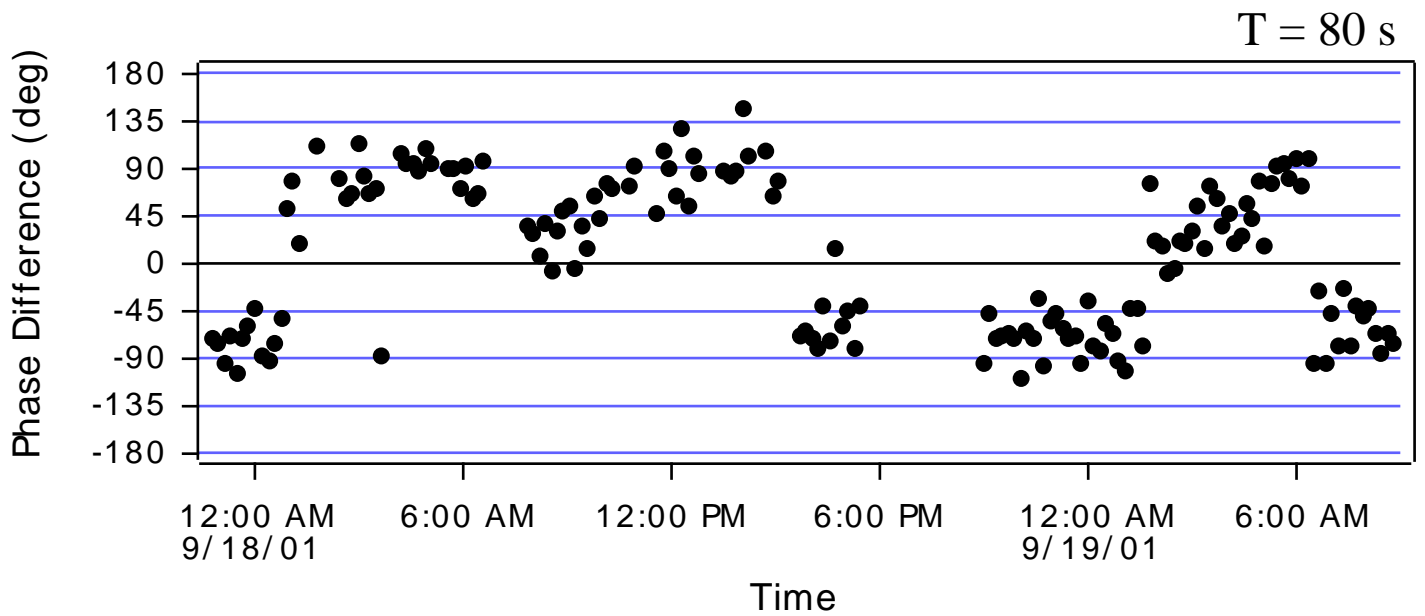


# Simultaneous Cyclotron Frequency Measurements



Big Jumps in Phase Difference !

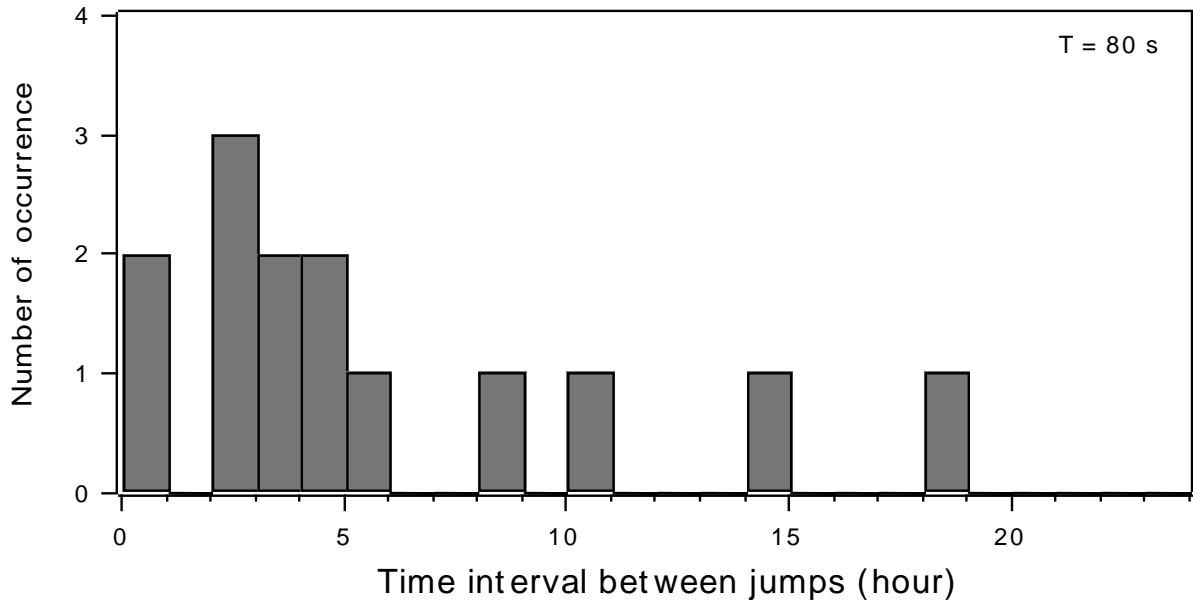
# Recurring Problem



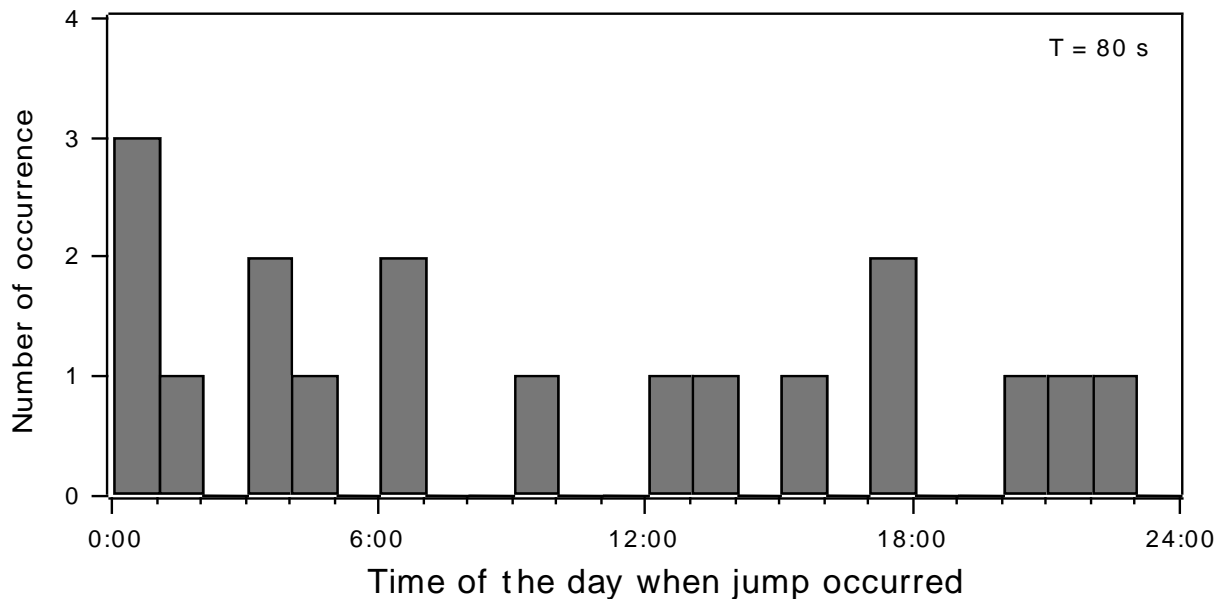
# Characteristics of Phase Jumps

We've observed ~ 20 jumps in 110 hours of data.

1) Not Periodic      shortest : 10 minutes  
                                 longest : 21 hours

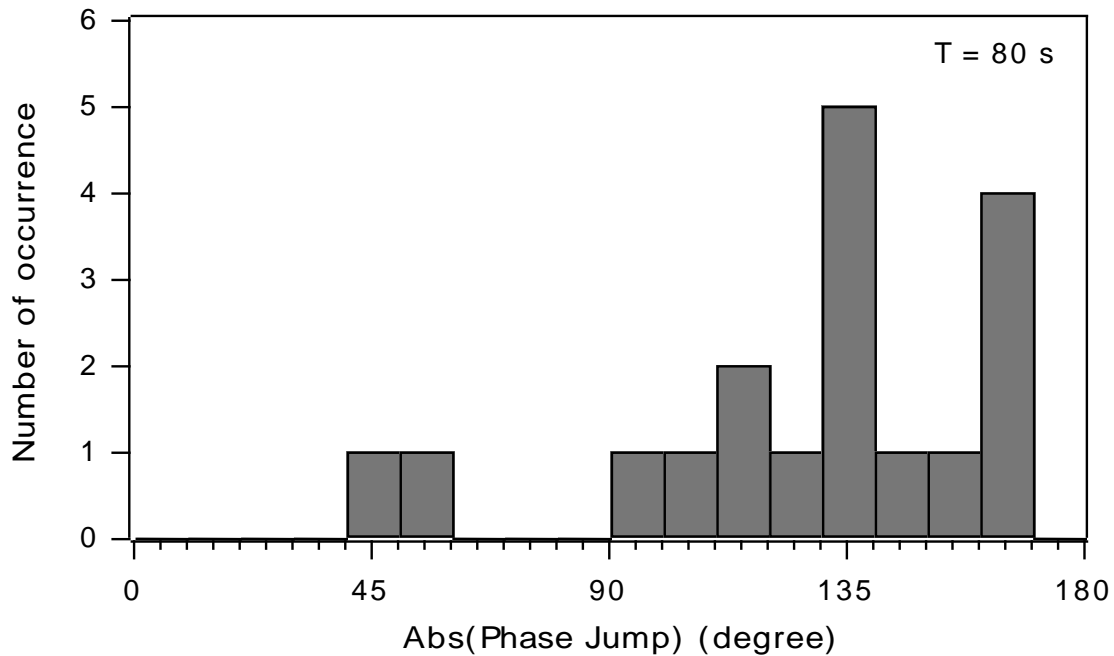


2) Do not occur at a fixed time of the day

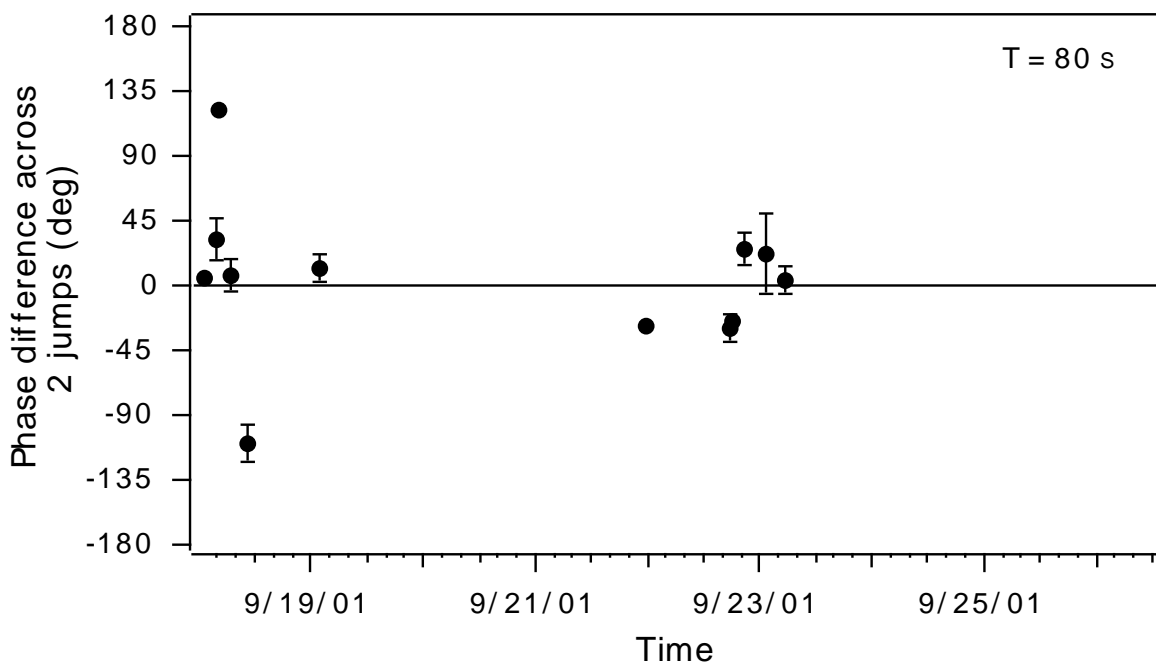


# Characteristics of Phase Jumps...

3) phase jump =  $130 (9)^\circ = 0.97 (7) \text{ ppb}$

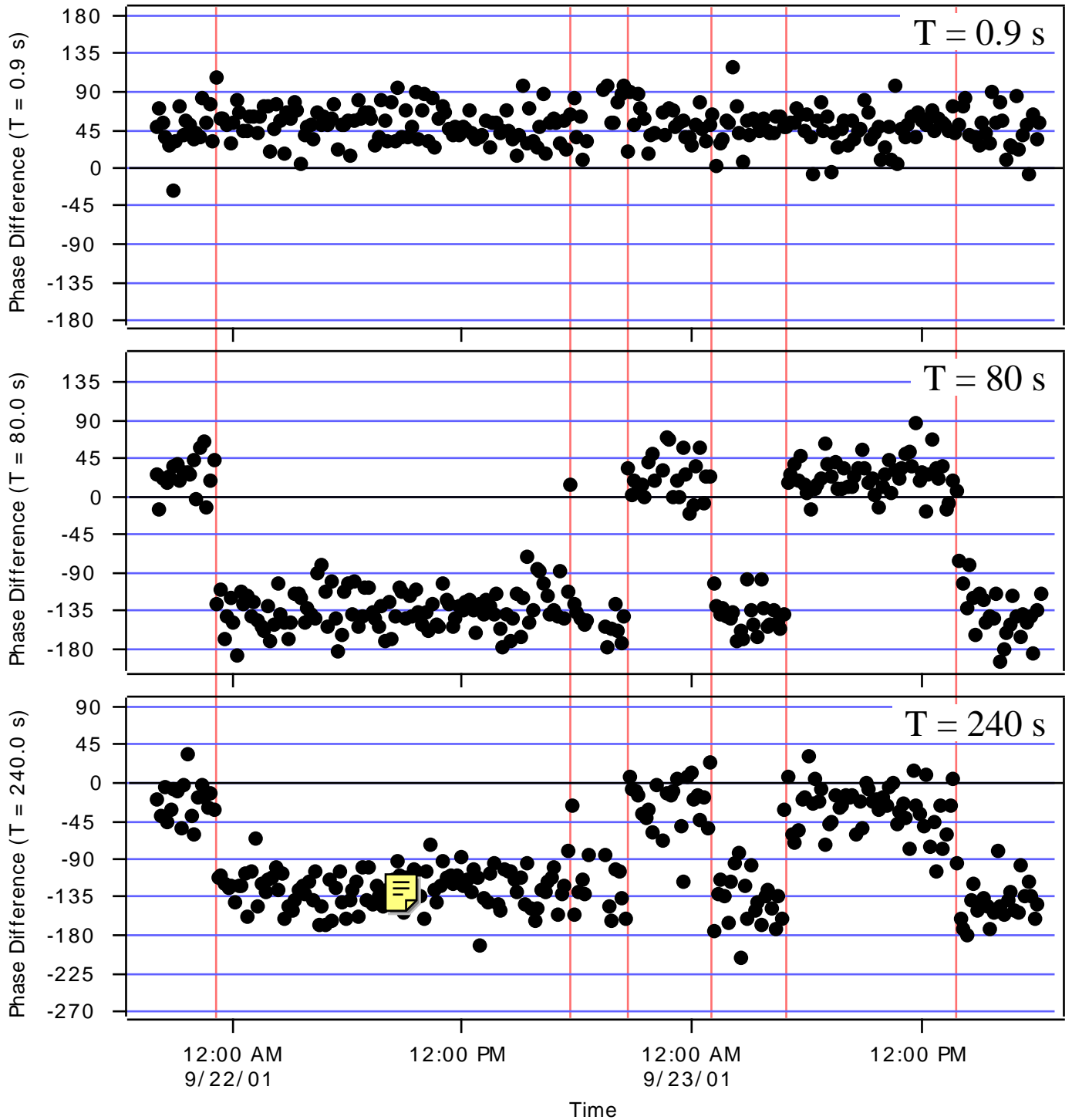


4) “Bistable” behavior: Phase “comes back” within  $35 (11)^\circ = 2.6 (8) \times 10^{-10}$ .



# Characteristics of Phase Jumps...

5) Look like a frequency shift



Phase jump is proportional to evolution time  $T$

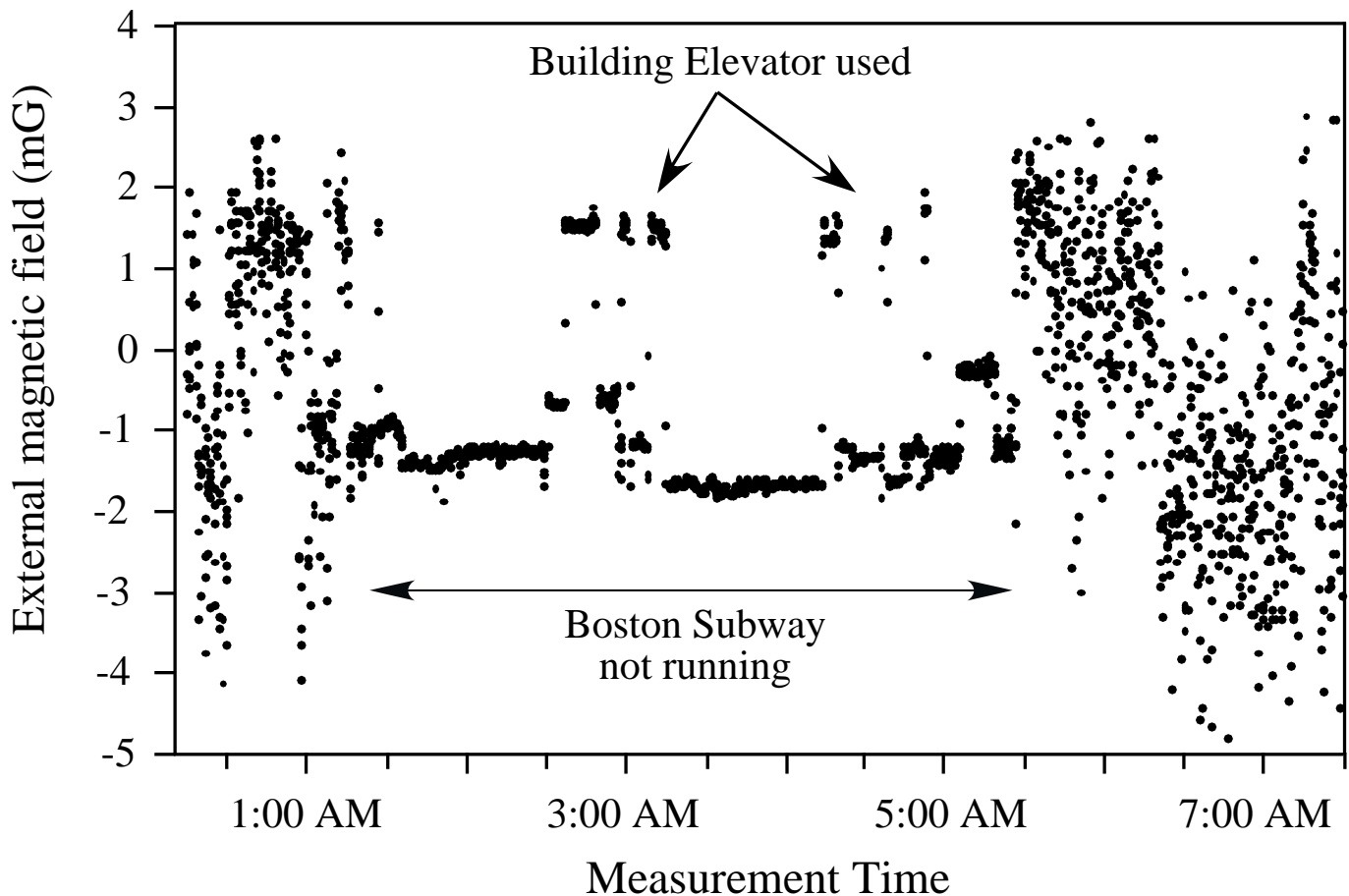
# Possible Causes

## 1) Technical problems:

- Really bad frequency reference
- Coupling leakage
- Other ions in the trap

## 2) Magnetic field jump:

- Need B field to jump by  $2.5 \times 10^{-6}$  (200 mG) to explain 1 ppb jump in difference.  
! Would result in 11 Hz shift in coupling frequency !



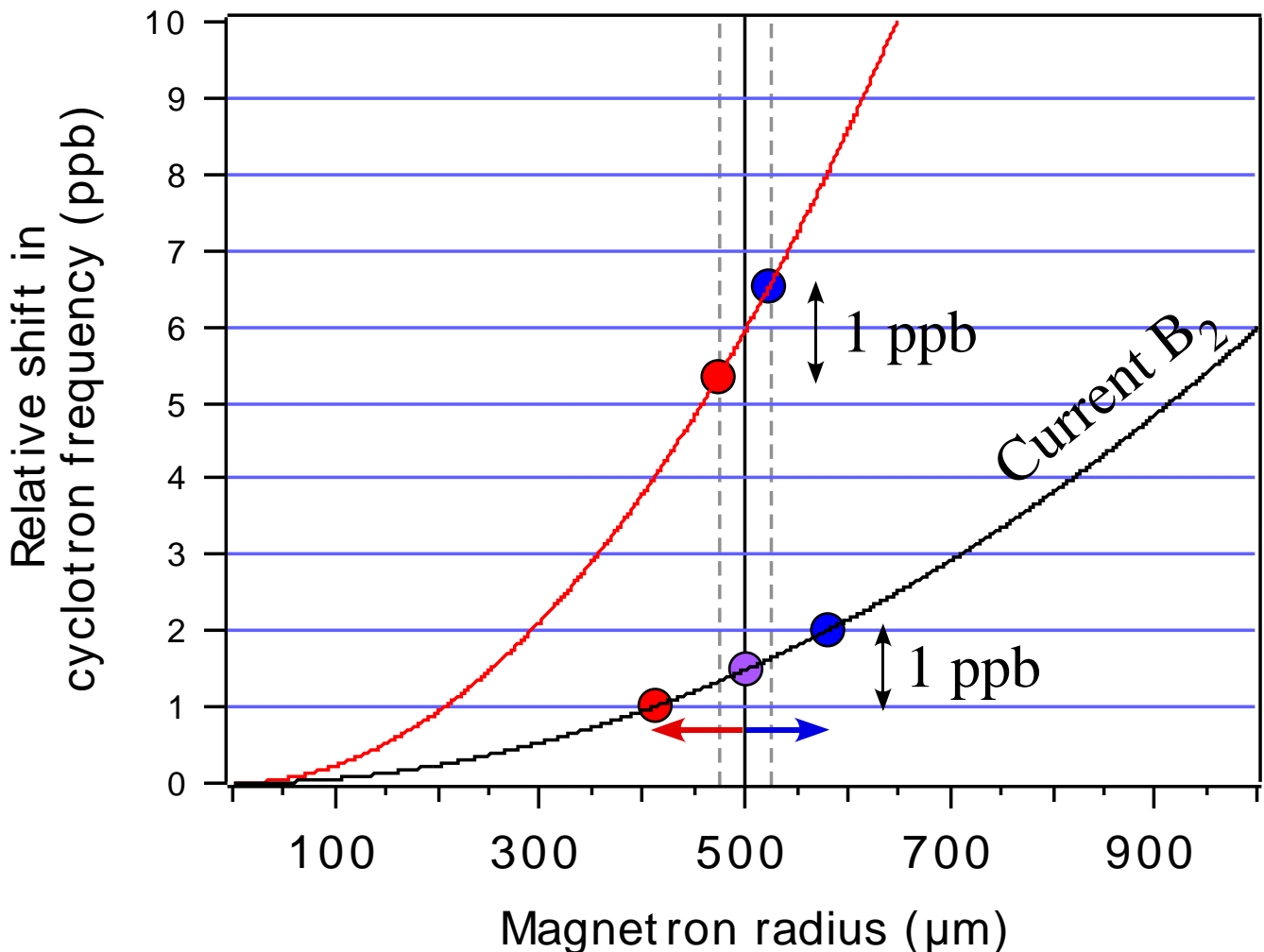
# Possible Causes...

## 3) Trapping field imperfections + dynamics

### a) Magnetic field inhomogeneities

$$\hat{z} = B_0 + B_2 z^2 - \frac{B_4}{2} z^4 + \dots$$

$$f_c'/f_c = 0.6 \times 10^{-10} \text{ per } (100 \mu\text{m})^2$$



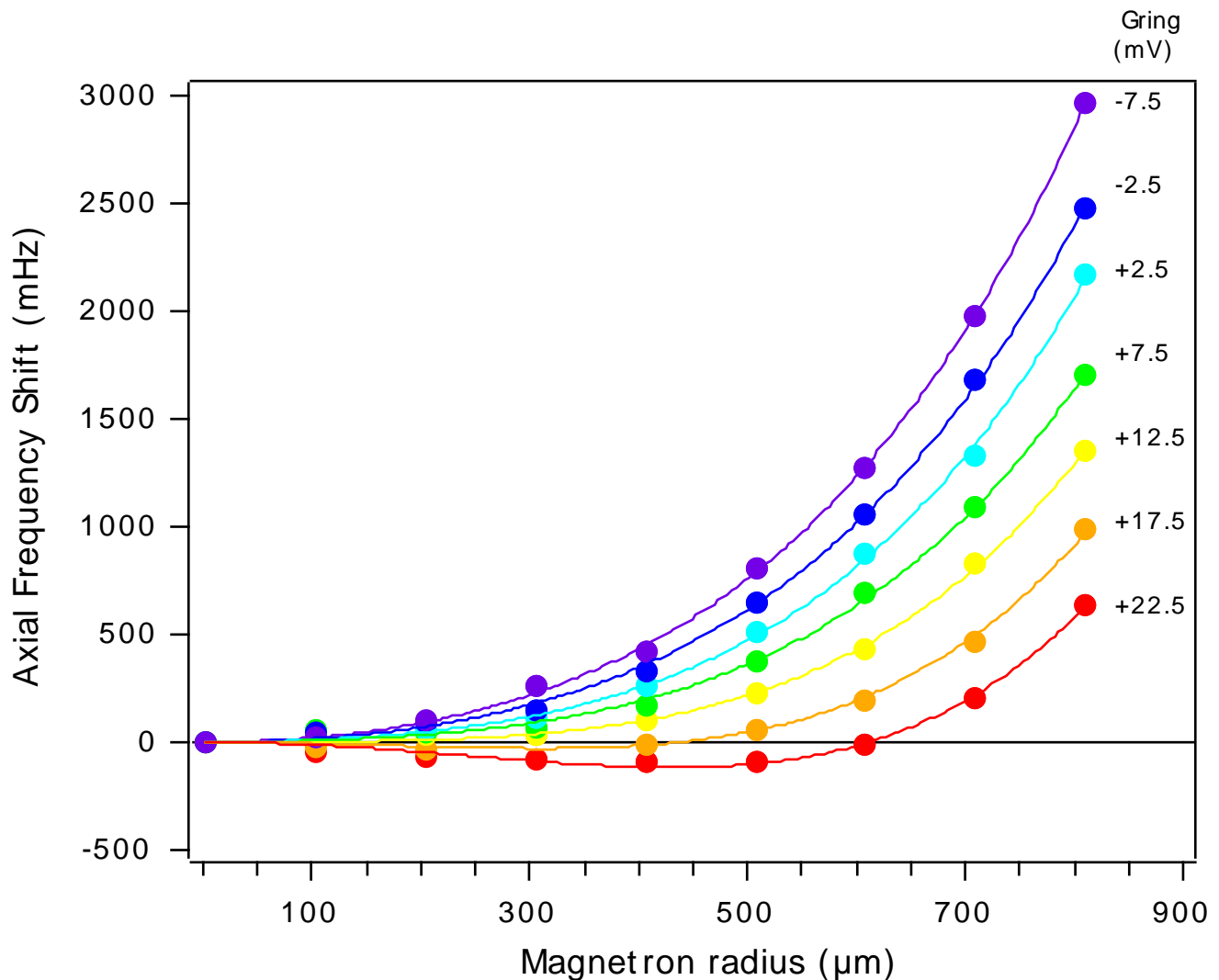
# Possible Causes...

3) Trapping field imperfections + dynamics...

b) Electrostatics anharmonicities

$$= \frac{C_2}{2d^2} z^2 - \frac{2}{2} + \frac{C_4}{2d^4} z^4 - 3z^2 + \frac{3}{8} z^4 + K$$

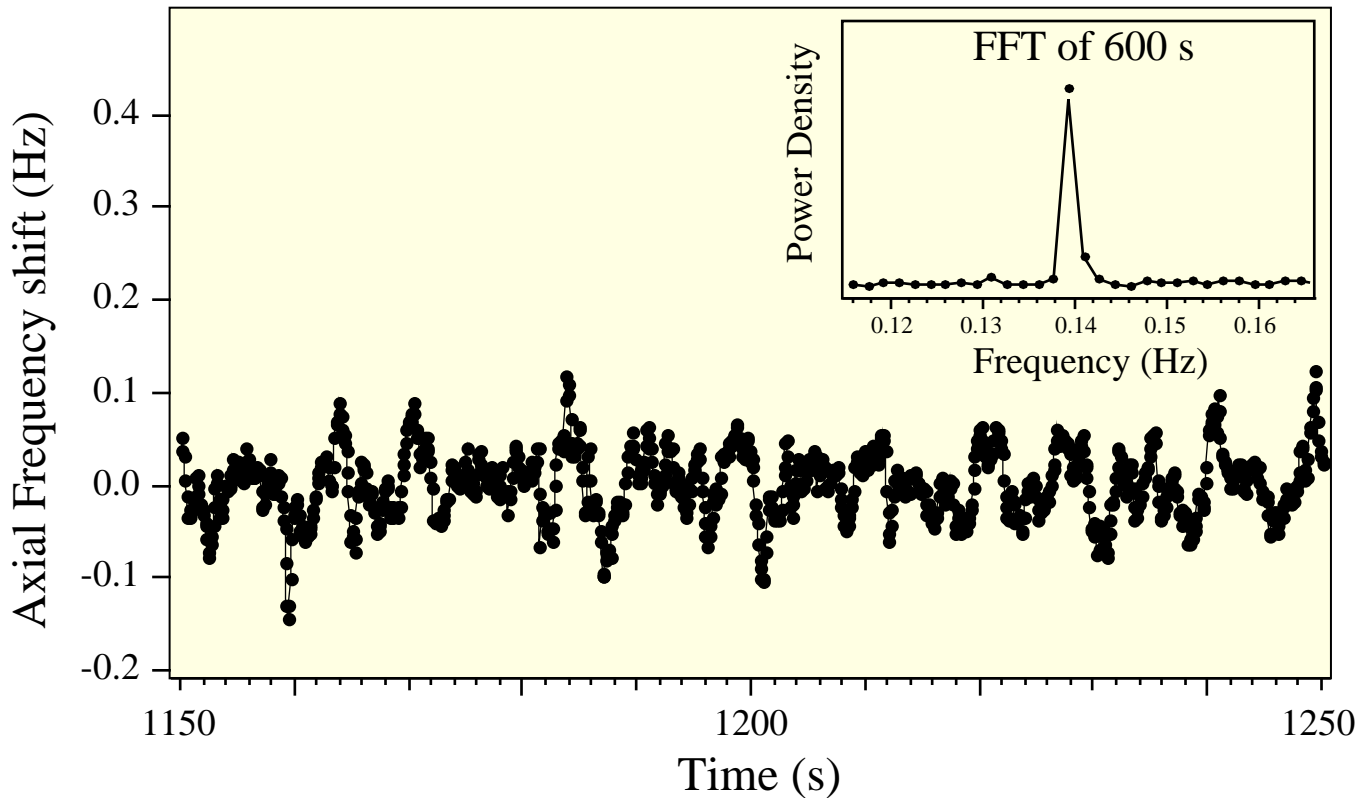
Amplitude calibration and new acquisition system  
⇒ Measurement of C4 and C6





# Watching the Swapping Motion

Axial frequency of  $\text{CO}^+$  in the presence of  $\text{N}_2^+$



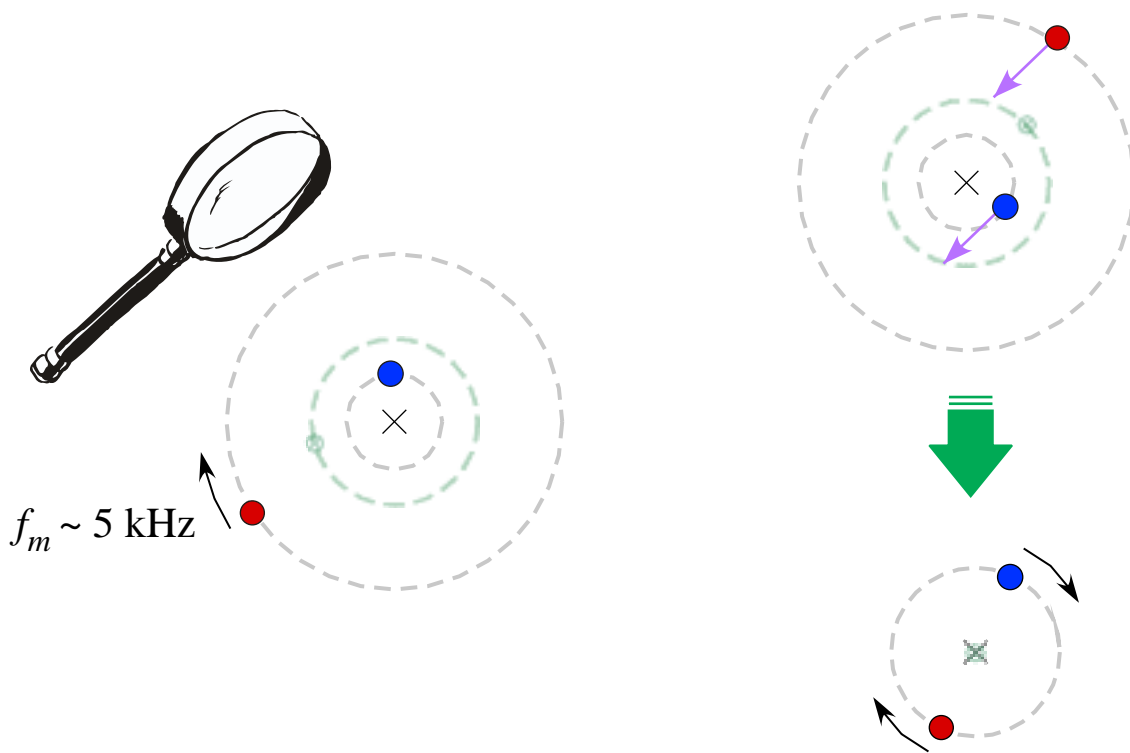
- Direct observation of swapping frequency.
- Period of oscillation ( $T_{\text{osc}} \sim 15$  s) matches calculation from estimated separation from make.
- $T_{\text{osc}} \sim \text{sep}^3$

\*\*\*\*\*

Observed no change in oscillation period and amplitude across a jump in the phase.

# What do we do next ?

- Measure  $f_z$  vs Guard Ring
- Study size of jump vs separation and <sup>mag</sup>
- “Measure-and-Zero” Technique: <sup>cyc</sup>



- Try with a different pair
- Modify apparatus to control  $C_6$

Once problem is solved:

- $N_2^+ / CO^+$  to study systematic errors
- $^{32}S / ^{33}S$  and  $^3H / ^3He$
- chemical binding energies ?

