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1. *Superfluid suppression of impurity scattering in a Bose-Einstein condensate*

The concept of superfluidity applies to both macroscopic and microscopic objects. In both cases, there is no dissipation or drag force as long as the objects move with a velocity less than the so-called critical velocity. A moving macroscopic object creates a complicated flow field. Above a certain velocity, vortices are created. In contrast, the physics of moving impurities, which are microscopic objects, is much simpler. At velocities larger than the Landau critical velocity, they will create elementary excitations, phonons or rotons in the case of liquid helium-4.

We could create impurity atoms in a trapped BEC by transferring some of the atoms into another hyperfine state using an optical Raman transition. The photon recoil and therefore the velocity of the impurity atoms was varied by the angle between the two laser beams. Collisions between the impurity atoms and the condensate were observed as a redistribution of momentum when the velocity distribution was analyzed with a ballistic expansion technique. The collisional cross section was dramatically reduced when the velocity of the impurities was reduced below the speed of sound of the condensate, in agreement with the Landau criterion for superfluidity [1].

![Diagram](image)

Observation of collisions between the condensate and impurities. The impurities in the \( m_F = 0 \) hyperfine state traveled at 6 cm/s to the left. Collisions redistribute the momentum over a sphere in momentum space, resulting in the observed halo (a). In figure (b), the impurities and the condensate in the \( m_F = -1 \) state were separated with a magnetic field gradient during the ballistic expansion. The effect of collisions is to slow down some of the impurity atoms and speed up the condensate atoms. The absorption images are 4.5 mm times 7.2 mm in size.

2. *Dissipationless flow and superfluidity in gaseous Bose-Einstein condensates*

In previous work [2] we found evidence for a critical velocity in a condensate. The Bose-Einstein condensate was stirred with a laser beam at variable velocity, and the onset of dissipation was observed by monitoring the temperature of the sample. We have studied the same system by observing the condensate during the stirring using repeated *in situ* non-destructive imaging of the condensate. These images show the distortion of the
Density dependence of the critical velocity. The onset of the drag force is shown for two different condensate densities, corresponding to maximum sound velocities of 4.8 mm/s (solid circles, left axis) and 7.0 mm/s (crosses, right axis). The stirring amplitudes are 29 µm and 58 µm, respectively. The two vertical axes are offset for clarity. The bars represent statistical errors.

The distortion or asymmetry of the flow is proportional to the drag force and a sensitive indicator for dissipation. The onset of dissipation was found at a critical velocity of about 10 % of the speed of sound which corrects the higher value found previously with a less sensitive method [2]. A comparison of the new technique observing the drag force to the calorimetric method showed good agreement.

Density dependence of the critical velocity. The onset of the drag force is shown for two different condensate densities, corresponding to maximum sound velocities of 4.8 mm/s (solid circles, left axis) and 7.0 mm/s (crosses, right axis). The stirring amplitudes are 29 µm and 58 µm, respectively. The two vertical axes are offset for clarity. The bars represent statistical errors.

3. Amplification of light and atoms in a Bose-Einstein condensate

Bose-Einstein condensates illuminated by an off-resonant laser beam (“dressed condensates”) were used to realize phase-coherent amplification of matter waves [4, 5]. The amplification process involved the scattering of a condensate atom and a laser photon into an atom in a recoil mode and a scattered photon. This four-wave mixing process between two electromagnetic fields and two Schrödinger fields became a self-amplifying process above a threshold laser intensity, leading to matter wave gain.
However, the symmetry between light and atoms indicates that a dressed condensate should not only amplify injected atoms, but also injected light.

Amplification of light and atoms by off-resonant light scattering. (a) The fundamental process is the absorption of a photon from the “dressing” beam by an atom in the condensate (state $|1\rangle$), which is transferred to a recoil state (state $|2\rangle$) by emitting a photon into the probe field. The intensity in the probe light field was monitored by a photomultiplier. (b) The two-photon Raman-type transition between two motional states ($|1\rangle, |2\rangle$) gives rise to a narrow resonance. (c) The dressed condensate is the upper state ($|1'\rangle$) of a two-level system, and decays to the lower state (recoil state of atoms, $|2\rangle$) by emitting a photon. Since the system is fully inverted, there is gain for the probe beam.

We have studied the optical properties of a dressed condensate above and below the threshold for the matter wave amplification [6]. The optical gain below the threshold has a narrow bandwidth due to the long coherence time of a condensate. The gain represents the imaginary part of the complex index of refraction. A sharp peak in the gain implies a steep dispersive shape for the real part of the index of refraction $n(\omega)$. This resulted in an extremely slow group velocity for the amplified light. The figure shows that light pulses were delayed by about 20 $\mu$s across the 20 $\mu$m wide condensate corresponding to a group velocity of 1 m/s. This is one order of magnitude slower than any value reported previously [7].

Above the threshold to matter wave amplification, we observed non-linear optical behavior. Thus we could map out the transition from single-atom gain to collective gain.

Pulse delay due to light amplification. (a) Amplification and 20 $\mu$s delay were observed when a Gaussian probe pulse of about 140 $\mu$s width and 0.11 mW/cm$^2$ peak intensity was sent through the dressed condensate (bottom trace). The top trace is a reference taken without the dressed condensate. Solid curves are Gaussian fits to guide the eyes. (b) The observed delay time was proportional to $\ln(g)$, where $g$ is the observed gain.
4. Enhancement and suppression of spontaneous emission and light scattering by quantum degeneracy

Quantum degeneracy modifies light scattering and spontaneous emission. For fermions, Pauli blocking leads to a suppression of both processes. In contrast, in a weakly interacting Bose-Einstein condensate, we found spontaneous emission to be enhanced, while light scattering is suppressed [8]. This difference is attributed to many-body effects and quantum interference in a Bose-Einstein condensate.

Generally, transition rates between an initial state with population $N_1$ and a final state with population $N_2$ are proportional to $N_1(1+N_2)$ for bosons and to $N_1(1-N_2)$ for fermions. This simple derivation of transition rates using occupation numbers becomes subtle or even invalid for correlated many-body states such as an interacting Bose-Einstein condensate ground state. We analyzed under which circumstances the simple approach can be used to reproduce the correct results for the interaction between light and a BEC.

We showed theoretically that spontaneous emission in a weakly interacting BEC is enhanced, consistent with the description using occupation numbers, and calculated the enhancement factor. We compared this result to light scattering in a BEC, which is suppressed due to many-body interference effects not included in the simple derivation, as we have shown experimentally and theoretically in previous work [9]. In contrast, in fermionic systems quantum degeneracy leads to a suppression of both spontaneous emission and light scattering.

Modification of spontaneous emission (solid line) and light scattering (dashed line) due to quantum degeneracy. In (a) we have plotted the enhancement factor for spontaneous emission and the suppression factor for light scattering for a weakly interacting Bose-Einstein condensate as a function of the light wave vector $k_L$ in units of $k_s$, the wave vector of an atom moving at the speed of sound. In (b) the suppression factors for spontaneous emission and light scattering in a Fermi gas at zero temperature are plotted as a function of $k_L$ in units of the Fermi wave vector $k_F$.

5. Dissipation in a stirred dilute Bose gas

We studied dissipation in a dilute Bose gas induced by the motion of a macroscopic object [10]. A blue-detuned laser beam focused on the center of a trapped gas of sodium atoms was scanned both above and below the BEC transition temperature. Measurements below the transition temperature confirmed the existence of a critical
velocity [2, 3]. Above the transition temperature, we found a quadratic dependence of the dissipated energy on velocity, in agreement with a simple model.

These measurements allowed for a comparison between the heating rates for the superfluid and normal gas. Outside the superfluid regime, well above the critical velocity, the intrinsic heating of the condensate (normalized for geometry) was seen to be similar to the heating of the normal component. In both cases, each collision with the stirrer at velocity $v$ transfers an energy of about $Mv^2$ to the gas.

Heating of the normal gas. The energy transfer rate per particle versus velocity of the moving laser beam shows a quadratic dependence.

6. Does matter wave amplification work for fermions?

Several recently observed phenomena Bose-Einstein condensates, superradiance of atoms, four-wave mixing and matter wave amplification were described as processes which are bosonically stimulated, i.e., their rates are proportional to $(N+1)$, where $N$ is the number of identical bosons in the final state. However, we had pointed out that atomic superradiance does not depend on Bose-Einstein statistics and would occur for thermal atoms or even for fermions, although with a much shorter coherence time [11]. These suggestions have stirred a controversy among researchers.

In Ref. [12], we reconciled the different physical descriptions with the central result that the stimulated processes mentioned above do not rely on quantum statistics, but rather on symmetry and coherence. Bosonic quantum-degeneracy is sufficient, but not necessary for these processes. It represents only one special way to prepare a system in a cooperative state which shows coherent and collective behavior.