

DNN Model and Hardware Co-Design

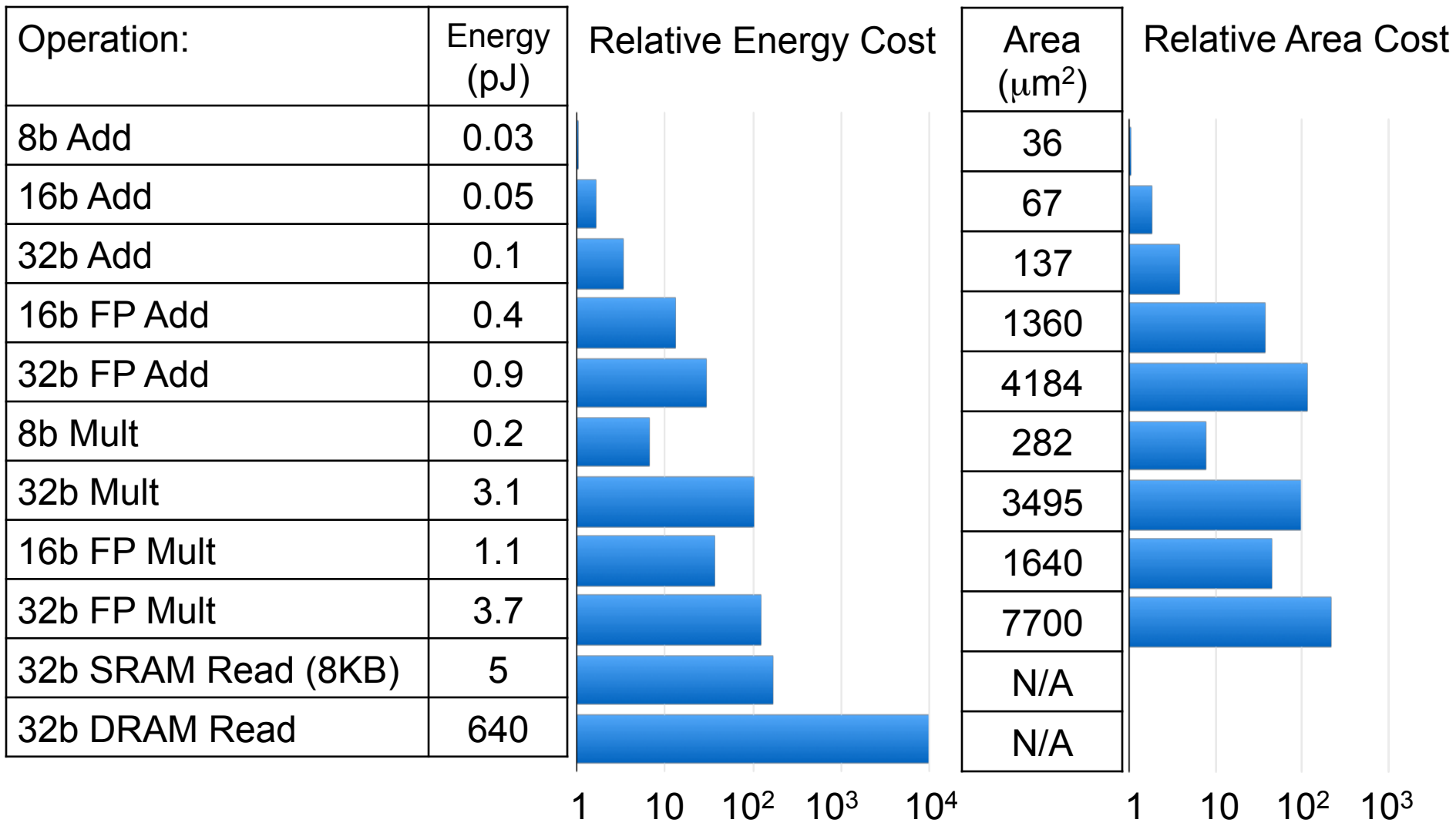
CICS/MTL Tutorial (2017)

Website: <http://eyeriss.mit.edu/tutorial.html>

Approaches


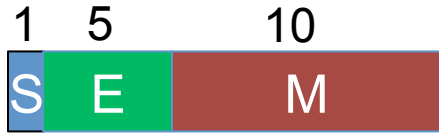



- **Reduce size of operands for storage/compute**
 - Floating point -> Fixed point
 - Bit-width reduction
 - Non-linear quantization
- **Reduce number of operations for storage/compute**
 - Exploit Activation Statistics (Compression)
 - Network Pruning
 - Compact Network Architectures

Cost of Operations



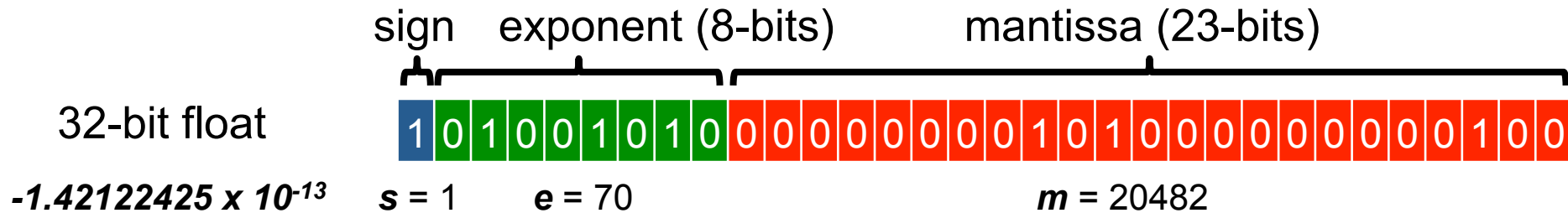
[Horowitz, "Computing's Energy Problem (and what we can do about it)", ISSCC 2014]

Number Representation

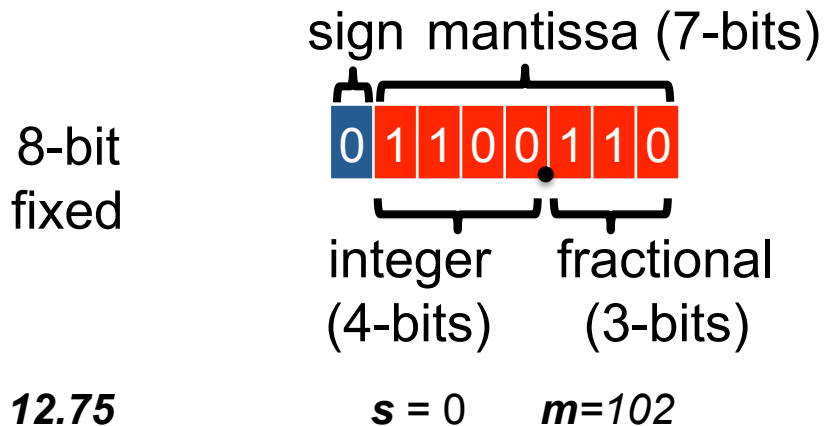
		Range	Accuracy
FP32		$10^{-38} - 10^{38}$.000006%
FP16		$6 \times 10^{-5} - 6 \times 10^4$.05%
Int32		$0 - 2 \times 10^9$	$\frac{1}{2}$
Int16		$0 - 6 \times 10^4$	$\frac{1}{2}$
Int8		$0 - 127$	$\frac{1}{2}$

Floating Point → Fixed Point

Floating Point

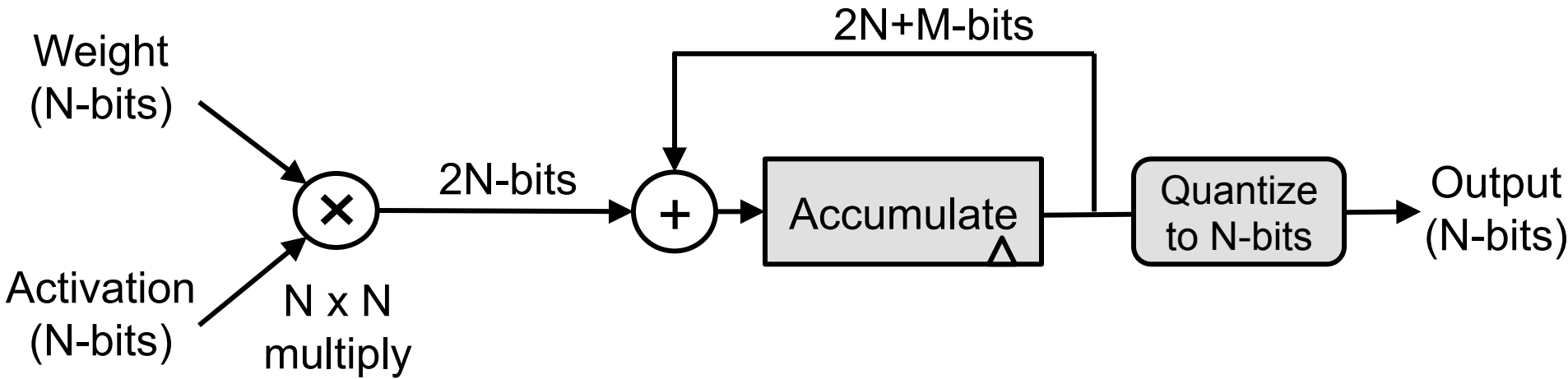


Fixed Point



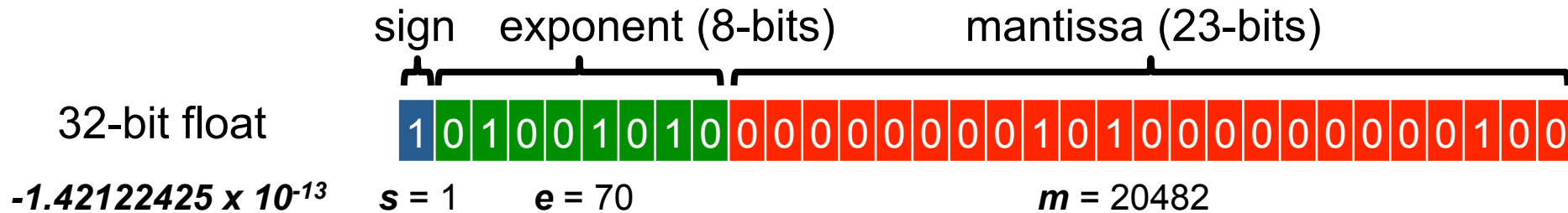
N-bit Precision

For no loss in precision, **M** is determined based on largest filter size (in the range of 10 to 16 bits for popular DNNs)

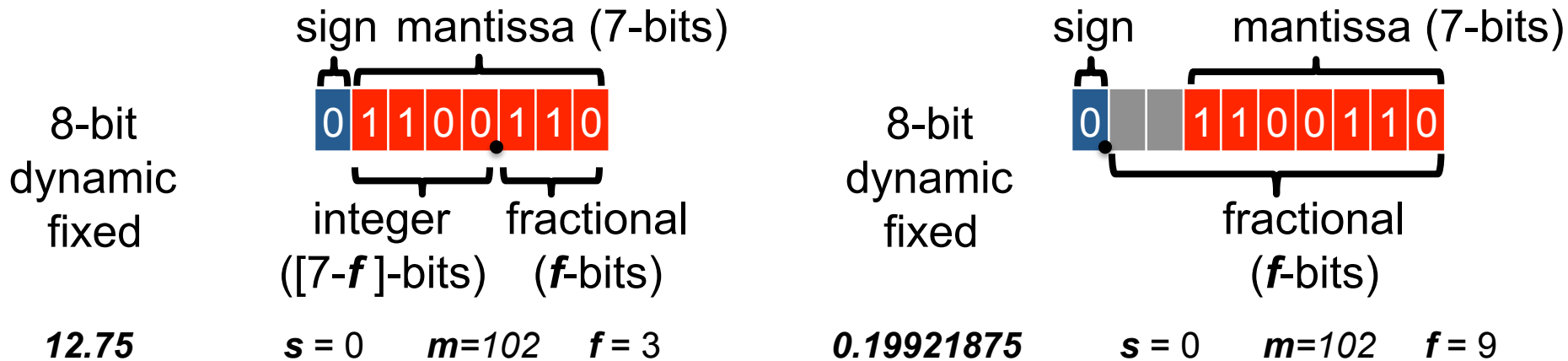


Dynamic Fixed Point

Floating Point



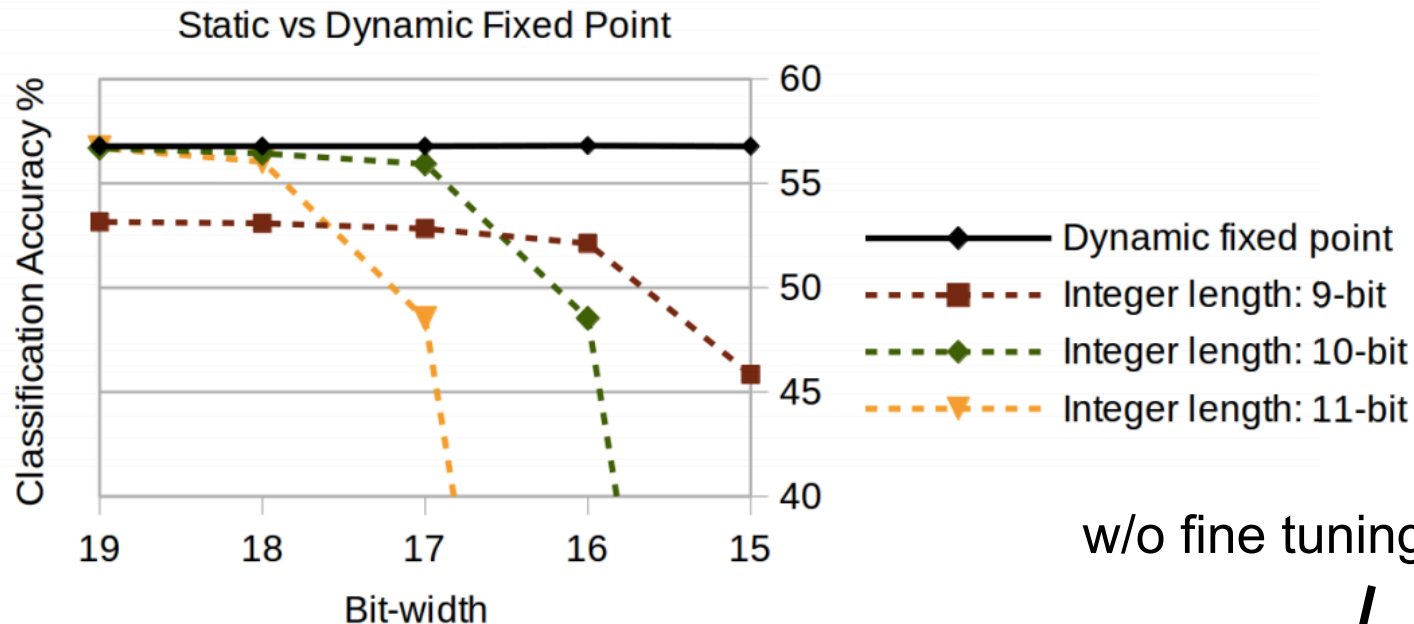
Fixed Point



Allow f to vary based on data type and layer

Impact on Accuracy

Top-1 accuracy
of CaffeNet
on ImageNet



	Layer outputs	CONV parameters	FC parameters	32-bit floating point baseline	Fixed point accuracy
LeNet (Exp 1)	4-bit	4-bit	4-bit	99.1%	99.0% (98.7%)
LeNet (Exp 2)	4-bit	2-bit	2-bit	99.1%	98.8% (98.0%)
Full CIFAR-10	8-bit	8-bit	8-bit	81.7%	81.4% (80.6%)
SqueezeNet top-1	8-bit	8-bit	8-bit	57.7%	57.1% (55.2%)
CaffeNet top-1	8-bit	8-bit	8-bit	56.9%	56.0% (55.8%)
GoogLeNet top-1	8-bit	8-bit	8-bit	68.9%	66.6% (66.1%)

Avoiding Dynamic Fixed Point

Batch normalization 'centers' dynamic range

AlexNet
(Layer 6)

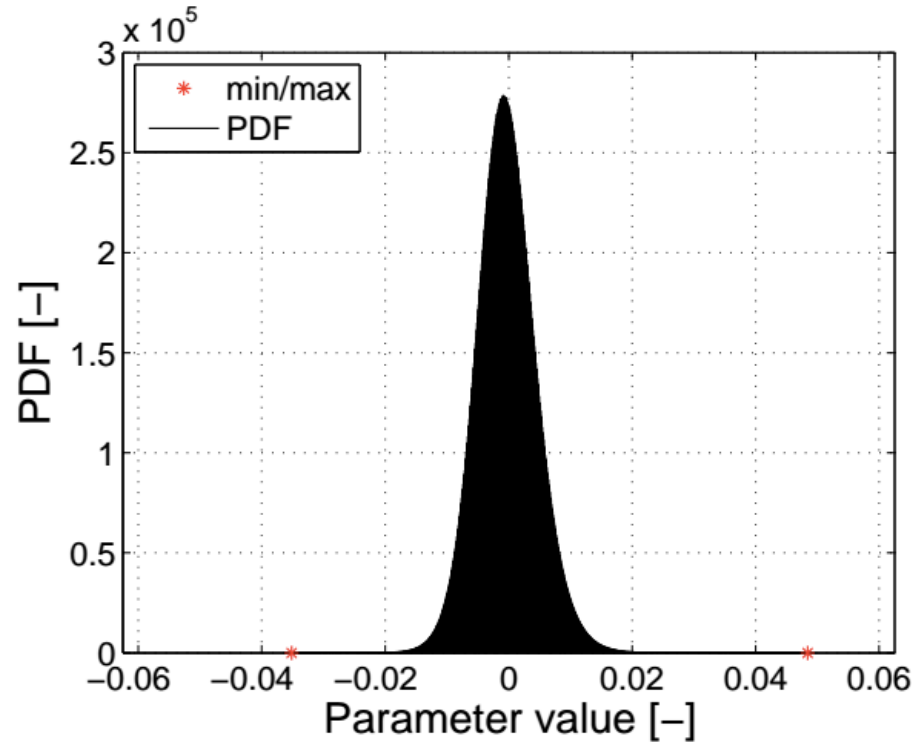


Image Source: Moons
et al, WACV 2016

'Centered' dynamic ranges might reduce need for
dynamic fixed point

Nvidia PASCAL

“New half-precision, **16-bit floating point instructions** deliver over **21 TeraFLOPS** for unprecedented training performance. **With 47 TOPS (tera-operations per second) of performance, new 8-bit integer instructions** in Pascal allow AI algorithms to deliver real-time responsiveness for deep learning inference.”

– Nvidia.com (April 2016)



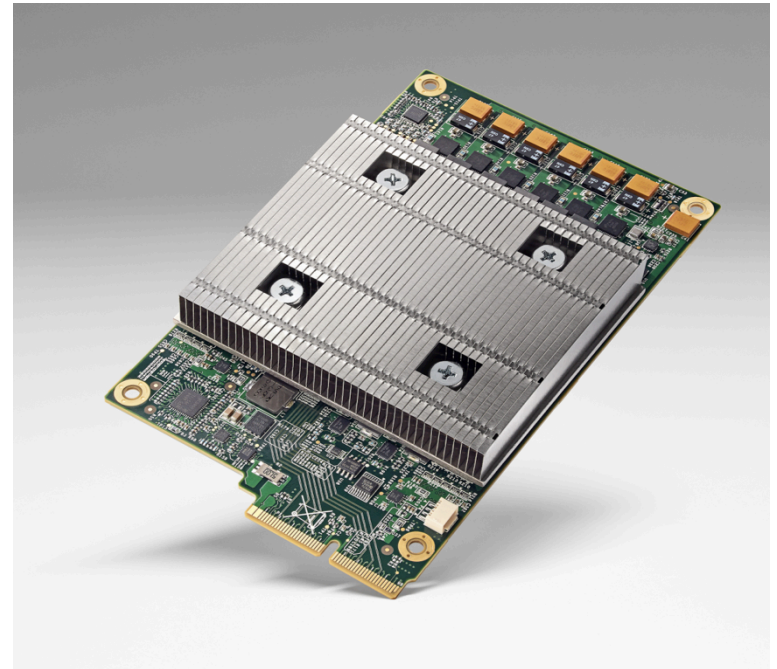
Google's Tensor Processing Unit (TPU)

“ With its TPU Google has seemingly focused on delivering the data really quickly by cutting down on precision. Specifically, it doesn't rely on floating point precision like a GPU

....

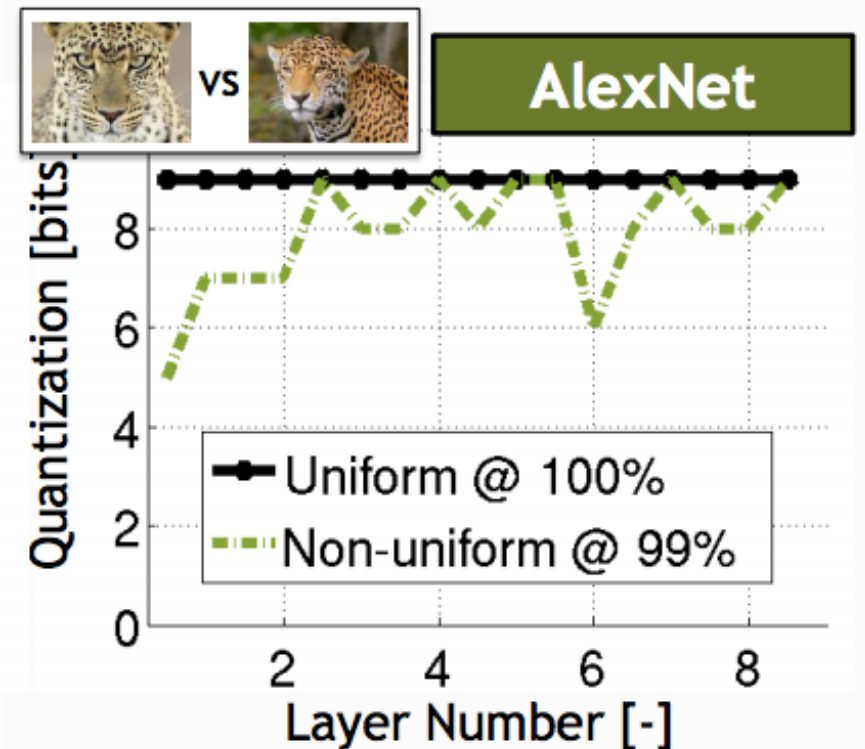
Instead the chip uses integer math...TPU used 8-bit integer.”

- Next Platform (May 19, 2016)



Precision Varies from Layer to Layer

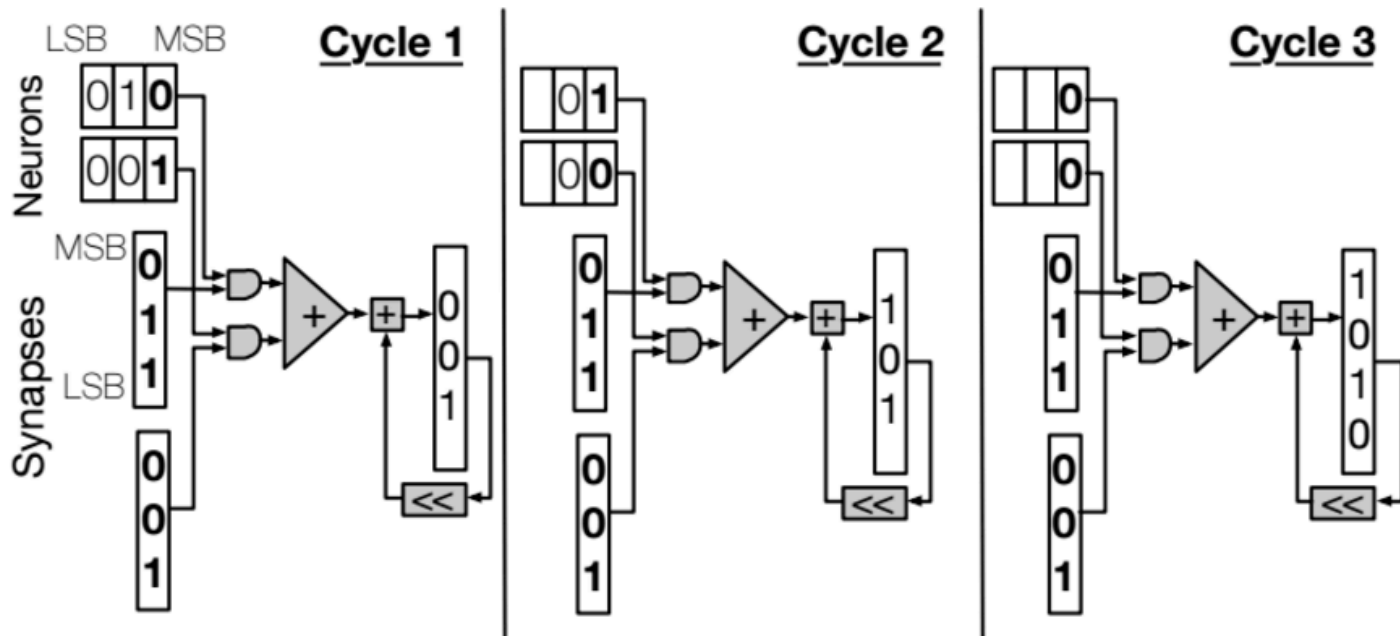
Tolerance	Bits per layer (I+F)
AlexNet (F=0)	
1%	10-8-8-8-8-8-6-4
2%	10-8-8-8-8-8-5-4
5%	10-8-8-8-7-7-5-3
10%	9-8-8-8-7-7-5-3



Bitwidth Scaling (Speed)

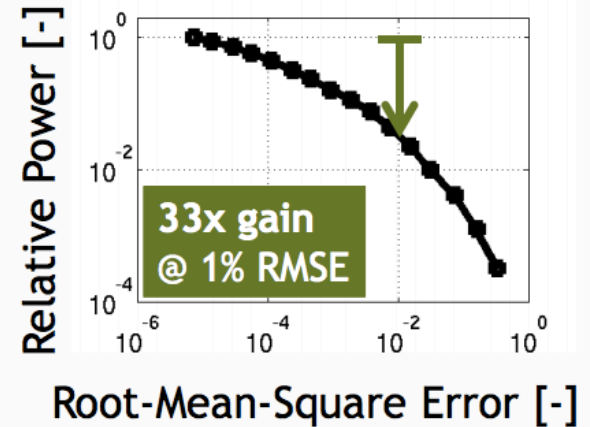
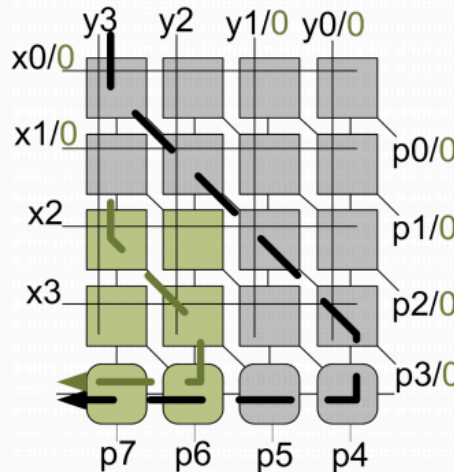
Bit-Serial Processing: Reduce Bit-width → Skip Cycles
Speed up of 2.24x vs. 16-bit fixed

$$\sum_{i=0}^{N_i-1} s_i \times n_i = \sum_{i=0}^{N_i-1} s_i \times \sum_{b=0}^{P-1} n_i^b \times 2^b = \sum_{b=0}^{P-1} 2^b \times \sum_{i=0}^{N_i-1} n_i^b \times S_i$$



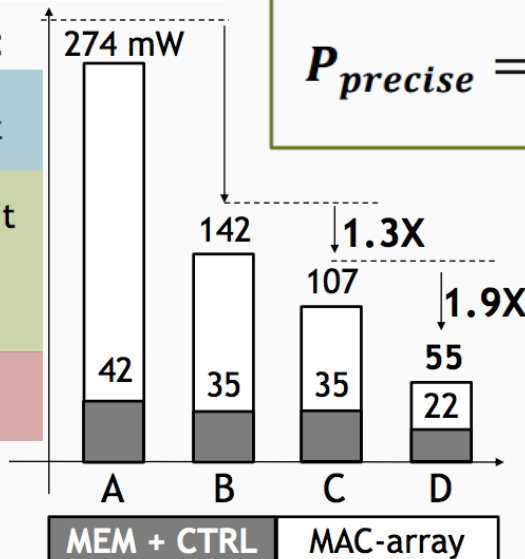
Bitwidth Scaling (Power)

Reduce Bit-width →
Shorter Critical Path
→ Reduce Voltage



AlexNet Layer 2 example:

- A. 2D-baseline @ 16 bit
- B. Precision-Scaling @ 7-7 bit
- C. Voltage-Scaling @ 0.9 V
- D. Sparse operation guarding



$$P_{precise} = \alpha C f V^2 \Rightarrow P_{imprecise} = \frac{\alpha}{k_1} C f \left(\frac{V}{k_2}\right)^2$$

**Power reduction of
2.56x vs. 16-bit fixed
On AlexNet Layer 2**

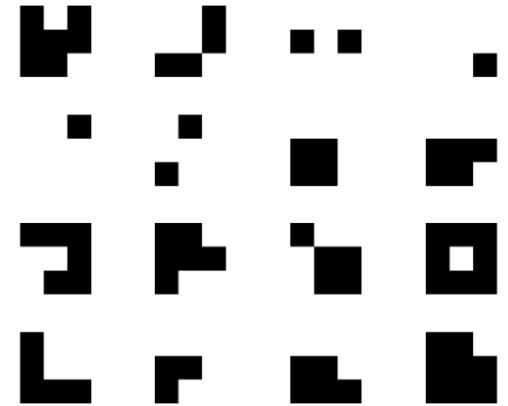
Binary Nets

- **Binary Connect (BC)**

- Weights $\{-1, 1\}$, Activations 32-bit float
- MAC \rightarrow addition/subtraction
- Accuracy loss: **19%** on AlexNet

[Courbariaux, NIPS 2015]

Binary Filters



- **Binarized Neural Networks (BNN)**

- Weights $\{-1, 1\}$, Activations $\{-1, 1\}$
- MAC \rightarrow XNOR
- Accuracy loss: **29.8%** on AlexNet

[Courbariaux, arXiv 2016]

Scale the Weights and Activations

- **Binary Weight Nets (BWN)**

- Weights $\{-\alpha, \alpha\}$ \rightarrow except first and last layers are 32-bit float
- Activations: 32-bit float
- α determined by the l_1 -norm of all weights in a layer
- Accuracy loss: **0.8%** on AlexNet

- **XNOR-Net**

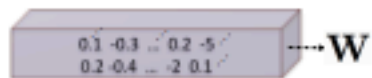
- Weights $\{-\alpha, \alpha\}$
- Activations $\{-\beta_i, \beta_i\}$ \rightarrow except first and last layers are 32-bit float
- β_i determined by the l_1 -norm of all activations across channels **for given position i** of the input feature map
- Accuracy loss: **11%** on AlexNet

Hardware needs to support both activation precisions

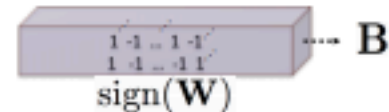
Scale factors (α, β_i) can change per layer or position in filter

XNOR-Net

(1) Binarizing Weight

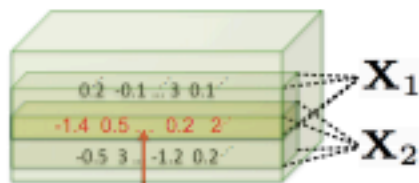


$$\frac{1}{n} \|W\|_{\ell_1} = \alpha$$



(2) Binarizing Input

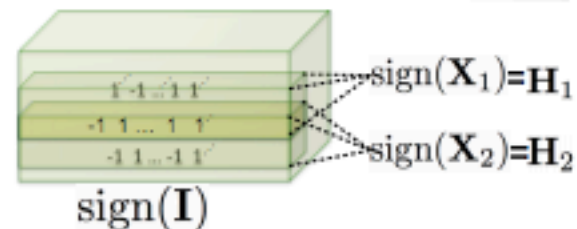
Inefficient



Redundant computations in overlapping areas

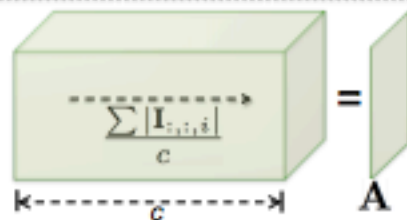
$$\frac{1}{n} \|X_1\|_{\ell_1} = \beta_1$$

$$\frac{1}{n} \|X_2\|_{\ell_1} = \beta_2$$



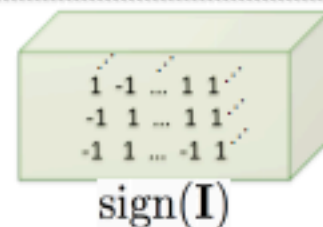
(3) Binarizing Input

Efficient

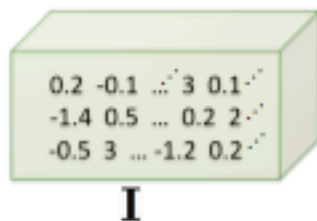


$$A * k = K$$

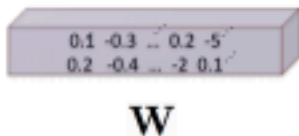
Efficient binarization process showing a matrix A with dimensions k and c , and a summation formula: $\sum |I_{i,j}| / c$



(4) Convolution with XNOR-Bitcount



*



\approx

$$\left[\begin{array}{c} \text{sign}(I) \\ \text{sign}(I) \\ \text{sign}(I) \end{array} \right] \otimes \left[\begin{array}{c} \text{sign}(W) \\ \text{sign}(W) \\ \text{sign}(W) \end{array} \right] \odot K \odot \alpha$$

Ternary Nets

- **Allow for weights to be zero**
 - Increase sparsity, but also increase number of bits (2-bits)
- **Ternary Weight Nets (TWN)** [Li et al., arXiv 2016]
 - Weights $\{-w, 0, w\}$ \rightarrow except first and last layers are 32-bit float
 - Activations: 32-bit float
 - Accuracy loss: **3.7%** on AlexNet
- **Trained Ternary Quantization (TTQ)** [Zhu et al., ICLR 2017]
 - Weights $\{-w_1, 0, w_2\}$ \rightarrow except first and last layers are 32-bit float
 - Activations: 32-bit float
 - Accuracy loss: **0.6%** on AlexNet

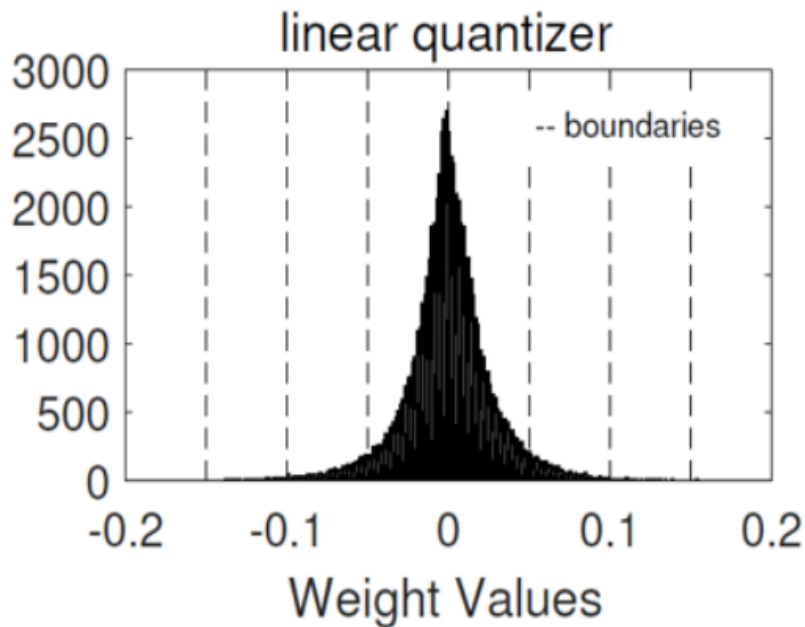
Non-Linear Quantization

- **Precision** refers to the **number of levels**
 - Number of bits = \log_2 (number of levels)
- **Quantization:** mapping data to a smaller set of **levels**
 - Linear, e.g., fixed-point
 - Non-linear
 - Computed
 - Table lookup

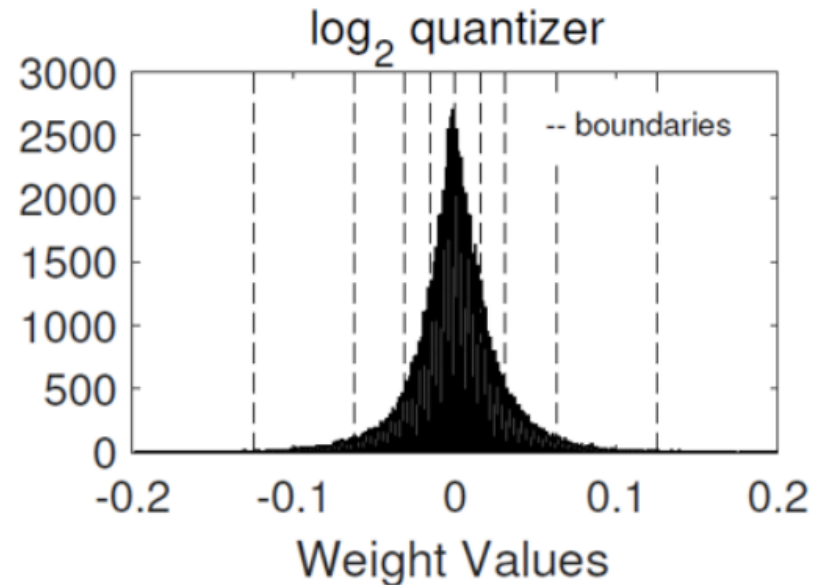
Objective: Reduce size to improve speed and/or reduce energy while preserving accuracy

Computed Non-linear Quantization

Log Domain Quantization



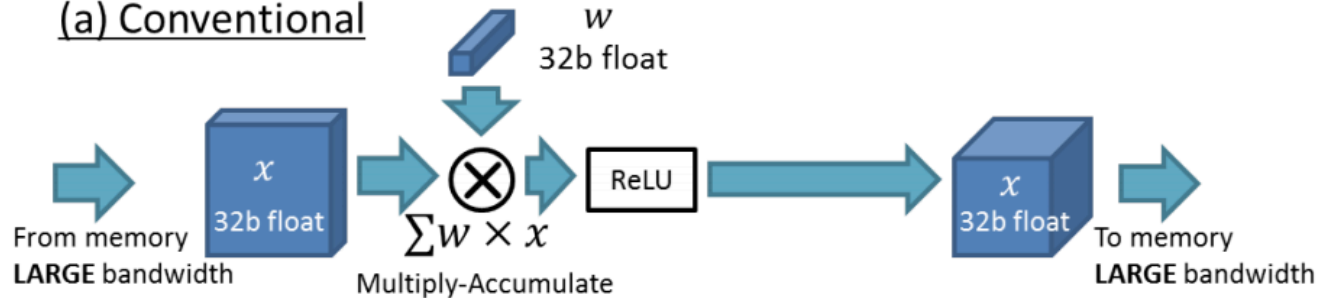
$$\text{Product} = X * W$$



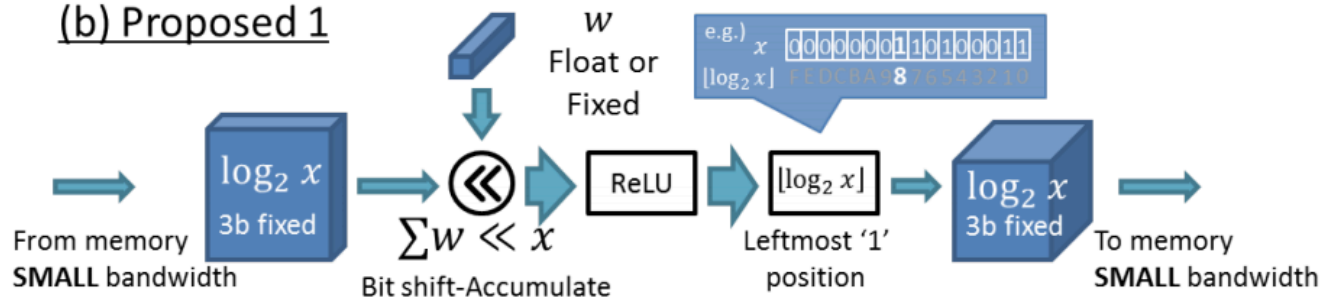
$$\text{Product} = X \ll W$$

Log Domain Computation

(a) Conventional

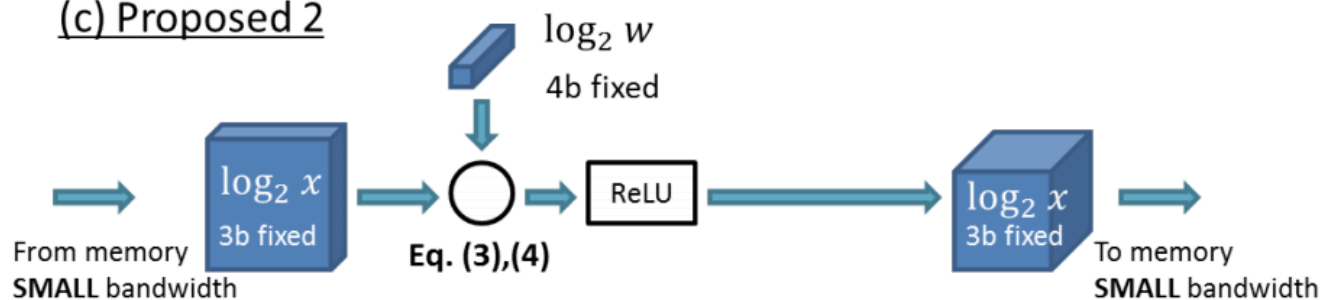


(b) Proposed 1



Only activation
in log domain

(c) Proposed 2



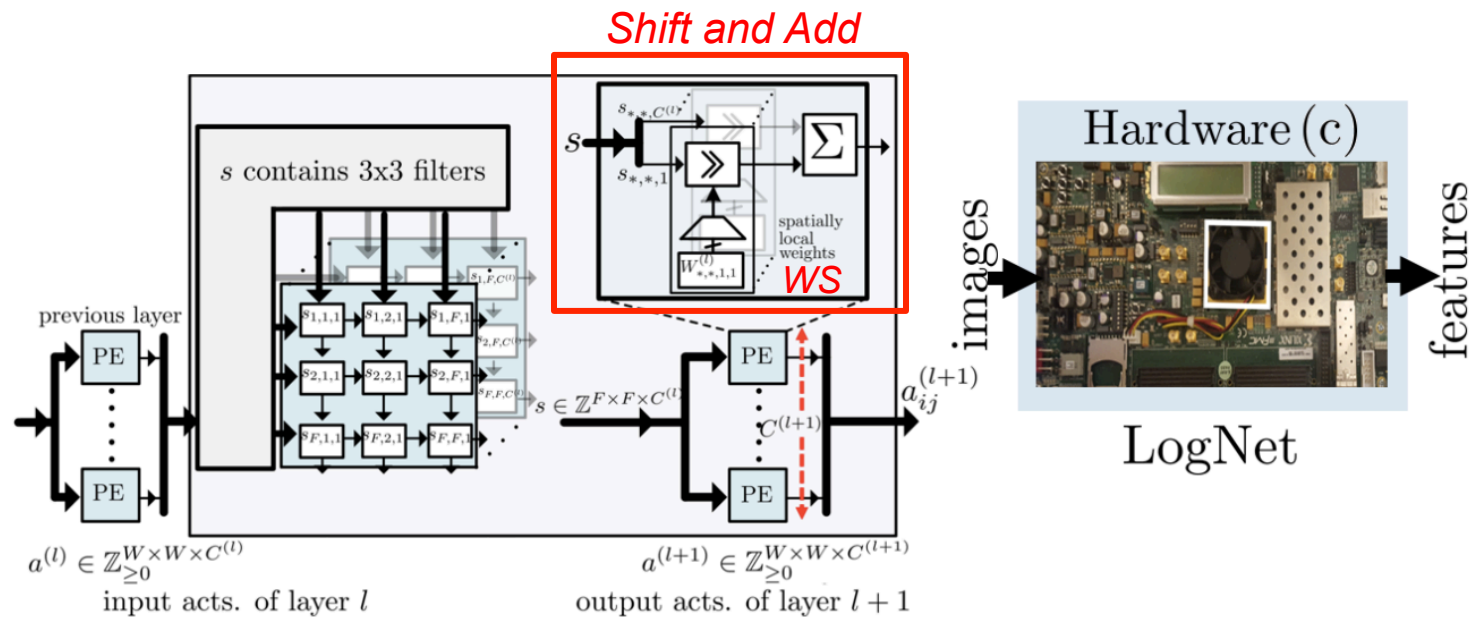
Both weights
and activations
in log domain

max, bitshifts, adds/subs

[Miyashita et al., arXiv 2016]

Log Domain Quantization

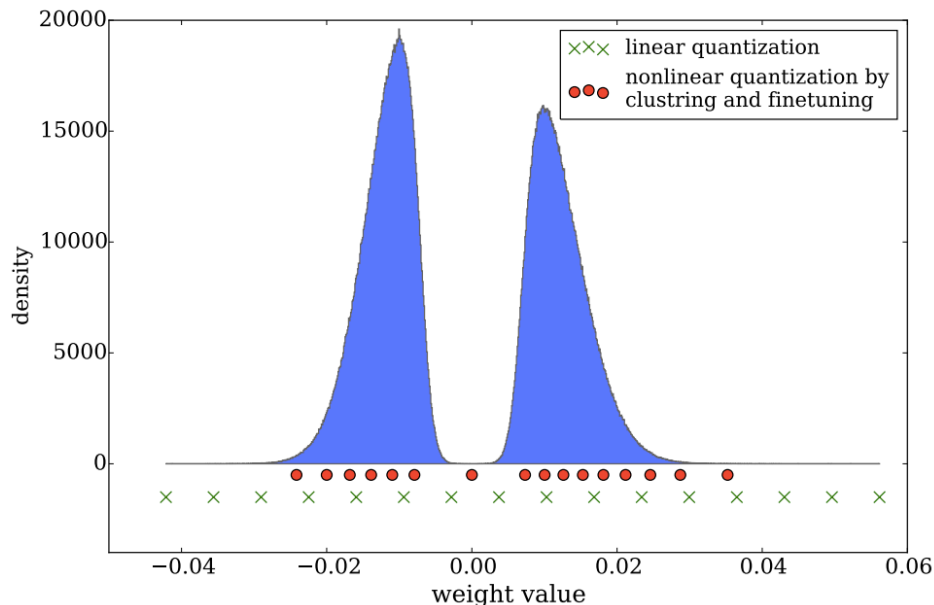
- **Weights: 5-bits for CONV, 4-bit for FC; Activations: 4-bits**
- Accuracy loss: **3.2%** on AlexNet



[Miyashita et al., arXiv 2016],
 [Lee et al., LogNet, ICASSP 2017]

Reduce Precision Overview

- **Learned mapping of data to quantization levels (e.g., k-means)**



*Implement with
look up table*

[Han et al., ICLR 2016]

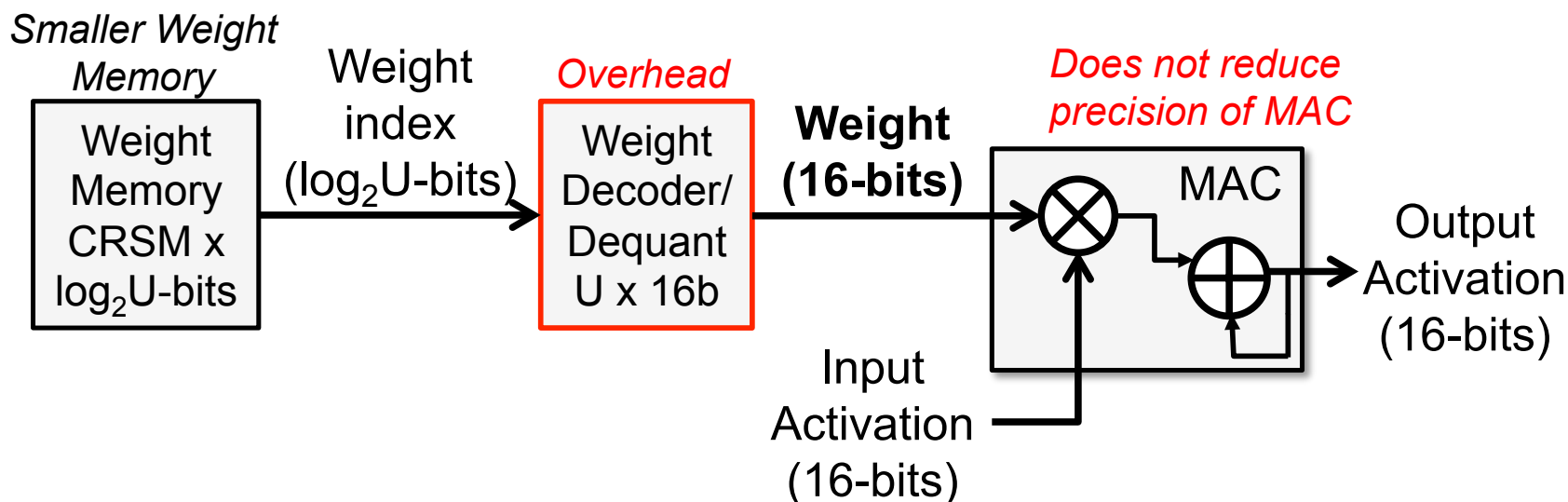
- **Additional Properties**

- **Fixed or Variable (across data types, layers, channels, etc.)**

Non-Linear Quantization Table Lookup

Trained Quantization: Find K weights via K -means clustering to reduce number of unique weights *per layer* (weight sharing)

Example: AlexNet (no accuracy loss)
256 unique weights for CONV layer
16 unique weights for FC layer



Consequences: Narrow weight memory and second access from (small) table

Summary of Reduce Precision

Category	Method	Weights (# of bits)	Activations (# of bits)	Accuracy Loss vs. 32-bit float (%)
Dynamic Fixed Point	w/o fine-tuning	8	10	0.4
	w/ fine-tuning	8	8	0.6
Reduce weight	Ternary weights Networks (TWN)	2*	32	3.7
	Trained Ternary Quantization (TTQ)	2*	32	0.6
	Binary Connect (BC)	1	32	19.2
	Binary Weight Net (BWN)	1*	32	0.8
Reduce weight and activation	Binarized Neural Net (BNN)	1	1	29.8
	XNOR-Net	1*	1	11
Non-Linear	LogNet	5(conv), 4(fc)	4	3.2
	Weight Sharing	8(conv), 4(fc)	16	0

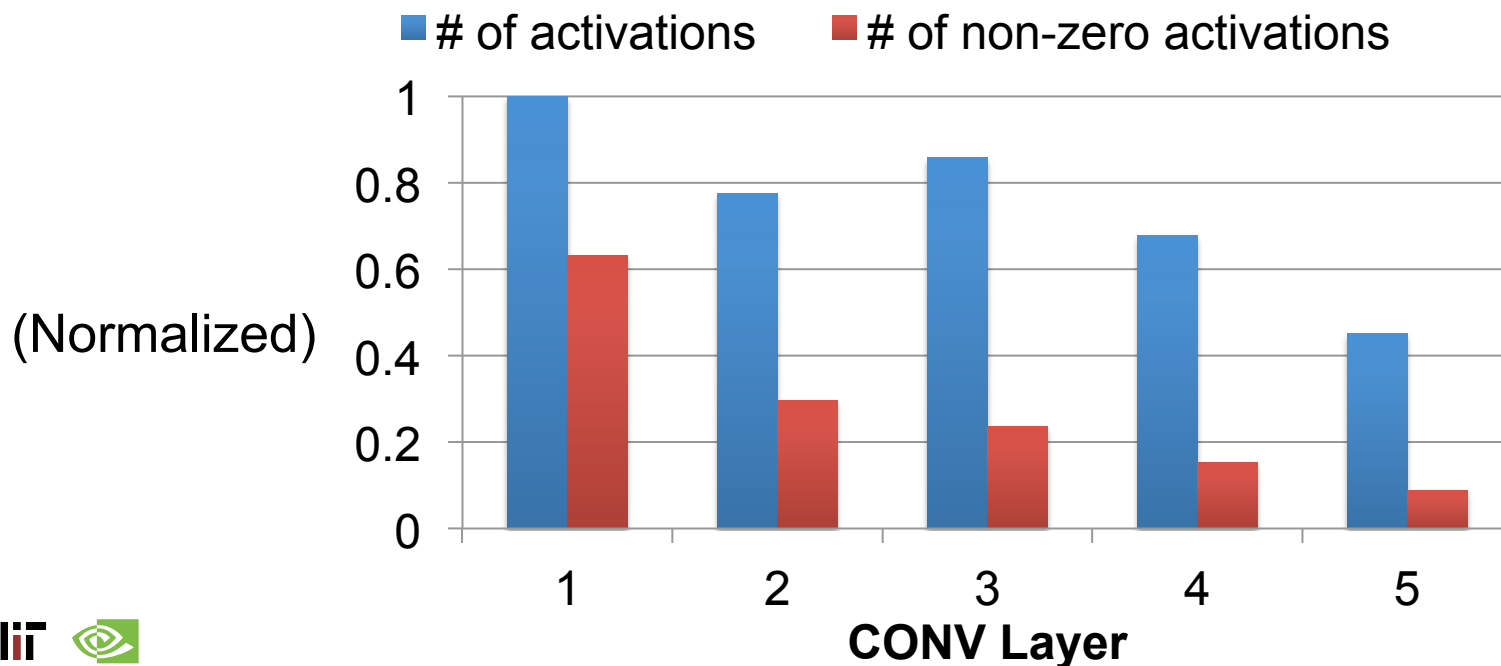
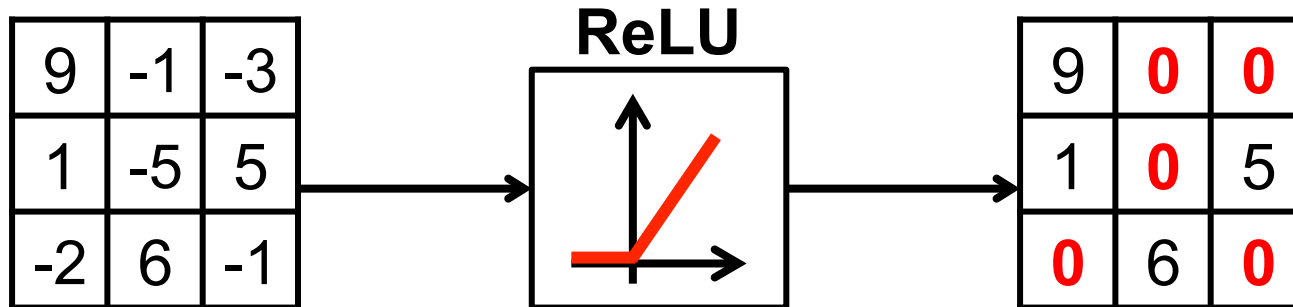
* first and last layers are 32-bit float

Reduce Number of Ops and Weights

- **Exploit Activation Statistics**
- **Network Pruning**
- **Compact Network Architectures**
- **Knowledge Distillation**

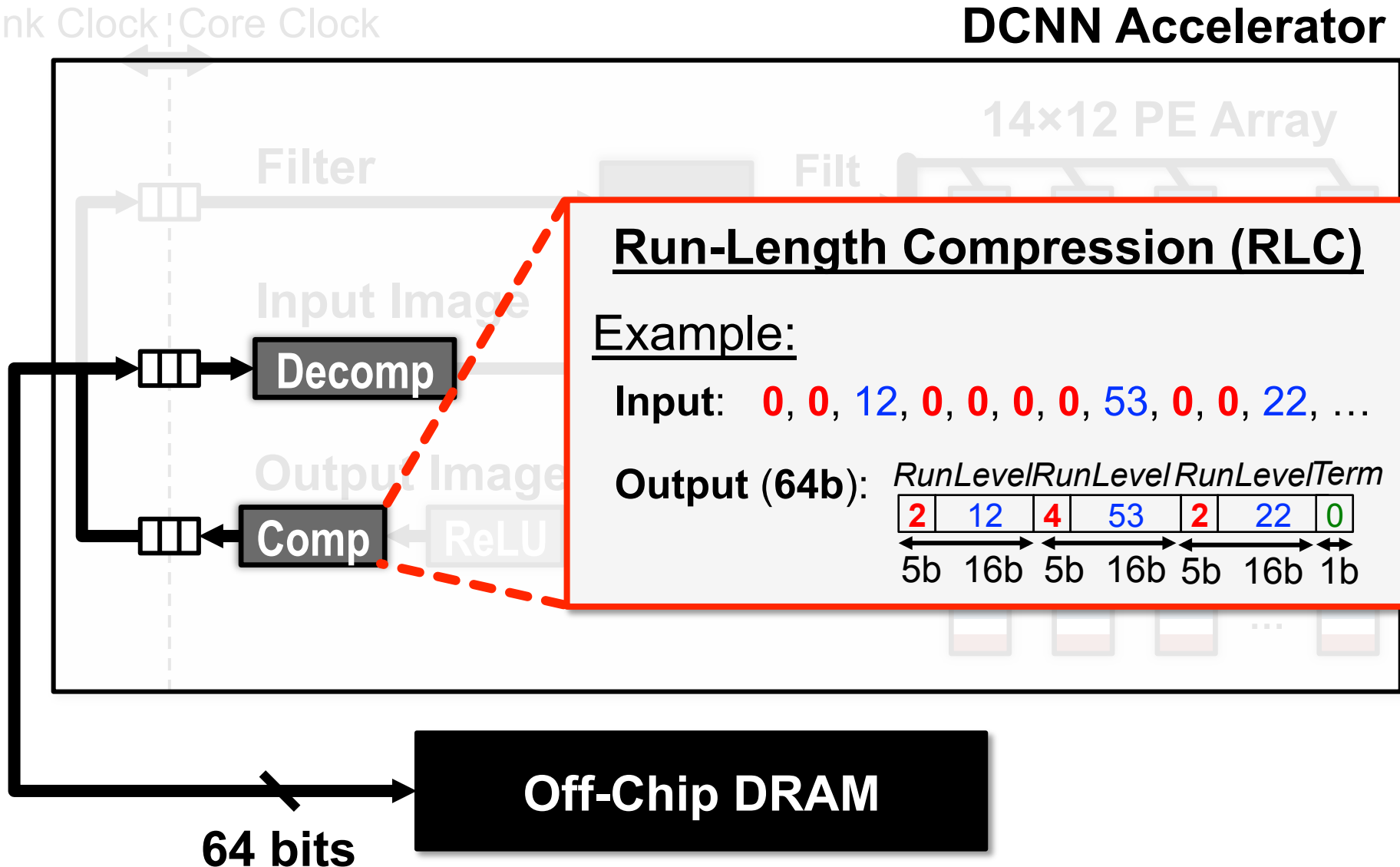
Sparsity in Fmaps

Many **zeros** in output fmaps after **ReLU**



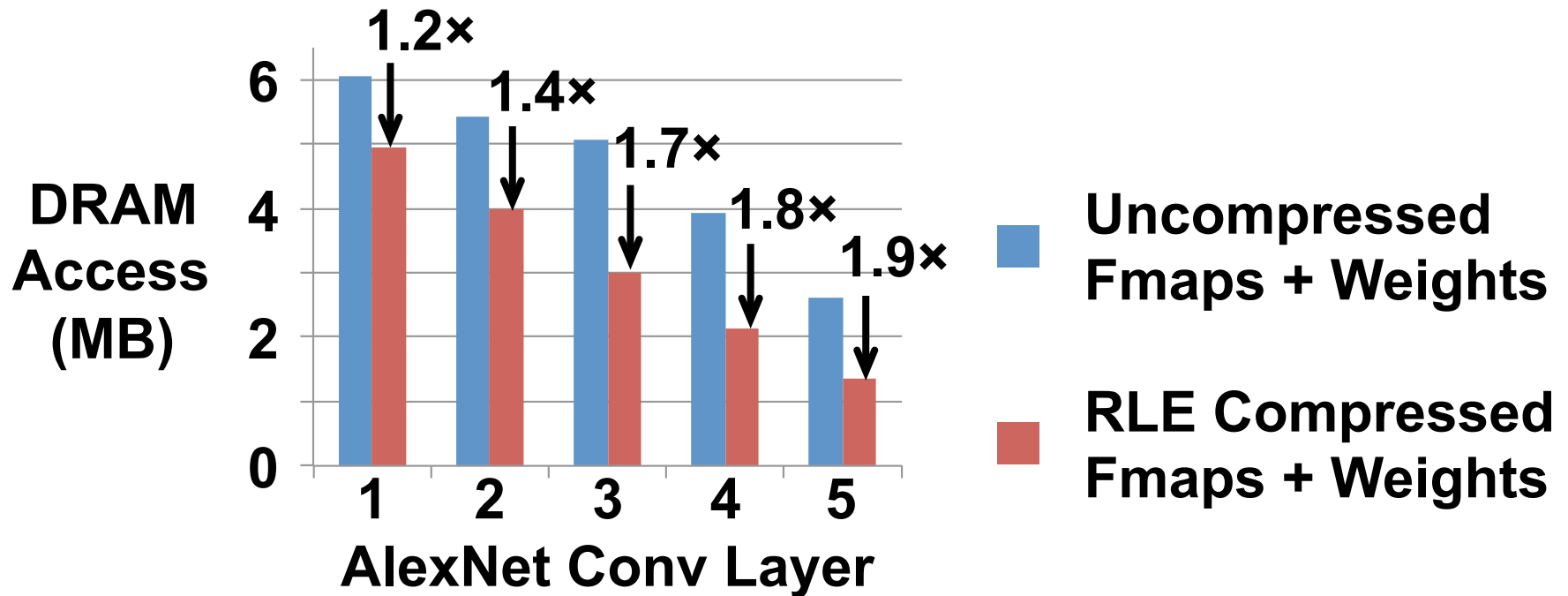
I/O Compression in Eyeriss

DCNN Accelerator



[Chen et al., ISSCC 2016]

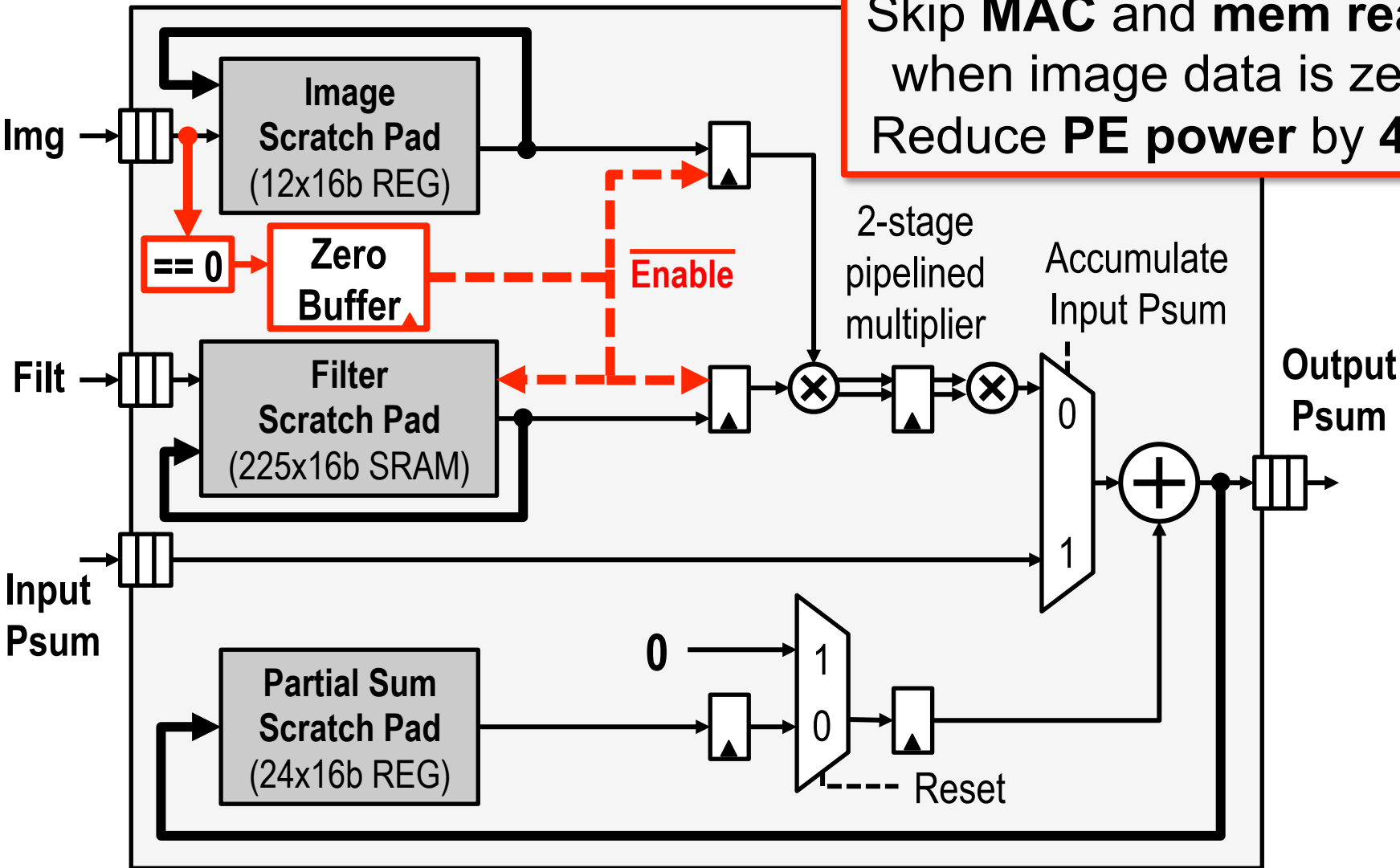
Compression Reduces DRAM BW



Simple RLC within 5% - 10% of theoretical entropy limit

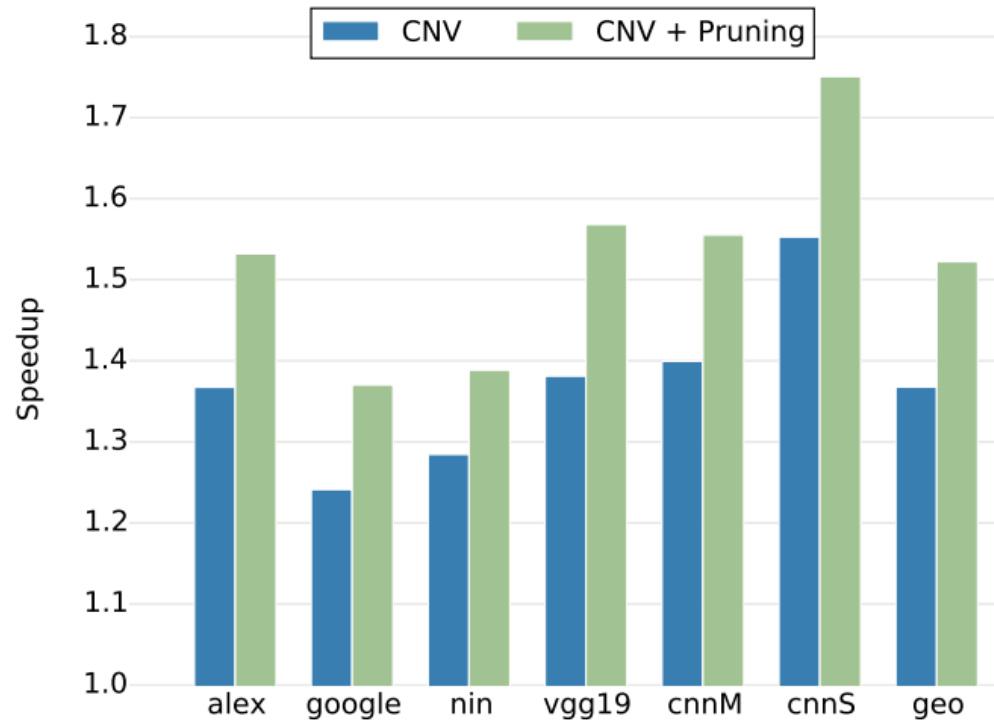
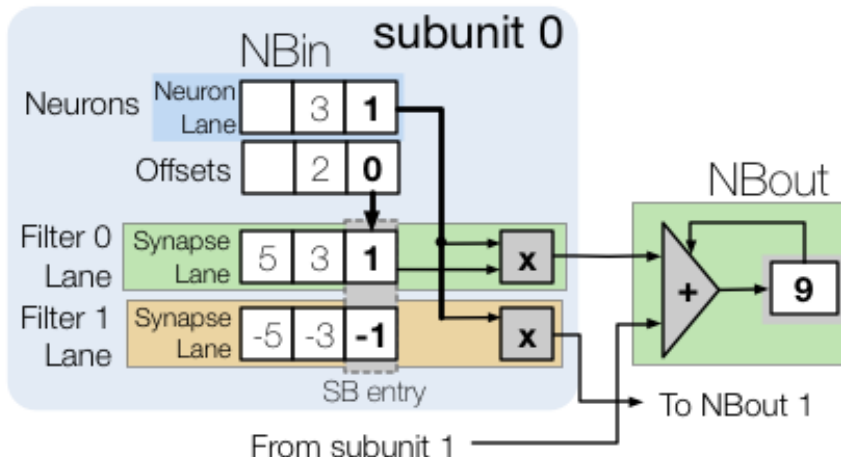
Data Gating / Zero Skipping in Eyeriss

Skip **MAC** and mem reads when image data is zero. Reduce **PE power by 45%**



Cnvlutin

- Process Convolution Layers
- Built on top of DaDianNao (4.49% area overhead)
- Speed up of 1.37x (1.52x with activation pruning)



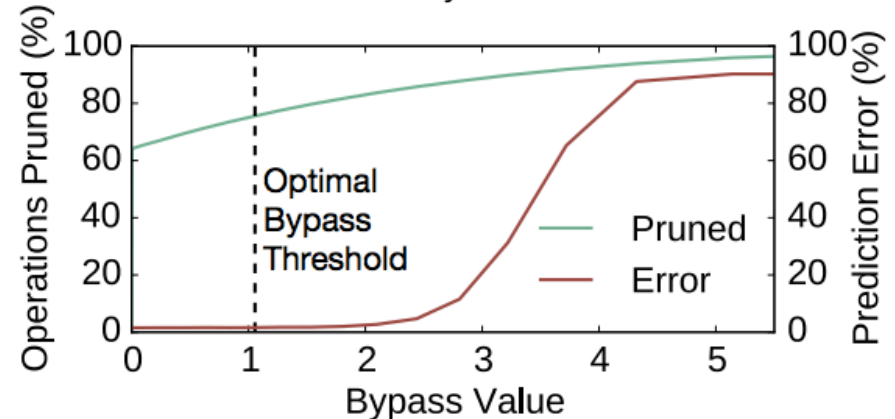
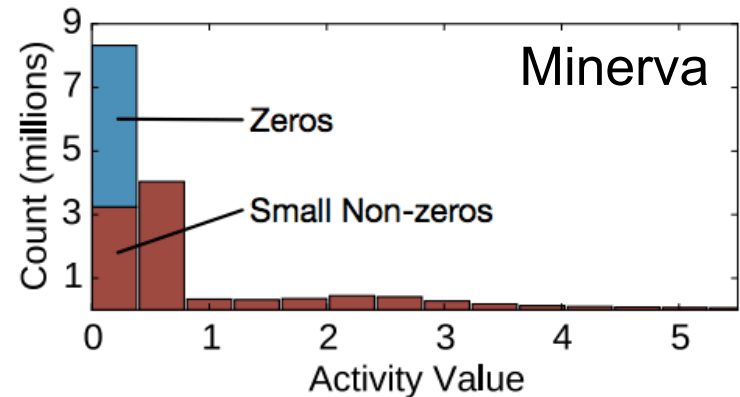
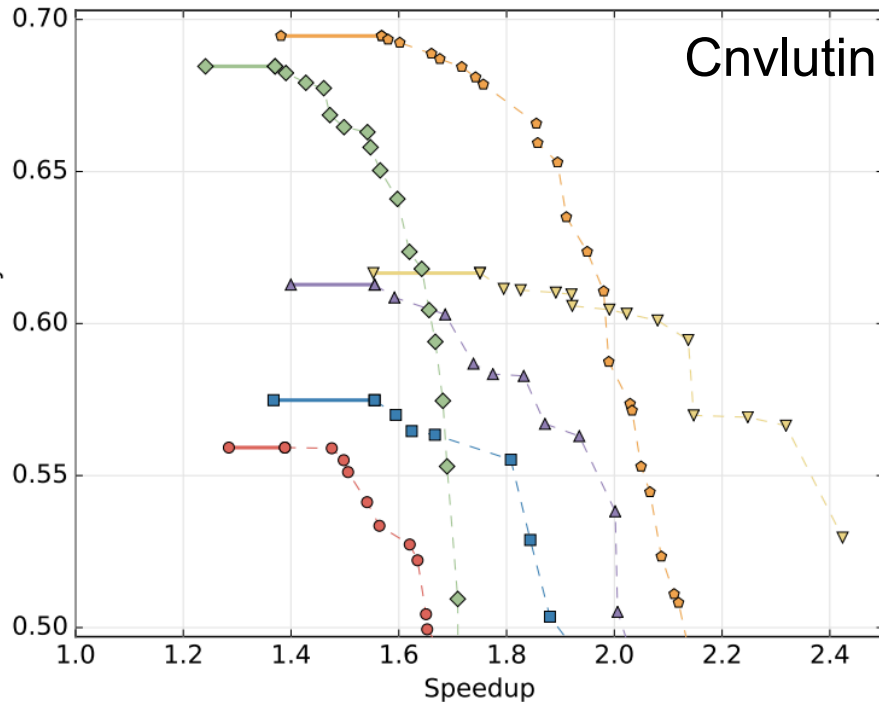
Pruning Activations

Remove small activation values

Speed up 11% (ImageNet)

Reduce power 2x (MNIST)

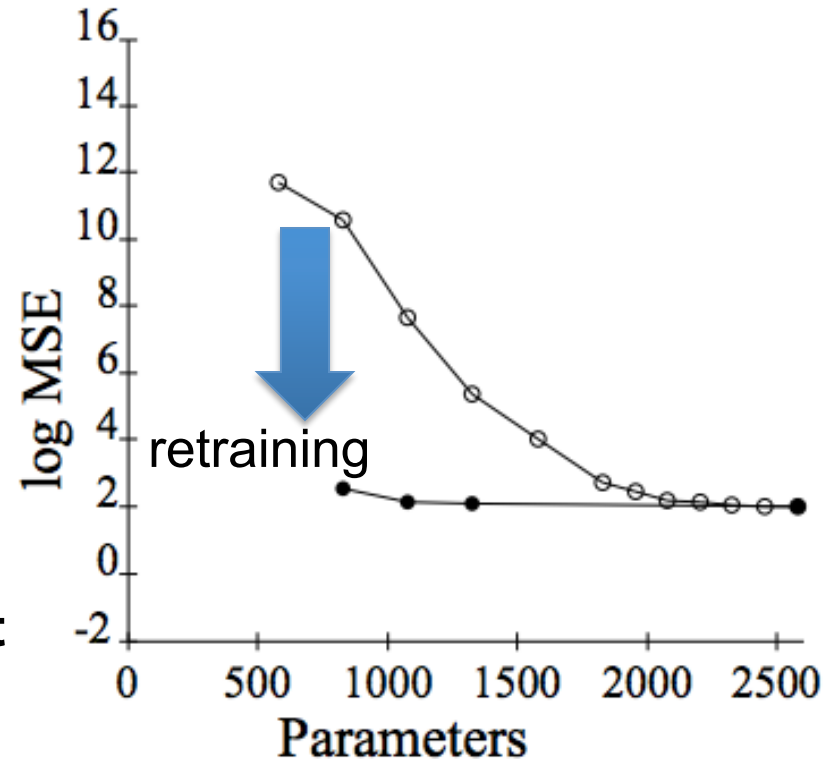
alex google nin vgg19 cnnM cnnS



Pruning – Make Weights Sparse

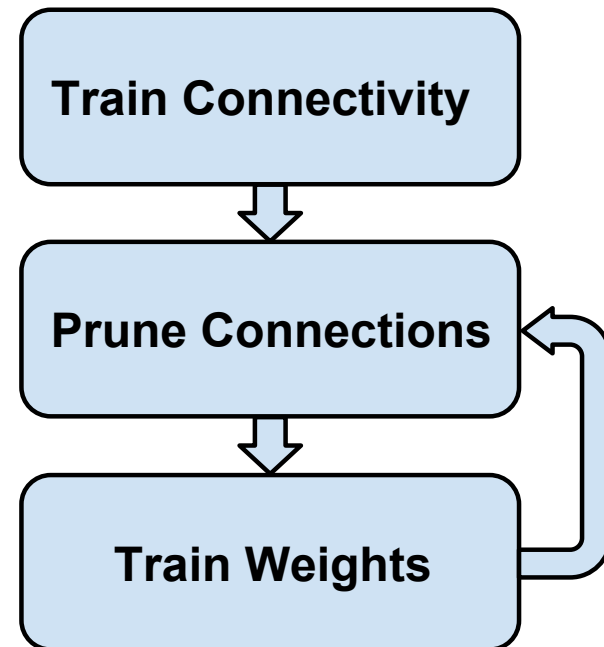
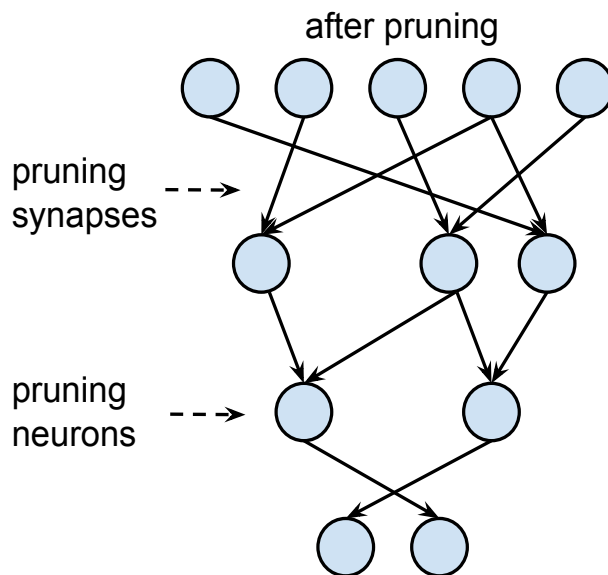
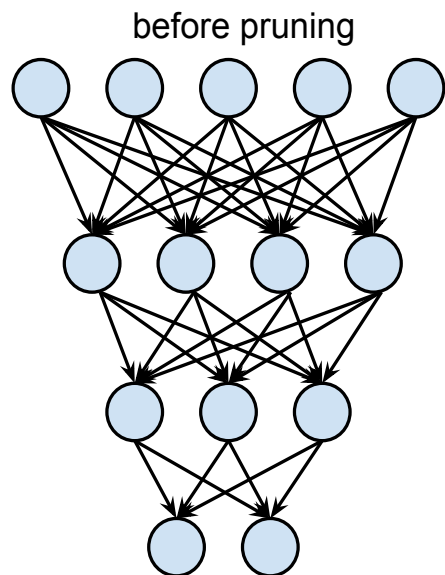
- **Optimal Brain Damage**

1. Choose a reasonable network architecture
2. Train network until reasonable solution obtained
3. Compute the second derivative for each weight
4. Compute saliencies (i.e. impact on training error) for each weight
5. Sort weights by saliency and delete low-saliency weights
6. Iterate to step 2



Pruning – Make Weights Sparse

Prune based on *magnitude* of weights



Example: AlexNet

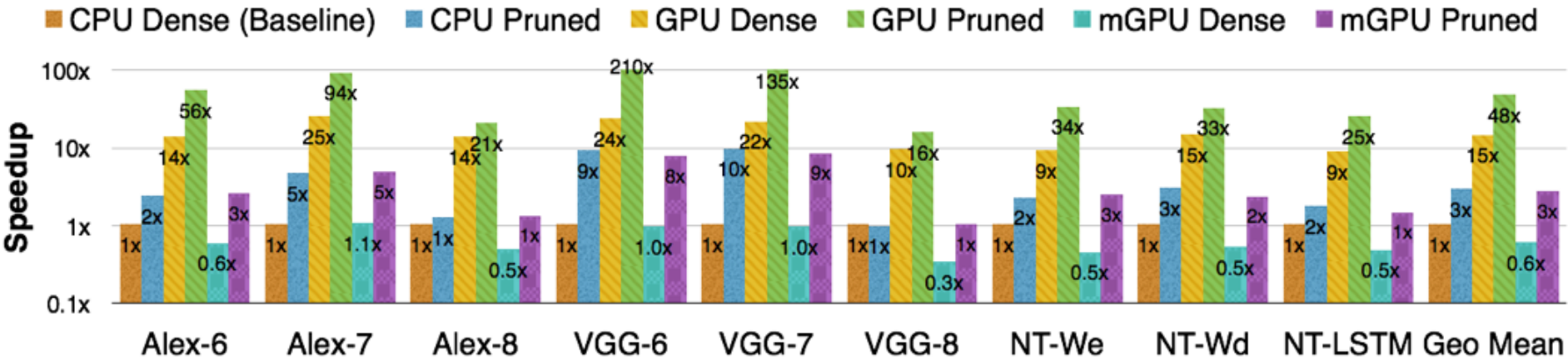
Weight Reduction: CONV layers 2.7x, FC layers 9.9x
(Most reduction on fully connected layers)

Overall: 9x weight reduction, 3x MAC reduction

Speed up of Weight Pruning on CPU/GPU

On Fully Connected Layers

Average Speed up of 3.2x on GPU, 3x on CPU, 5x on mGPU



Intel Core i7 5930K: MKL CBLAS GEMV, MKL SPBLAS CSRMMV
NVIDIA GeForce GTX Titan X: cuBLAS GEMV, cuSPARSE CSRMMV
NVIDIA Tegra K1: cuBLAS GEMV, cuSPARSE CSRMMV

Batch size = 1



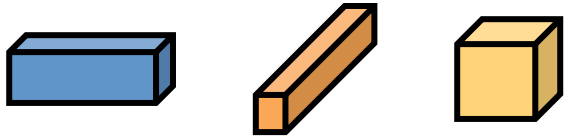
Key Metrics for Embedded DNN

- **Accuracy** → Measured on Dataset
- **Speed** → Number of MACs
- **Storage Footprint** → Number of Weights
- **Energy** → ?

Energy-Aware Pruning

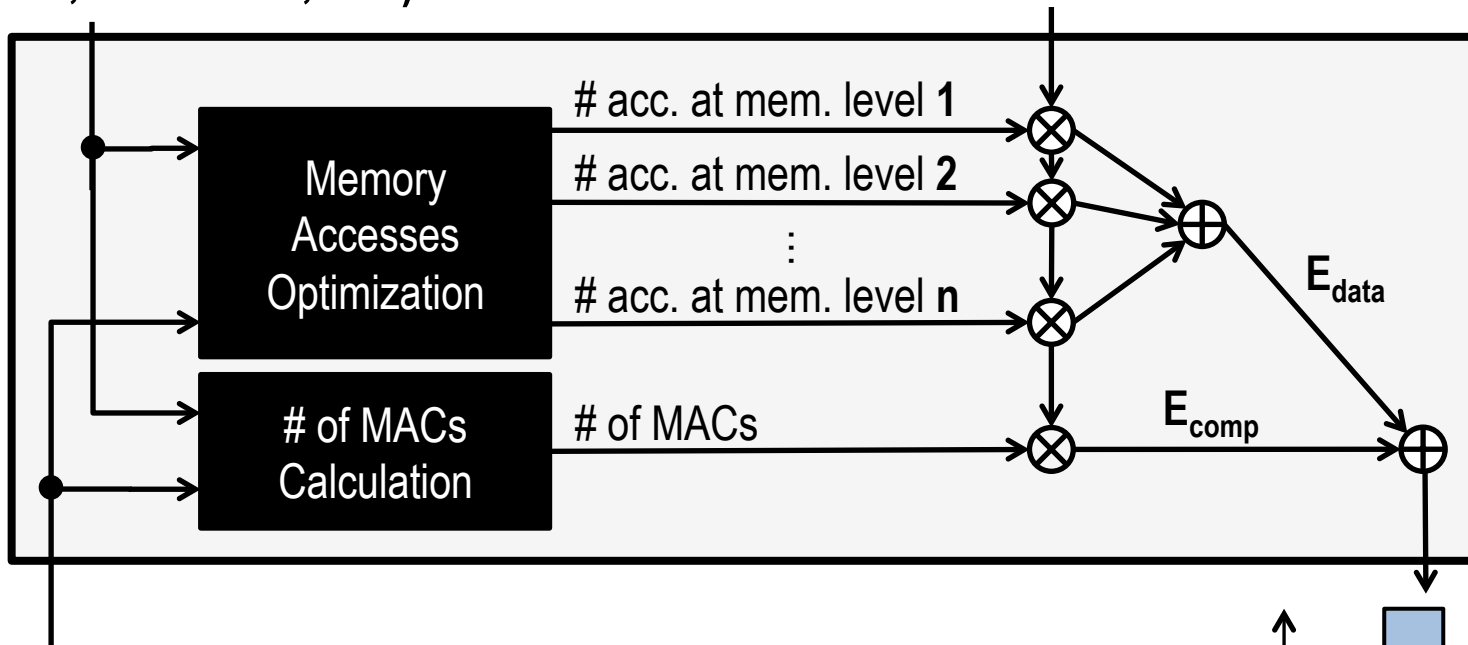
- **# of Weights alone is not a good metric for energy**
 - **Example (AlexNet):**
 - # of Weights (FC Layer) > # of Weights (CONV layer)
 - Energy (FC Layer) < Energy (CONV layer)
- **Use energy evaluation method to estimate DNN energy**
 - **Account for data movement**

Energy-Evaluation Methodology



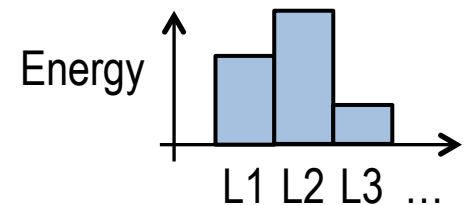
CNN Shape Configuration
(# of channels, # of filters, etc.)

Hardware Energy Costs of each
MAC and Memory Access



CNN Weights and Input Data

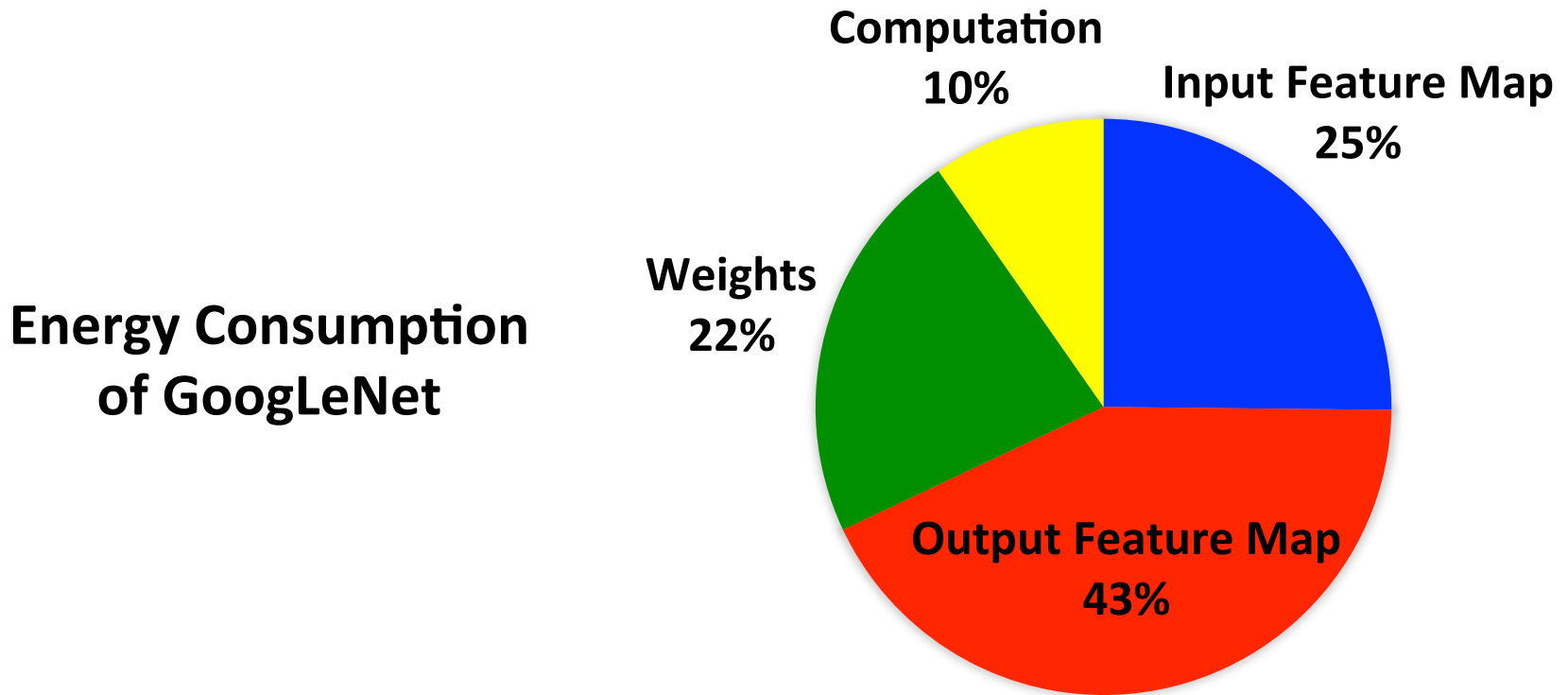
[0.3, 0, -0.4, 0.7, 0, 0, 0.1, ...]



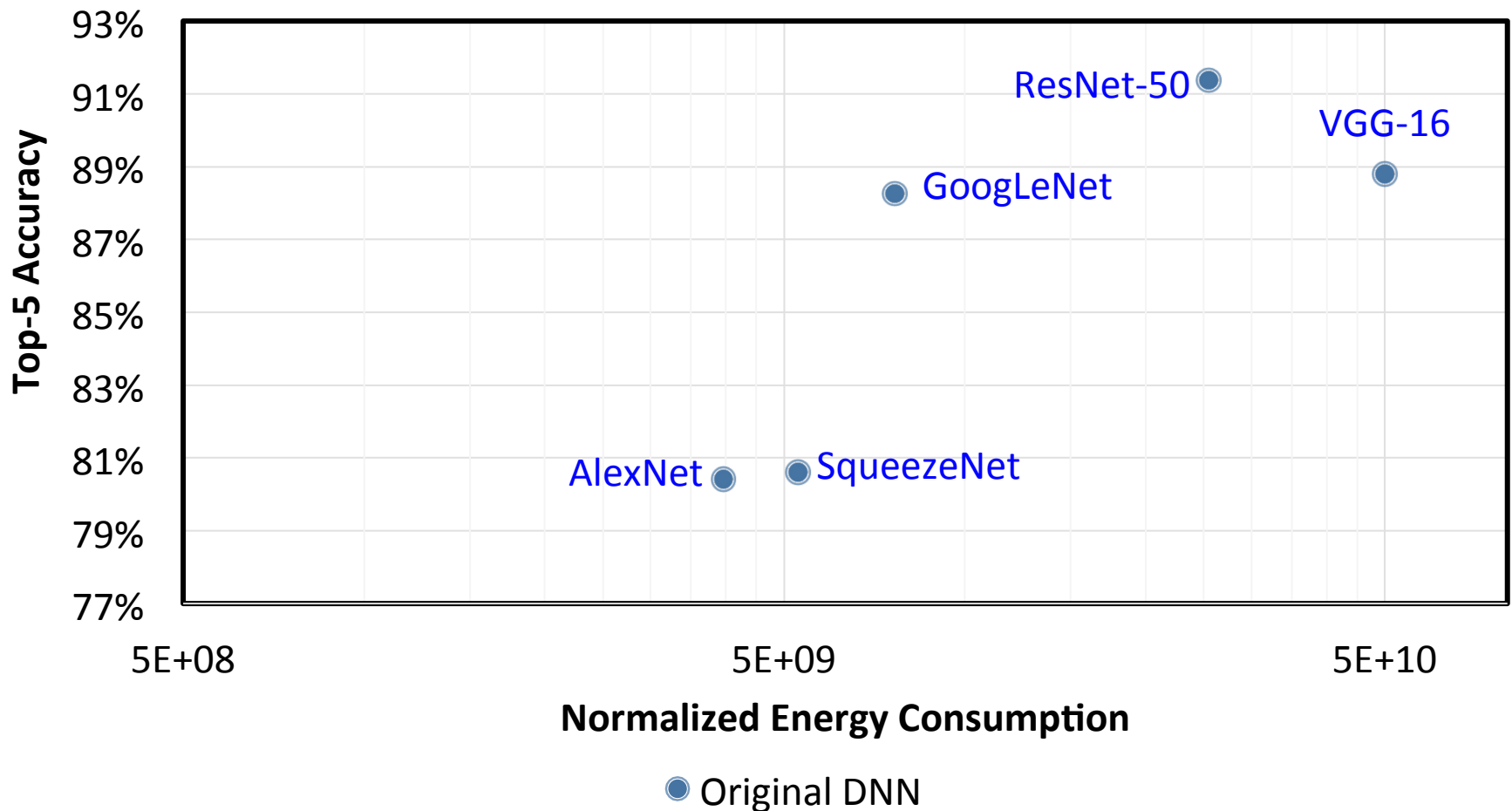
CNN Energy Consumption

Key Observations

- Number of weights ***alone*** is not a good metric for energy
- **All data types** should be considered

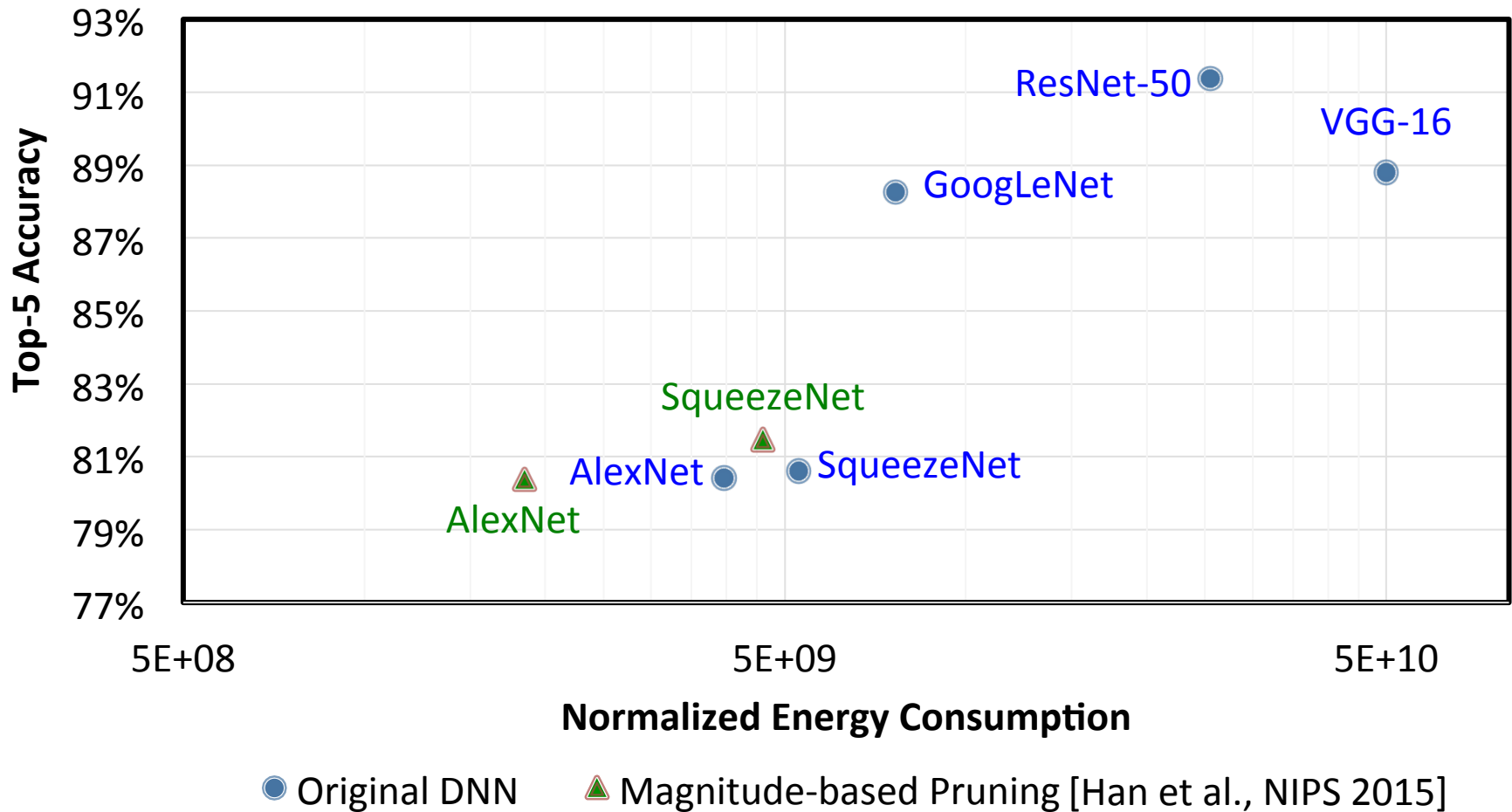


Energy Consumption of Existing DNNs



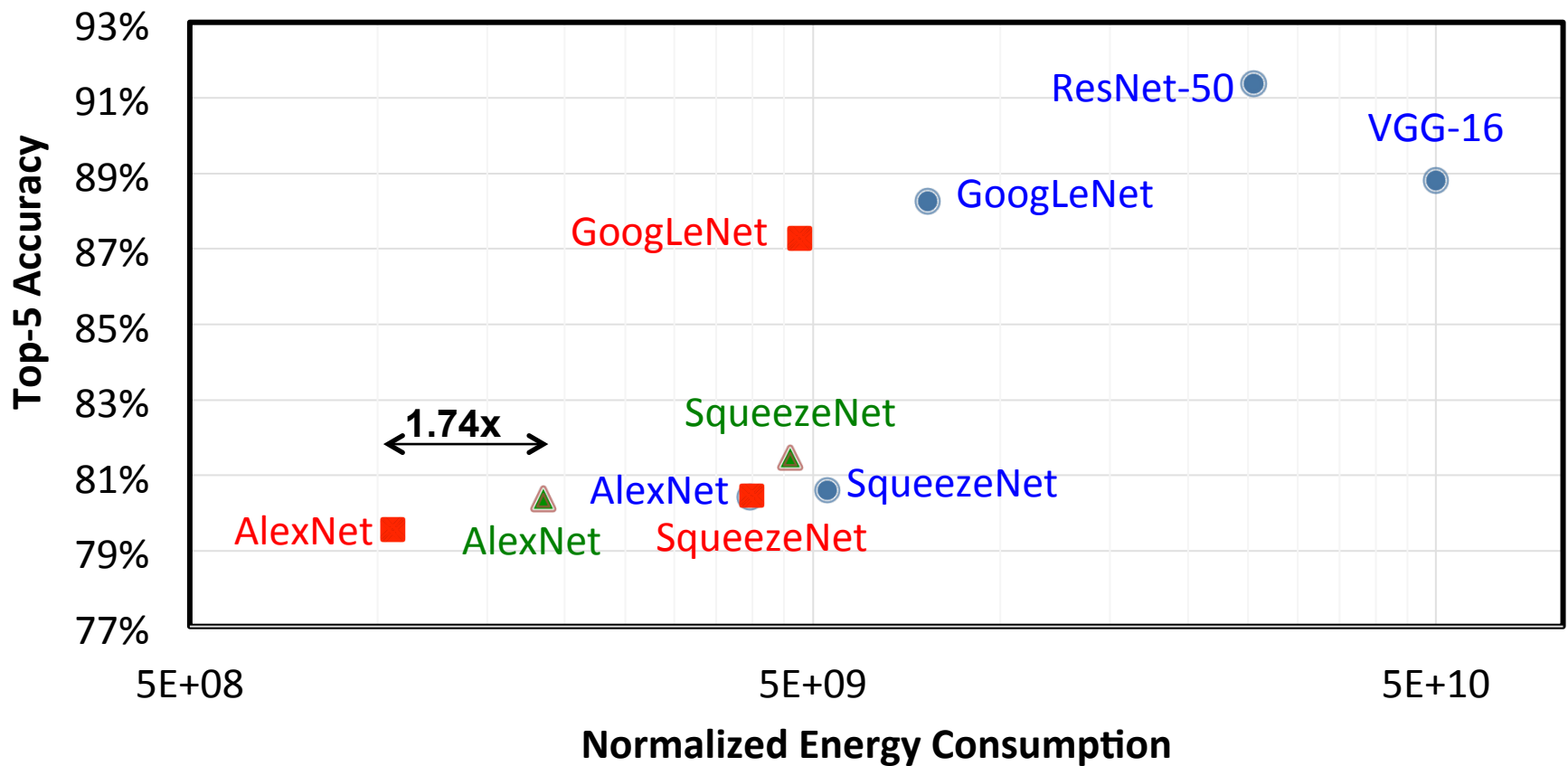
Deeper CNNs with fewer weights do not necessarily consume less energy than shallower CNNs with more weights

Magnitude-based Weight Pruning



Reduce number of weights by **removing small magnitude weights**

Energy-Aware Pruning



● Original DNN ▲ Magnitude-based Pruning ■ Energy-aware Pruning (This Work)

Remove weights from layers in order of highest to lowest energy
3.7x reduction in AlexNet / 1.6x reduction in GoogLeNet

Compression of Weights & Activations

- Compress weights and activations between DRAM and accelerator
- Variable Length / Huffman Coding

Example:

Value: **16'b0** → Compressed Code: {**1'b0**}

Value: **16'bx** → Compressed Code: {**1'b1**, **16'bx**}

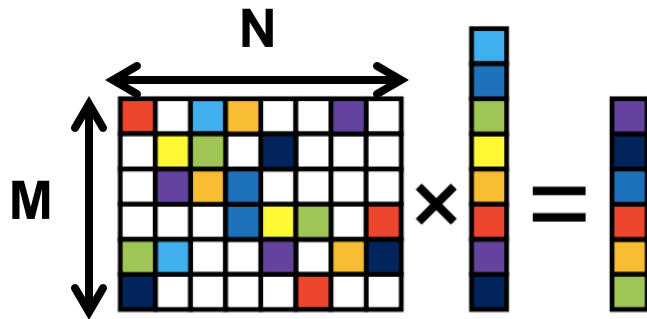
- Tested on AlexNet → **2× overall BW Reduction**

Layer	Filter / Image bits (0%)	Filter / Image BW Reduc.	IO / HuffIO (MB/frame)	Voltage (V)	MMACs/ Frame	Power (mW)	Real (TOPS/W)
General CNN	16 (0%) / 16 (0%)	1.0x		1.1	—	288	0.3
AlexNet 11	7 (21%) / 4 (29%)	1.17x / 1.3x	1 / 0.77	0.85	105	85	0.96
AlexNet 12	7 (19%) / 7 (89%)	1.15x / 5.8x	3.2 / 1.1	0.9	224	55	1.4
AlexNet 13	8 (11%) / 9 (82%)	1.05x / 4.1x	6.5 / 2.8	0.92	150	77	0.7
AlexNet 14	9 (04%) / 8 (72%)	1.00x / 2.9x	5.4 / 3.2	0.92	112	95	0.56
AlexNet 15	9 (04%) / 8 (72%)	1.00x / 2.9x	3.7 / 2.1	0.92	75	95	0.56
Total / avg.	—	—	19.8 / 10	—	—	76	0.94
LeNet-5 11	3 (35%) / 1 (87%)	1.40x / 5.2x	0.005 / 0.001	0.7	0.3	25	1.07
LeNet-5 12	4 (26%) / 6 (55%)	1.25x / 1.9x	0.050 / 0.042	0.8	1.6	35	1.75
Total / avg.	—	—	0.053 / 0.043	—	—	33	1.6

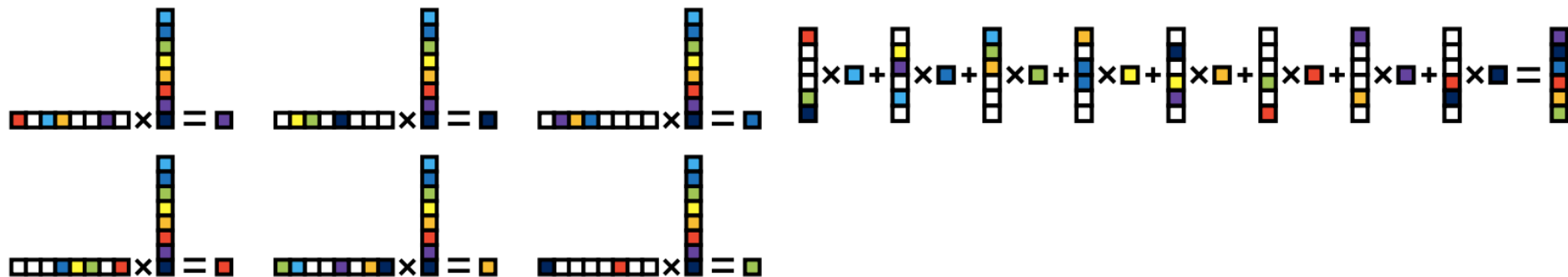
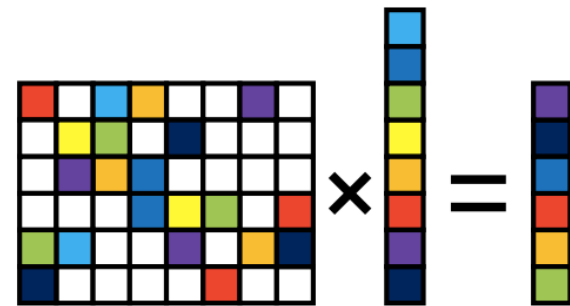
Sparse Matrix-Vector DSP

- Use **CSC** rather than **CSR** for **SpMxV**

Compressed Sparse Row (CSR)



Compressed Sparse Column (CSC)

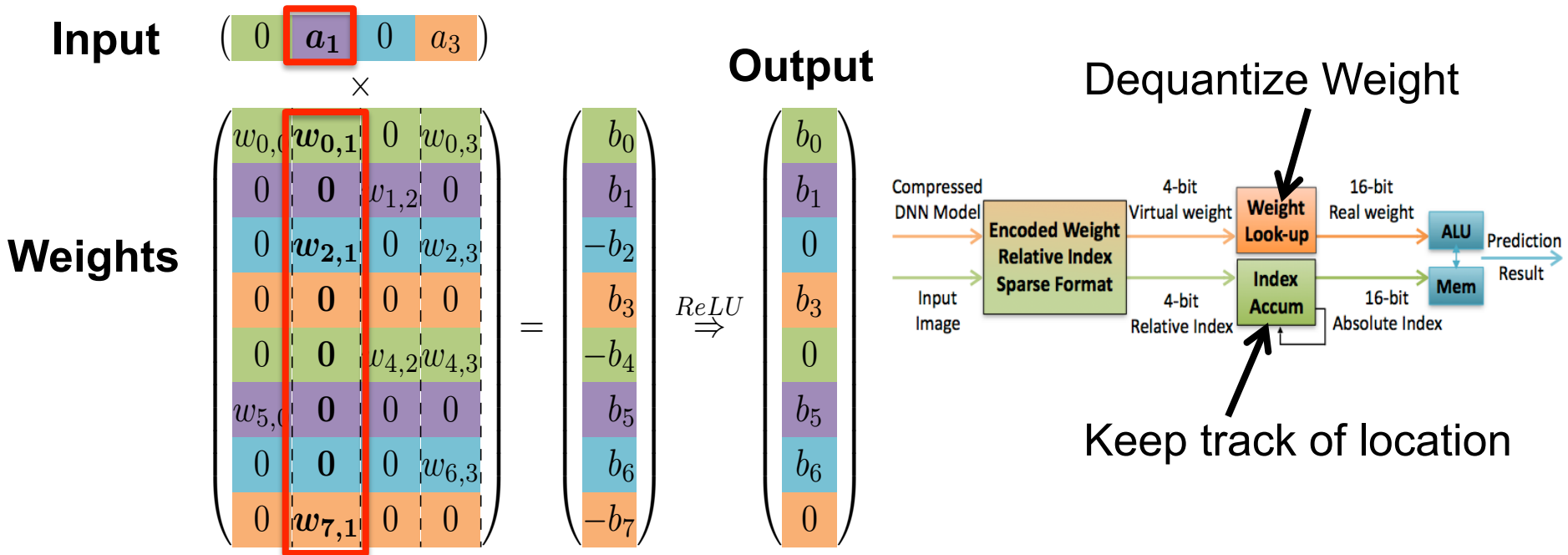


Reduce memory bandwidth by 2x (when not $M \gg N$)

For DNN, M = # of filters, N = # of weights per filter

EIE: A Sparse Linear Algebra Engine

- Process Fully Connected Layers (after Deep Compression)
- Store weights column-wise in Run Length format
 - Non-zero weights, Run-length of zeros
 - Start location of each column since variable length
- Read relative column when input is non-zero



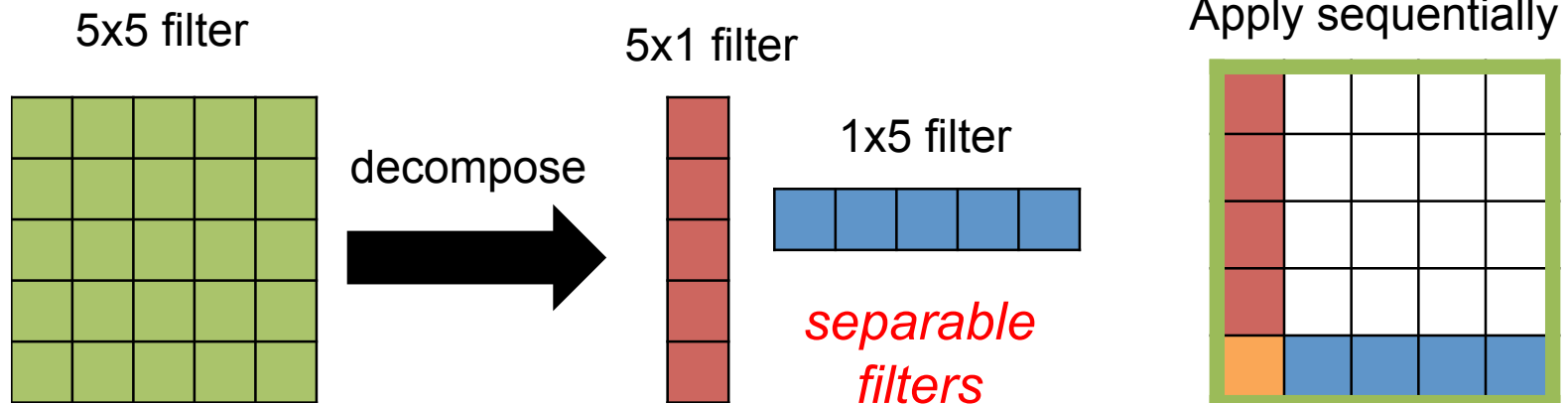
Compact Network Architectures

- **Break large convolutional layers into a series of smaller convolutional layers**
 - Fewer weights, but same effective receptive field
- **Before Training: Network Architecture Design**
- **After Training: Decompose Trained Filters**

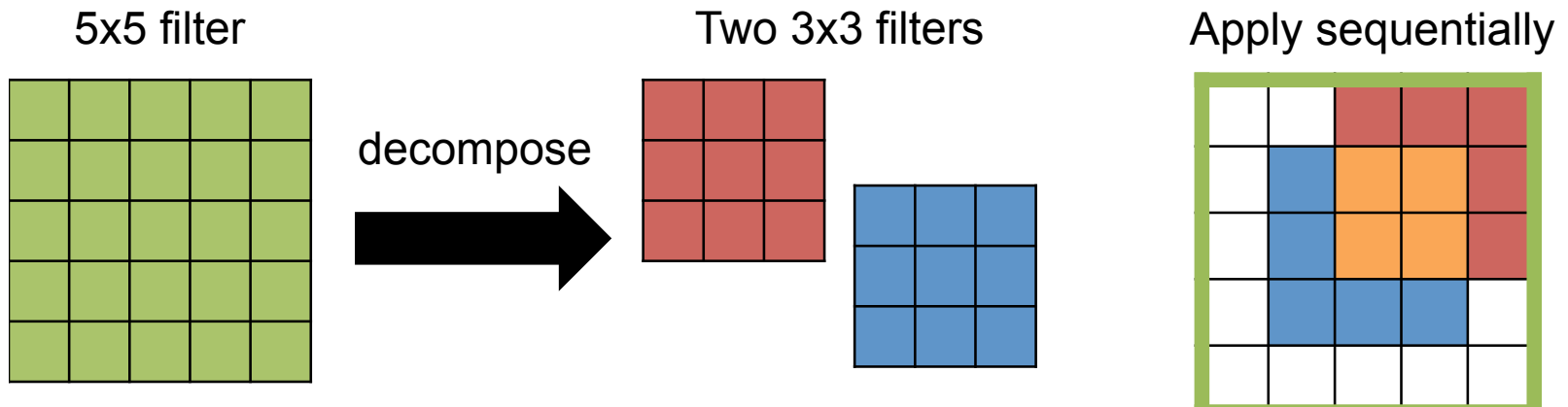
Network Architecture Design

Build Network with series of Small Filters

GoogleNet/Inception v3

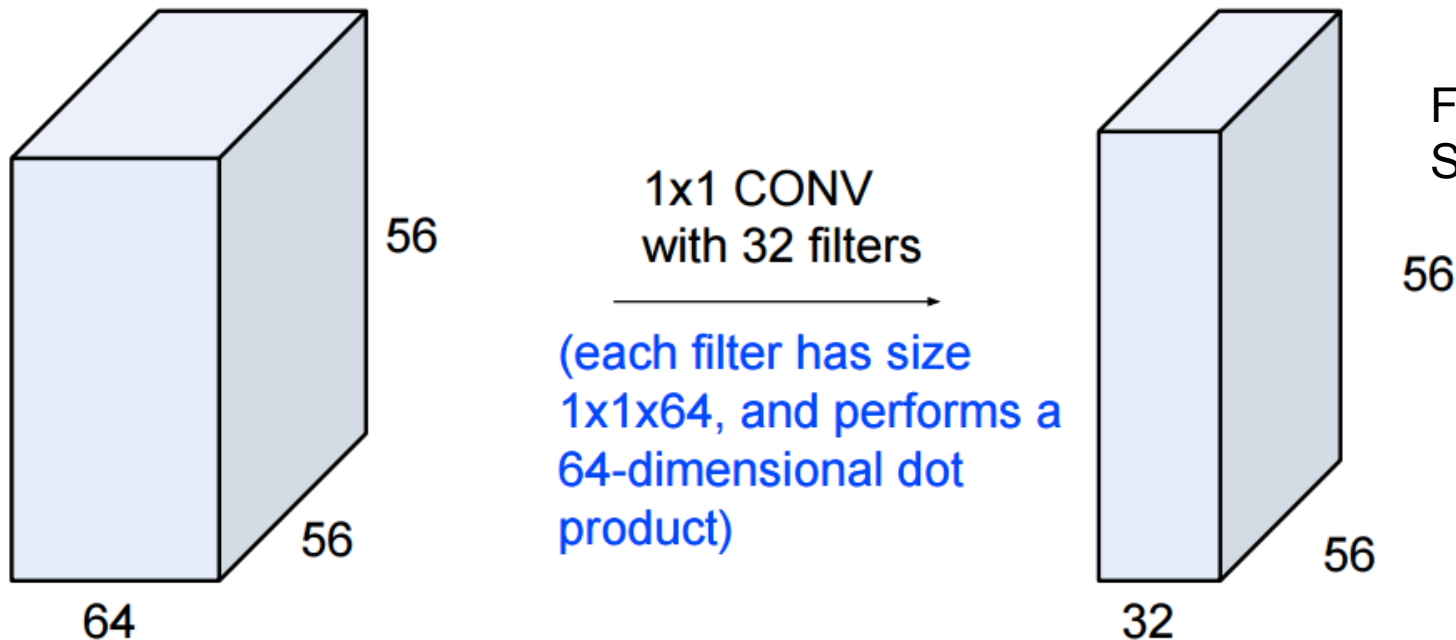


VGG-16



Network Architecture Design

Reduce size and computation with 1x1 Filter (**bottleneck**)



Used in Network In Network(NiN) and GoogLeNet

[Lin et al., ArXiv 2013 / ICLR 2014] [Szegedy et al., ArXiv 2014 / CVPR 2015]

Network Architecture Design

Reduce size and computation with 1x1 Filter (**bottleneck**)

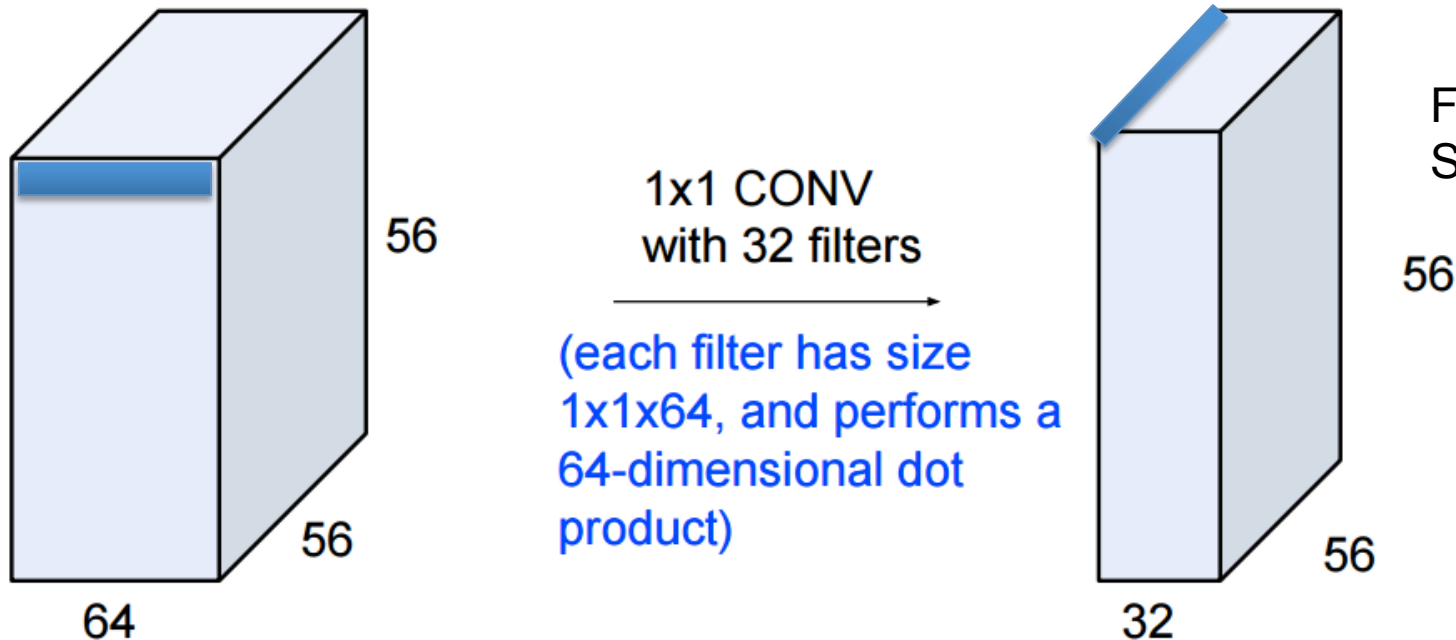


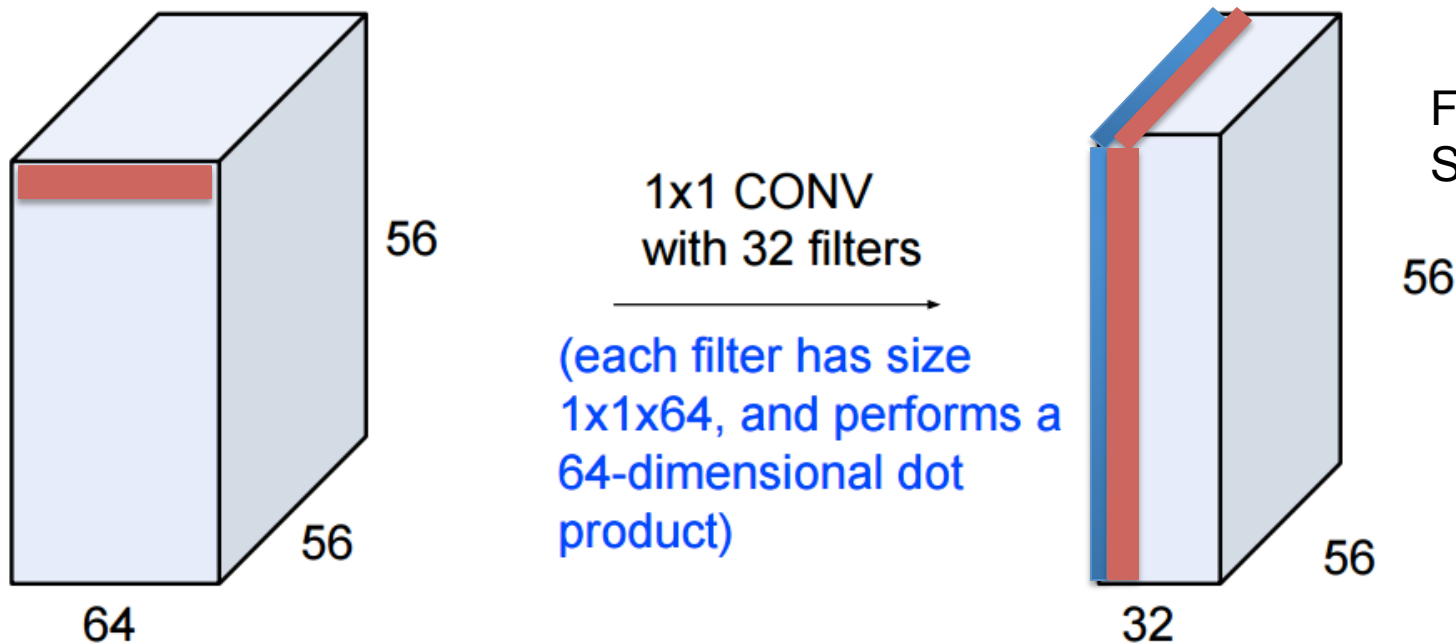
Figure Source:
Stanford cs231n

Used in Network In Network(NiN) and GoogLeNet

[Lin et al., ArXiv 2013 / ICLR 2014] [Szegedy et al., ArXiv 2014 / CVPR 2015]

Network Architecture Design

Reduce size and computation with 1x1 Filter (**bottleneck**)

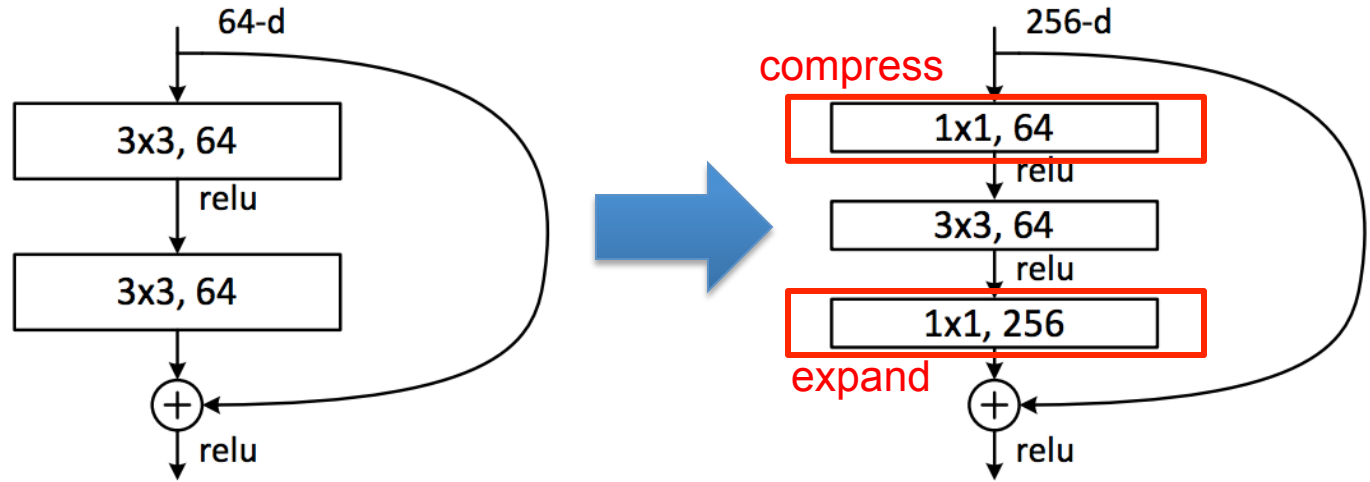


Used in Network In Network(NiN) and GoogLeNet

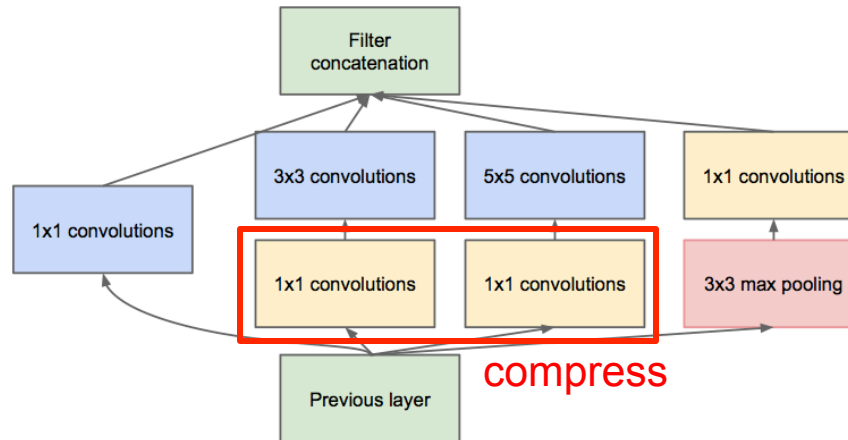
[Lin et al., ArXiv 2013 / ICLR 2014] [Szegedy et al., ArXiv 2014 / CVPR 2015]

Bottleneck in Popular DNN models

ResNet

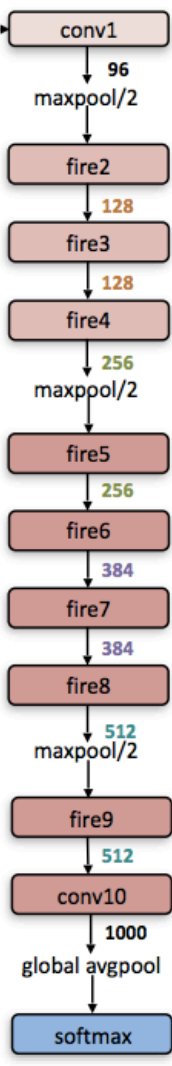
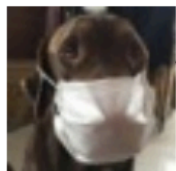


GoogleNet

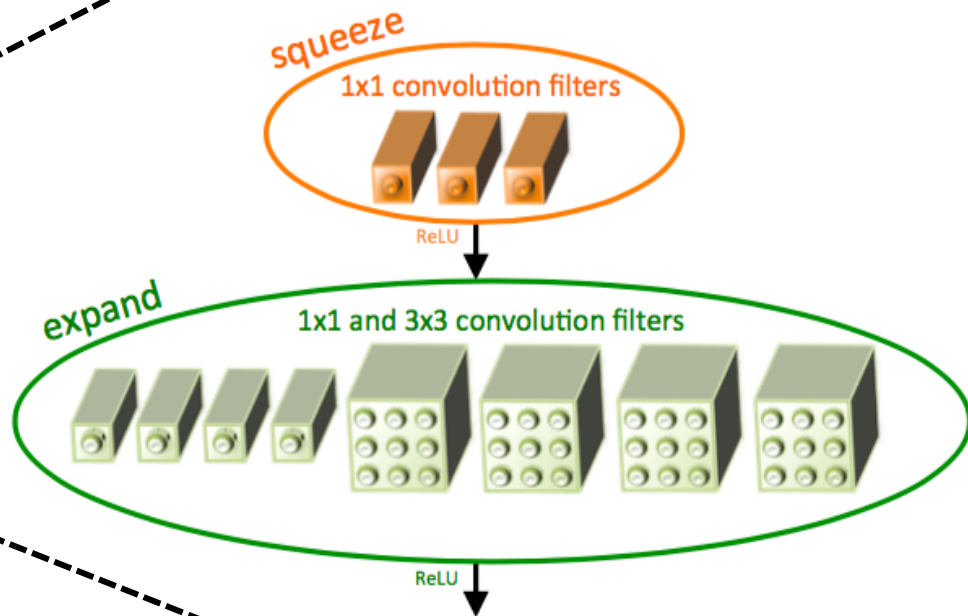


SqueezeNet

Reduce weights by reducing number of input channels by “squeezing” with 1x1
50x fewer weights than AlexNet
(no accuracy loss)

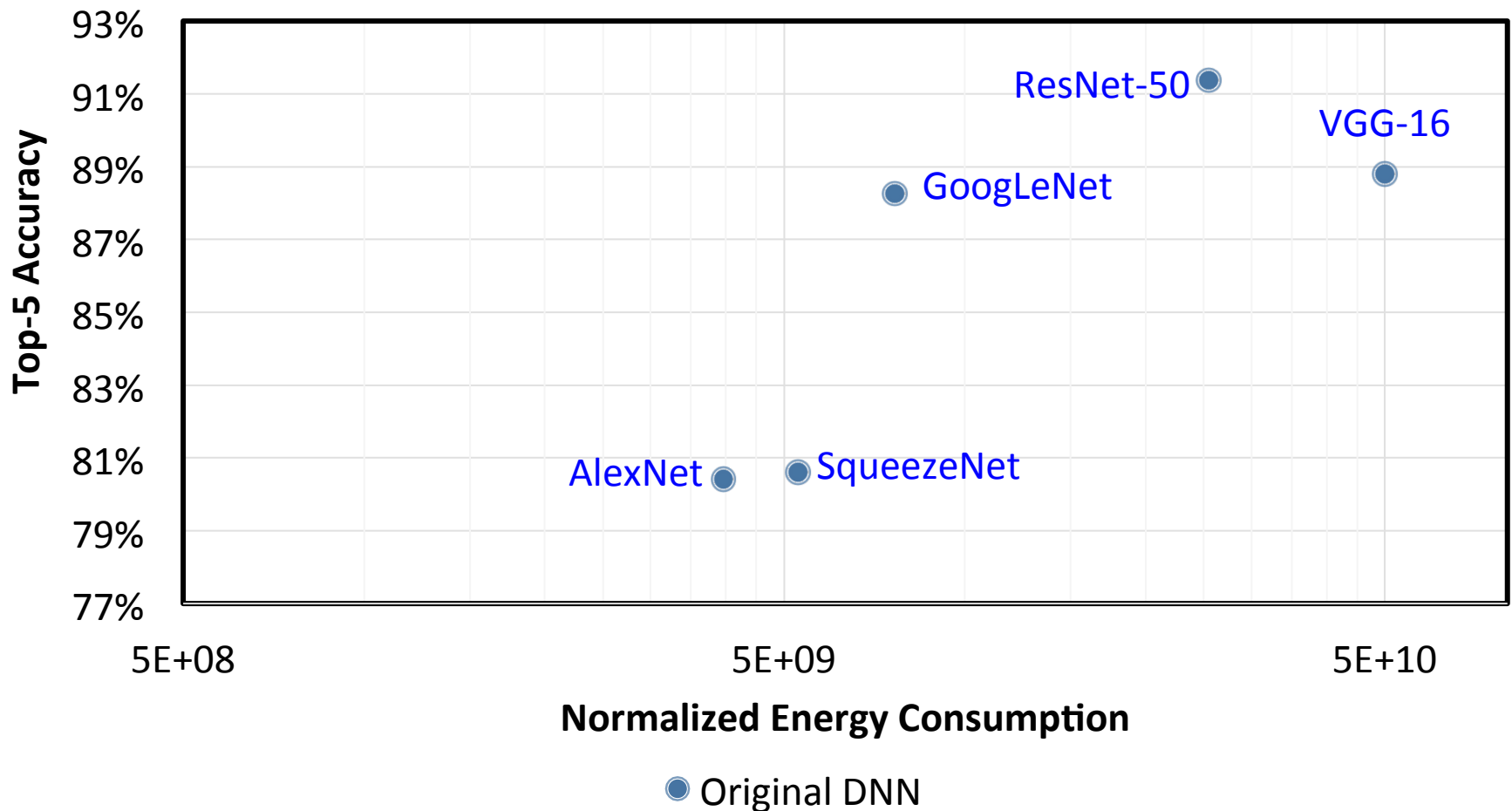


Fire Module



"labrador
retriever
dog"

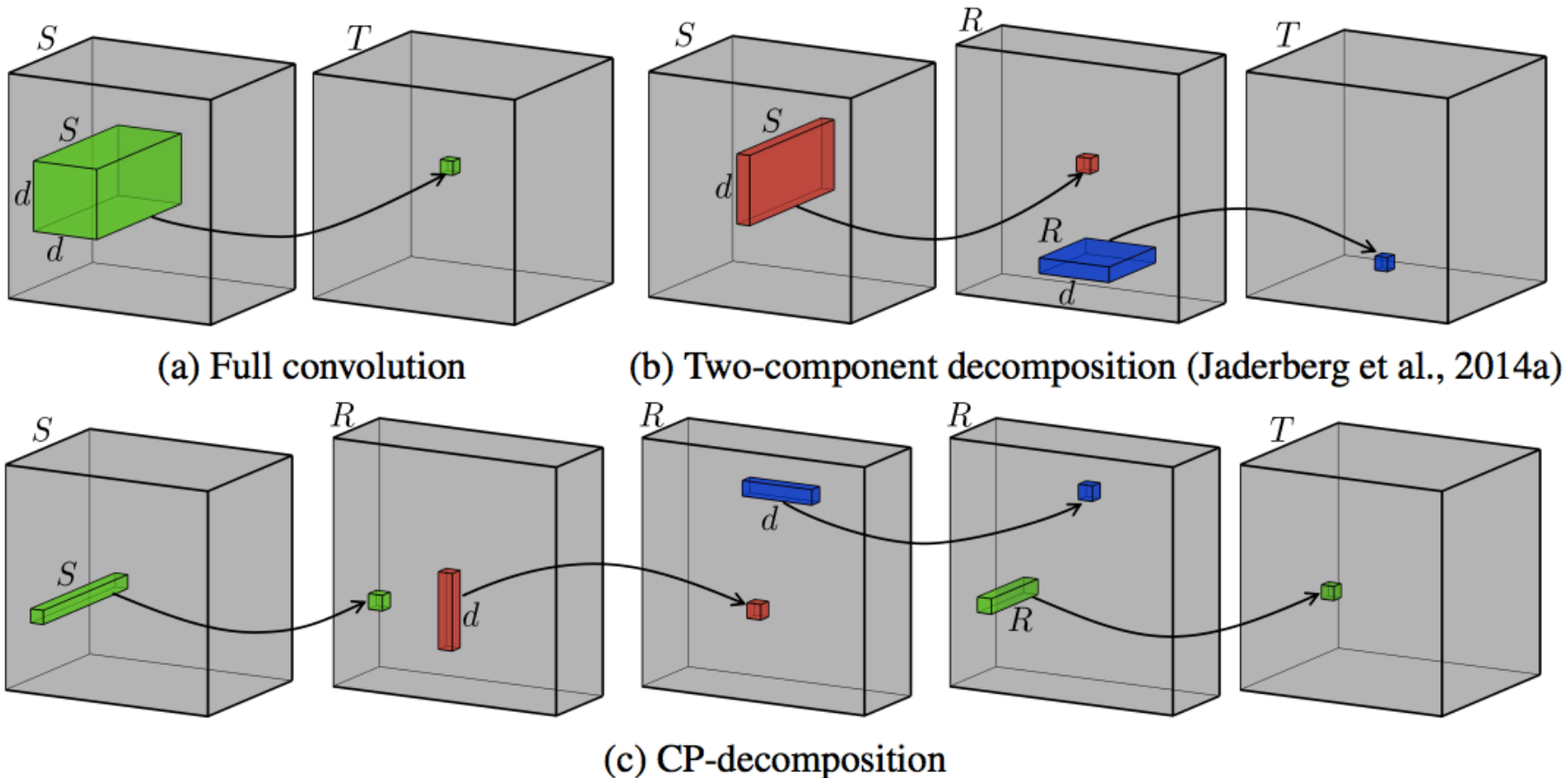
Energy Consumption of Existing DNNs



Deeper CNNs with fewer weights do not necessarily consume less energy than shallower CNNs with more weights

Decompose Trained Filters

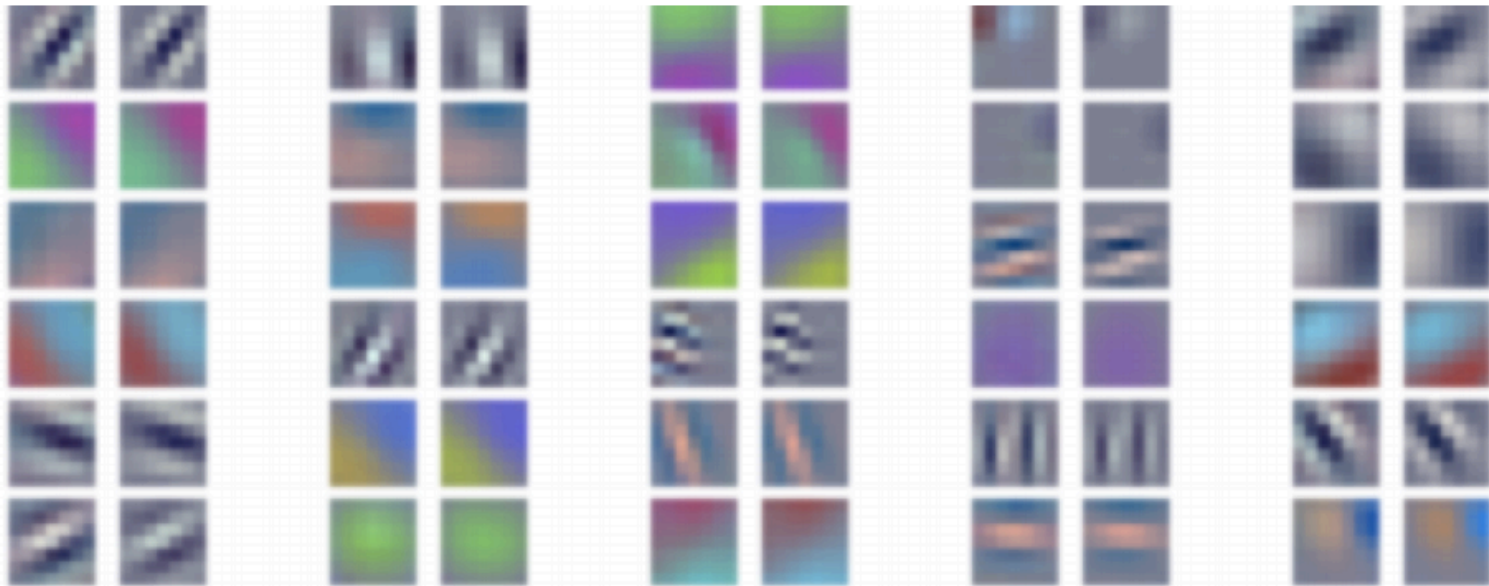
After training, perform **low-rank approximation** by applying **tensor decomposition** to weight kernel; then **fine-tune** weights for accuracy



Decompose Trained Filters

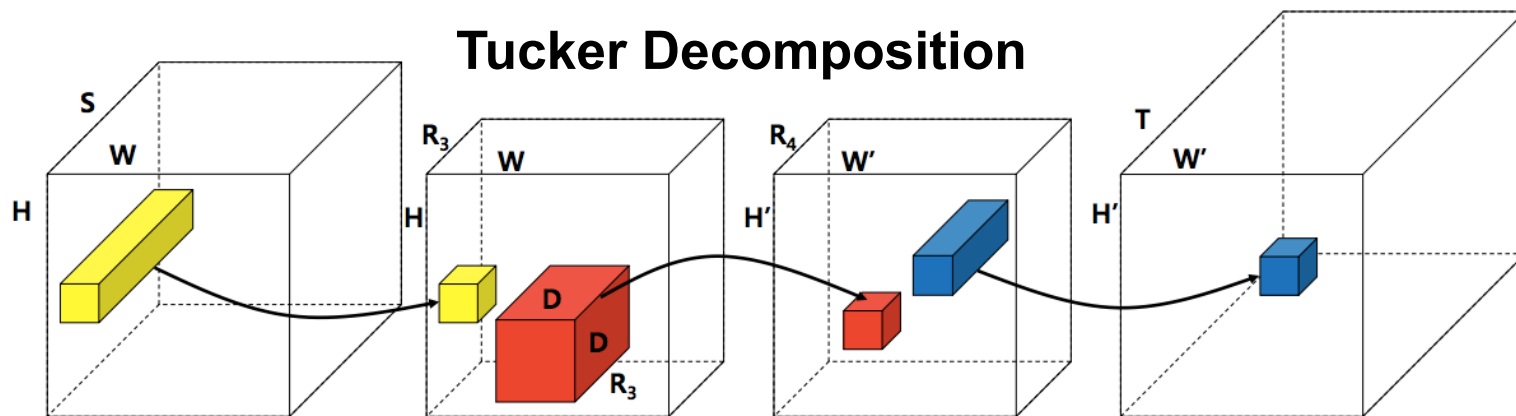
Visualization of Filters



Original Approx.



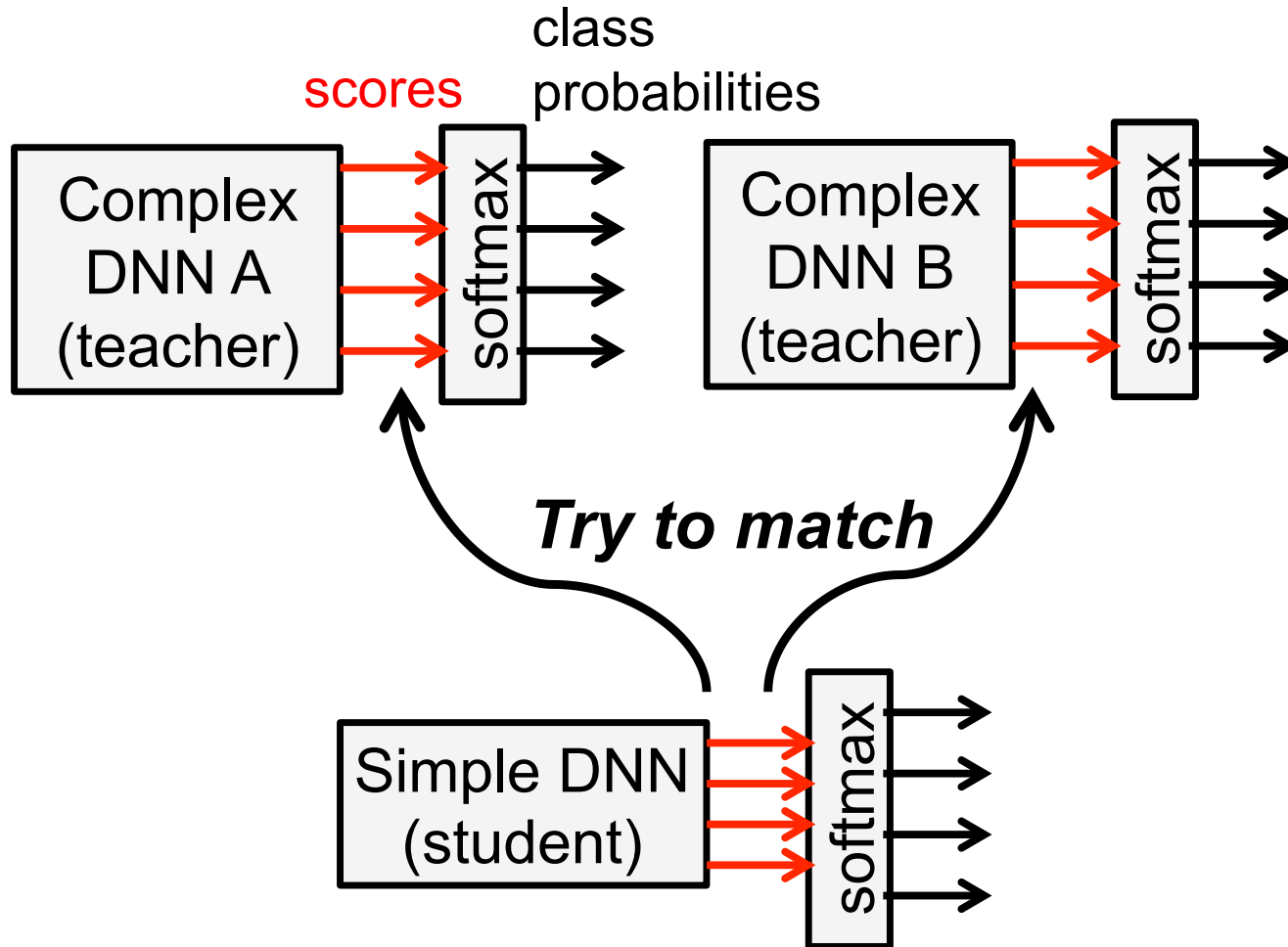
- **Speed up by 1.6 – 2.7x** on CPU/GPU for CONV1, CONV2 layers
- **Reduce size by 5 - 13x** for FC layer
- **< 1% drop in accuracy**

Decompose Trained Filters on Phone



Model	Top-5	Weights	FLOPs	S6		
<i>AlexNet</i>	80.03	61M	725M	117ms	245mJ	0.54ms
<i>AlexNet*</i>	78.33	11M	272M	43ms	72mJ	0.30ms
(imp.)	(-1.70)	(×5.46)	(×2.67)	(×2.72)	(×3.41)	(×1.81)
<i>VGG-S</i>	84.60	103M	2640M	357ms	825mJ	1.86ms
<i>VGG-S*</i>	84.05	14M	549M	97ms	193mJ	0.92ms
(imp.)	(-0.55)	(×7.40)	(×4.80)	(×3.68)	(×4.26)	(×2.01)
<i>GoogLeNet</i>	88.90	6.9M	1566M	273ms	473mJ	1.83ms
<i>GoogLeNet*</i>	88.66	4.7M	760M	192ms	296mJ	1.48ms
(imp.)	(-0.24)	(×1.28)	(×2.06)	(×1.42)	(×1.60)	(×1.23)
<i>VGG-16</i>	89.90	138M	15484M	1926ms	4757mJ	10.67ms
<i>VGG-16*</i>	89.40	127M	3139M	576ms	1346mJ	4.58ms
(imp.)	(-0.50)	(×1.09)	(×4.93)	(×3.34)	(×3.53)	(×2.33)

Knowledge Distillation



Metrics to Compare DNN Models

- **How can we compare different models?**
- **Accuracy**
- **Network Architecture**
 - # Layers, filter size, # of filters, # of channels
- **# of Weights (storage capacity)**
 - Number of non-zero (NZ) weights
- **# of MACs (operations)**
 - Number of non-zero (NZ) MACS

Metrics of DNN Models

Metrics	AlexNet	VGG-16	GoogLeNet (v1)	ResNet-50
Accuracy (top-5 error)*	19.8	8.80	10.7	7.02
Input	227x227	224x224	224x224	224x224
# of CONV Layers	5	16	21	49
Filter Sizes	3, 5, 11	3	1, 3, 5, 7	1, 3, 7
# of Channels	3 - 256	3 - 512	3 - 1024	3 - 2048
# of Filters	96 - 384	64 - 512	64 - 384	64 - 2048
Stride	1, 4	1	1, 2	1, 2
# of Weights	2.3M	14.7M	6.0M	23.5M
# of MACs	666M	15.3G	1.43G	3.86G
# of FC layers	3	3	1	1
# of Weights	58.6M	124M	1M	2M
# of MACs	58.6M	124M	1M	2M
Total Weights	61M	138M	7M	25.5M
Total MACs	724M	15.5G	1.43G	3.9G

*Single crop results: <https://github.com/jcjohnson/cnn-benchmarks>

Metrics of DNN Models

Metrics	AlexNet	VGG-16	GoogLeNet (v1)	ResNet-50
Accuracy (top-5 error)*	19.8	8.80	10.7	7.02
# of CONV Layers	5	16	21	49
# of Weights	2.3M	14.7M	6.0M	23.5M
# of MACs	666M	15.3G	1.43G	3.86G
# of NZ MACs**	394M	7.3G	806M	1.5G
# of FC layers	3	3	1	1
# of Weights	58.6M	124M	1M	2M
# of MACs	58.6M	124M	1M	2M
# of NZ MACs**	14.4M	17.7M	639k	1.8M
Total Weights	61M	138M	7M	25.5M
Total MACs	724M	15.5G	1.43G	3.9G
# of NZ MACs**	409M	7.3G	806M	1.5G

*Single crop results: <https://github.com/jcjohnson/cnn-benchmarks>



**# of NZ MACs based on 50k ImageNet validation images


Metrics of DNN Algorithms

Metrics	AlexNet	AlexNet (sparse)
Accuracy (top-5 error)	19.8	19.8
# of Conv Layers	5	5
# of Weights	2.3M	2.3M
# of MACs	666M	666M
# of NZ weights	2.3M	863k
# of NZ MACs	394M	207M
# of FC layers	3	3
# of Weights	58.6M	58.6M
# of MACs	58.6M	58.6M
# of NZ weights	58.6M	5.9M
# of NZ MACs	14.4M	2.1M
Total Weights	61M	61M
Total MACs	724M	724M
# of NZ weights	61M	6.8M
# of NZ MACs	409M	209M

Tutorial Summary

- **DNNs are a critical component in the AI revolution**, delivering record breaking accuracy on many important AI tasks for a wide range of applications; however, it comes at the cost of **high computational complexity**
- **Efficient processing of DNNs** is an important area of research with many promising opportunities for innovation at **various levels of hardware design, including algorithm co-design**
- When considering different DNN solutions it is important to **evaluate with the appropriate workload** in term of both input and model, and recognize that they are **evolving rapidly**.
- It's important to consider a **comprehensive set of metrics** when evaluating different DNN solutions: **accuracy, speed, energy, and cost**

Resources

- **Eyeriss Project:** <http://eyeriss.mit.edu>
 - Tutorial Slides
 - Benchmarking
 - Energy modeling
 - Mailing List for updates  Follow @eems_mit
 - <http://mailman.mit.edu/mailman/listinfo/eems-news>
 - **Paper based on today's tutorial:**
 - V. Sze, Y.-H. Chen, T-J. Yang, J. Emer, “*Efficient Processing of Deep Neural Networks: A Tutorial and Survey*”, arXiv, 2017