

# Efficient Image Processing with Deep Neural Networks

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*In collaboration with  
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# Contributors



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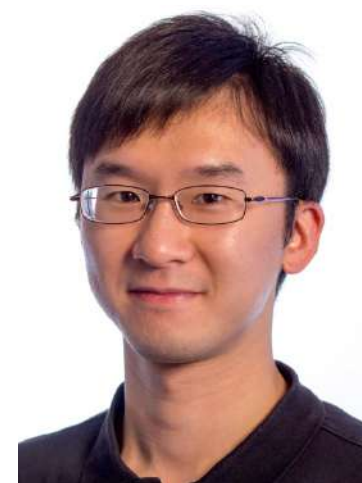
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# Outline of Tutorial

- Brief overview of Deep Neural Networks (DNN)
- **Part 1: Hardware Platforms for DNNs** (e.g., CPU, GPU, FPGA, ASIC) and **metrics for evaluating the efficiency of DNNs**
- **Part 2: Co-design algorithms and hardware** for efficient DNNs (e.g., precision, sparsity, network architecture design, network architecture search, designing networks with hardware in the loop)
- **Part 3: Application of efficient DNNs** on a wide range of image processing and computer vision tasks (e.g., image classification, depth estimation, image segmentation, super-resolution)

# Additional Resources

## Overview Paper

V. Sze, Y.-H. Chen, T.-J. Yang, J. Emer, “*Efficient Processing of Deep Neural Networks: A Tutorial and Survey*,” **Proceedings of the IEEE**, Dec. 2017

***Book Coming Soon!***

More info about **Tutorial on DNN Architectures**

<http://eyeriss.mit.edu/tutorial.html>

MIT Professional Education Course on

**“Designing Efficient Deep Learning Systems”**

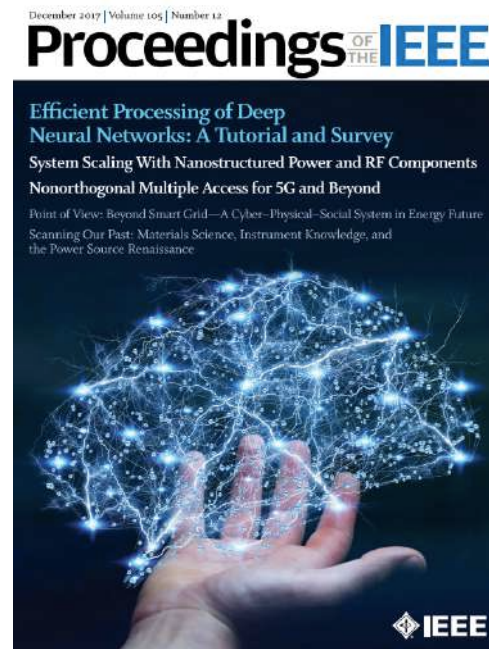
<http://professional-education.mit.edu/deeplearning>

For updates



Follow @eems\_mit

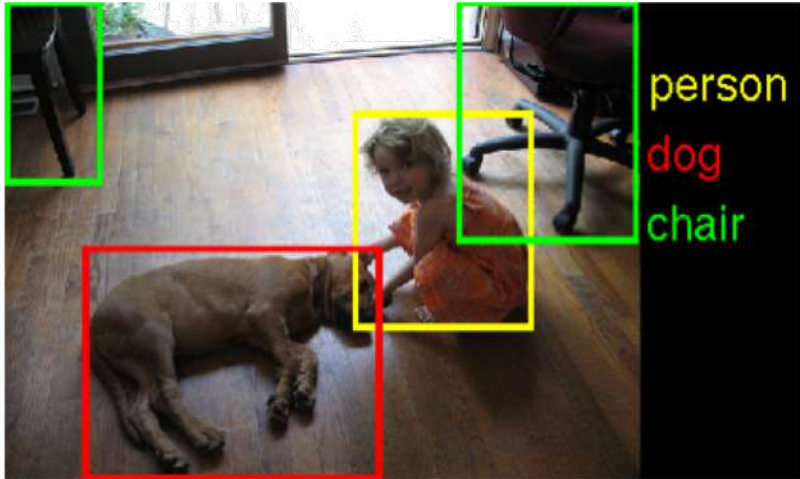
<http://mailman.mit.edu/mailman/listinfo/eems-news>





# Example Applications of Deep Learning

## Computer Vision



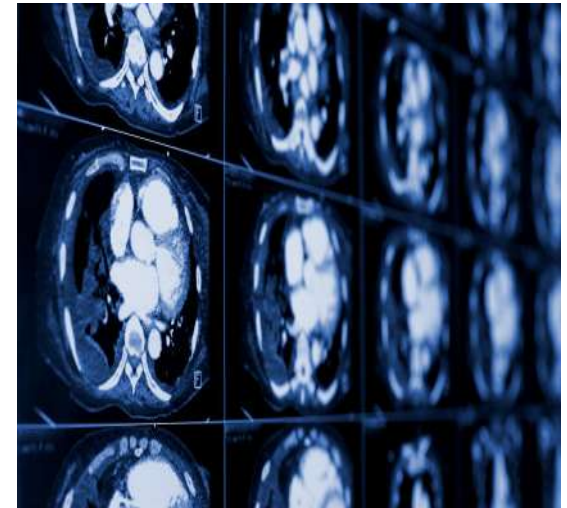
## Speech Recognition



## Game Play



## Medical



# Compute Demands for Deep Learning

## Common carbon footprint benchmarks

in lbs of CO2 equivalent

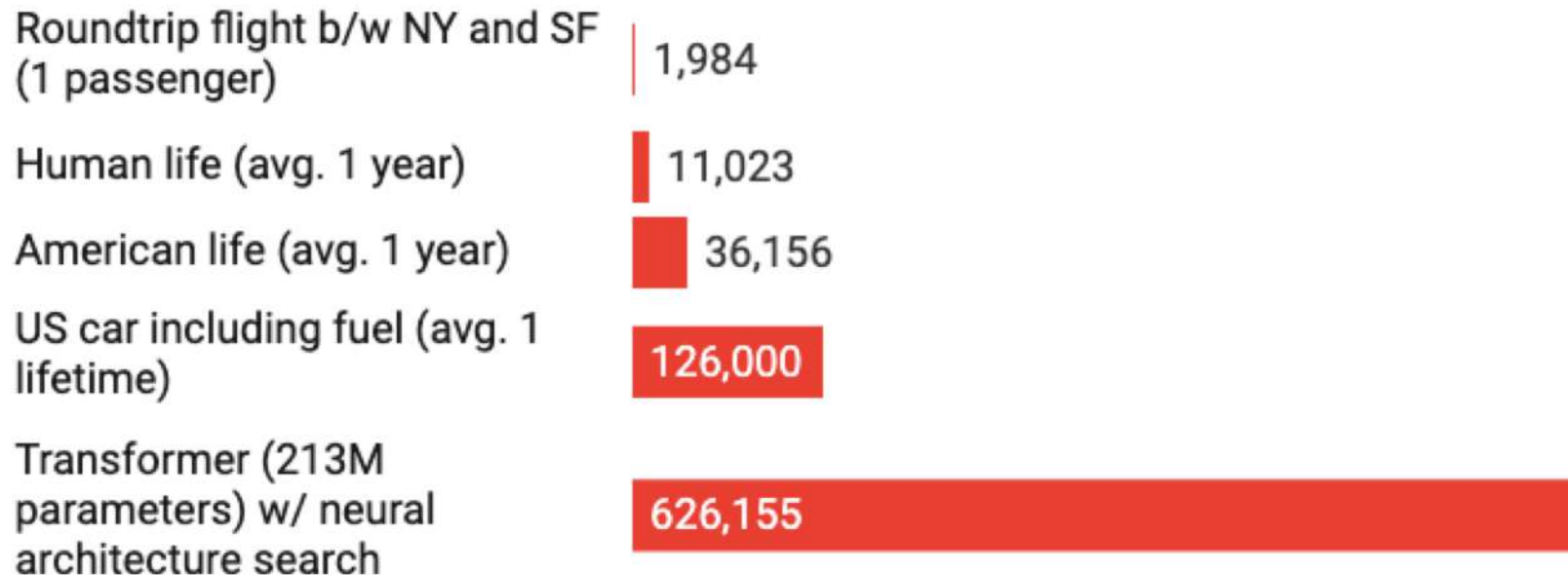
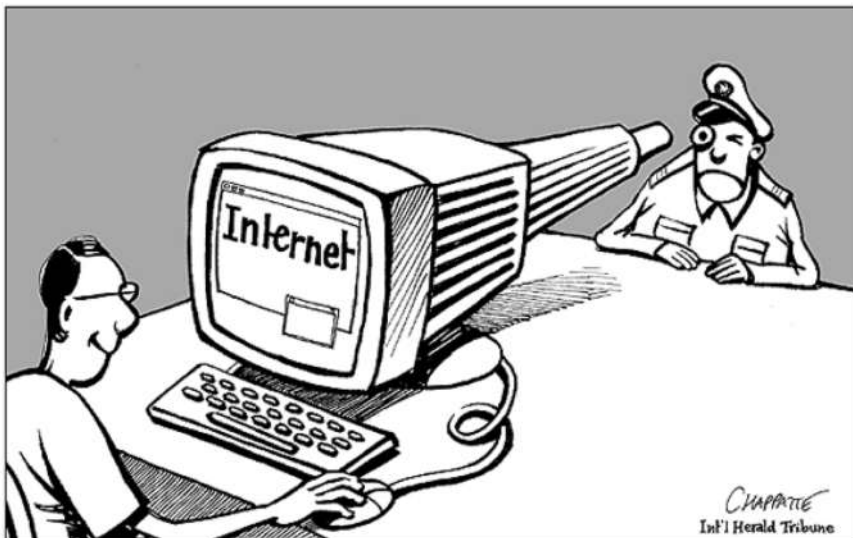


Chart: MIT Technology Review • Source: Strubell et al. • [Created with Datawrapper](#)

# Processing at “Edge” instead of the “Cloud”

## Privacy



## Communication



Image source:  
[www.theregister.co.uk](http://www.theregister.co.uk)

## Latency



Sensor



Actuator



Cloud

Image source: [ericsson.com](http://ericsson.com)



# Deep Learning for Self-Driving Cars

JACK STEWART TRANSPORTATION 02.06.18 08:00 AM

## SELF-DRIVING CARS USE CRAZY AMOUNTS OF POWER, AND IT'S BECOMING A PROBLEM



Shelley, a self-driving Audi TT developed by Stanford University, uses the brains in the trunk to speed around a racetrack autonomously.

NIKKI KAHN/THE WASHINGTON POST/GETTY IMAGES

# WIRED

(Feb 2018)

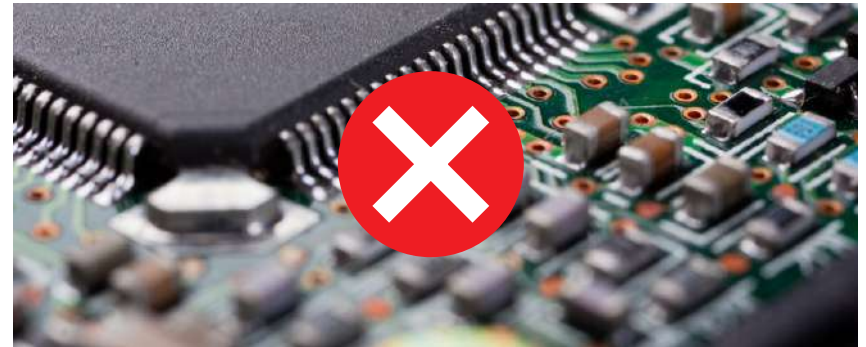
Cameras and radar generate ~6 gigabytes of data every 30 seconds.

Prototypes use around 2,500 Watts.  
Generates wasted heat and some prototypes need water-cooling!

# Existing Processors Consume Too Much Power



**< 1 Watt**



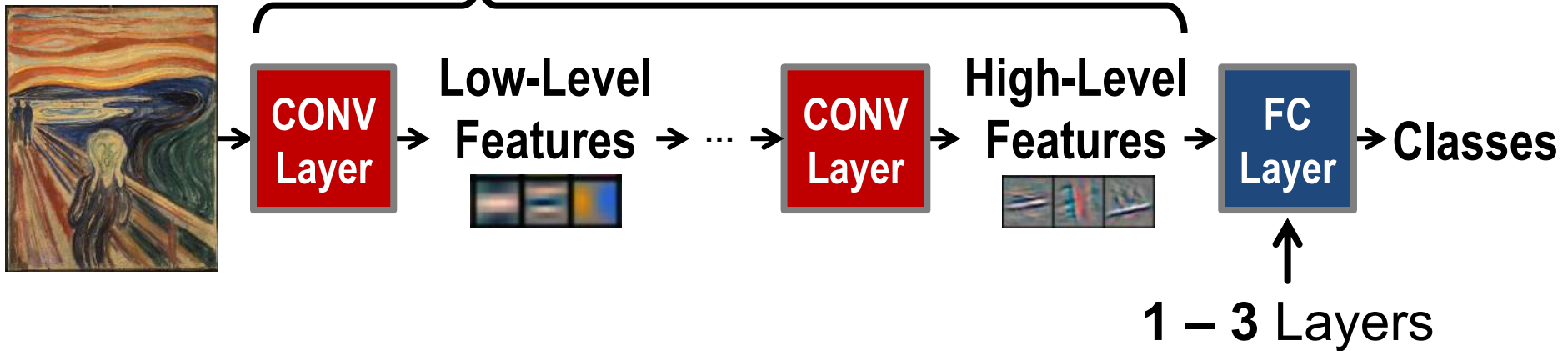
**> 10 Watts**



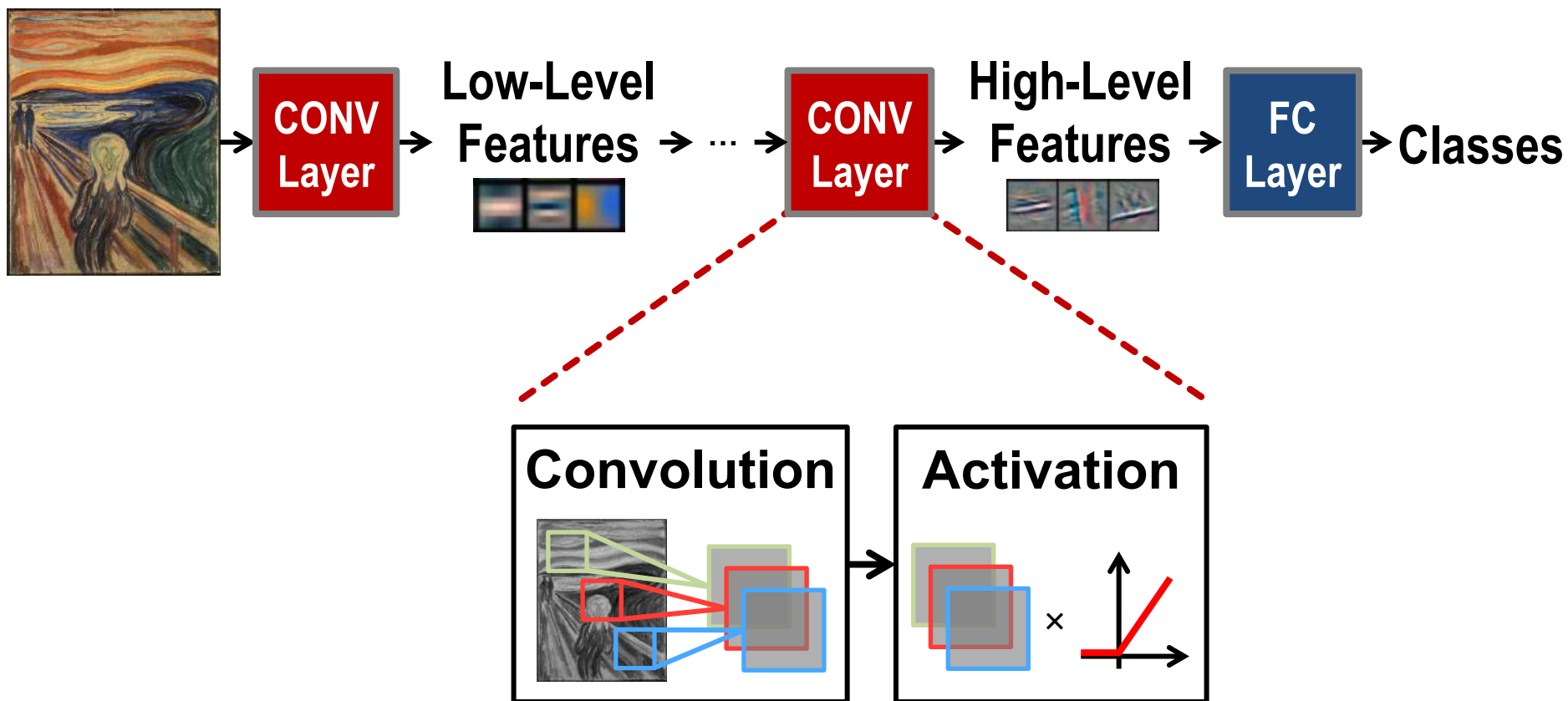
# Overview of Deep Neural Networks

# Deep Convolutional Neural Networks

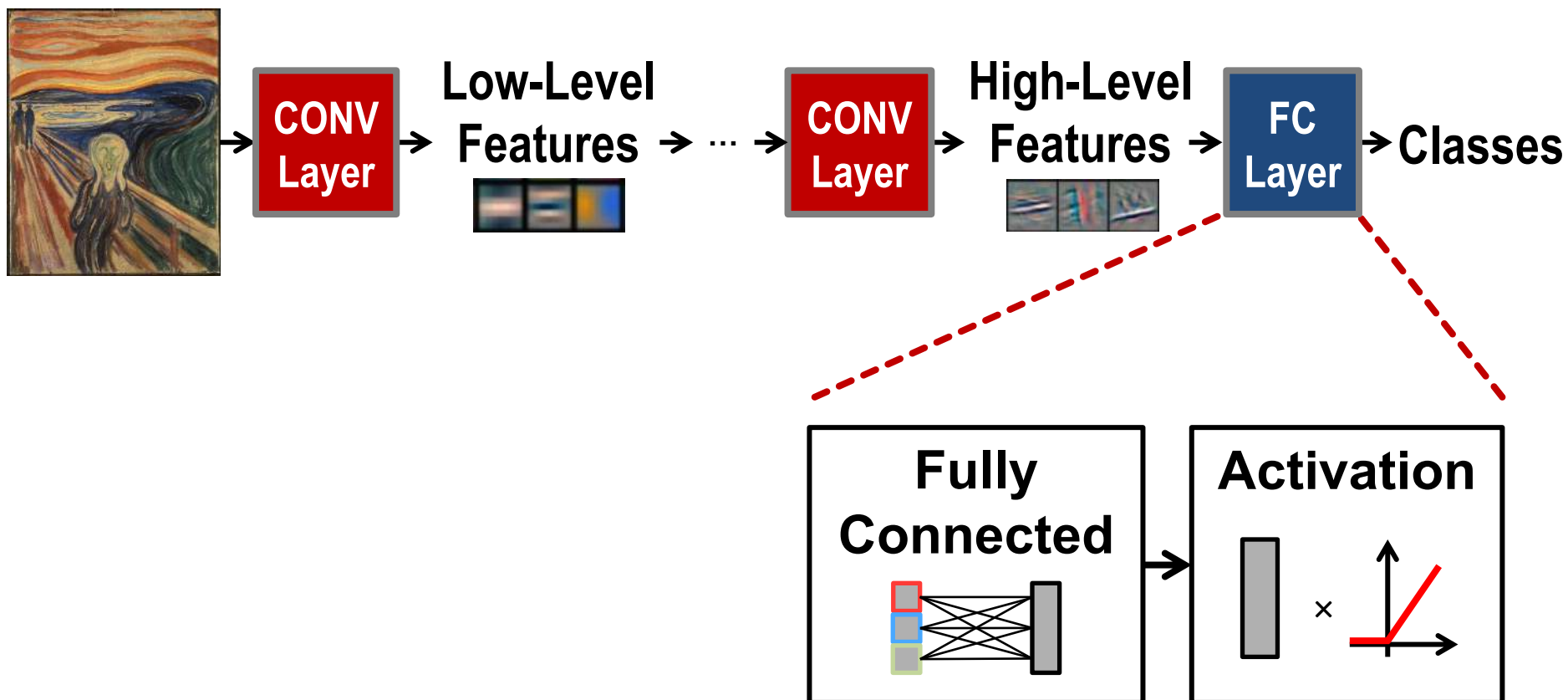
Modern **Deep** CNN: 5 – 1000 Layers



# Deep Convolutional Neural Networks



# Deep Convolutional Neural Networks



# Deep Convolutional Neural Networks

Optional layers in between  
CONV and/or FC layers



**CONV  
Layer**

**NORM  
Layer**

**POOL  
Layer**

**CONV  
Layer**

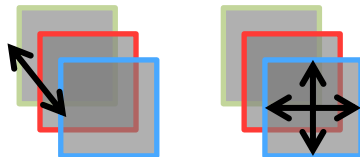
High-Level  
Features



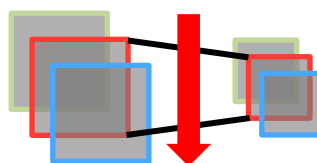
**FC  
Layer**

**Classes**

**Normalization**

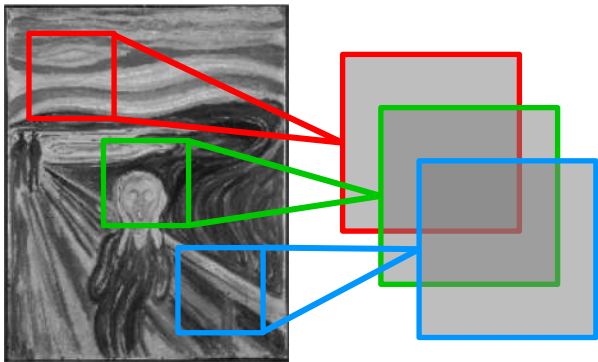
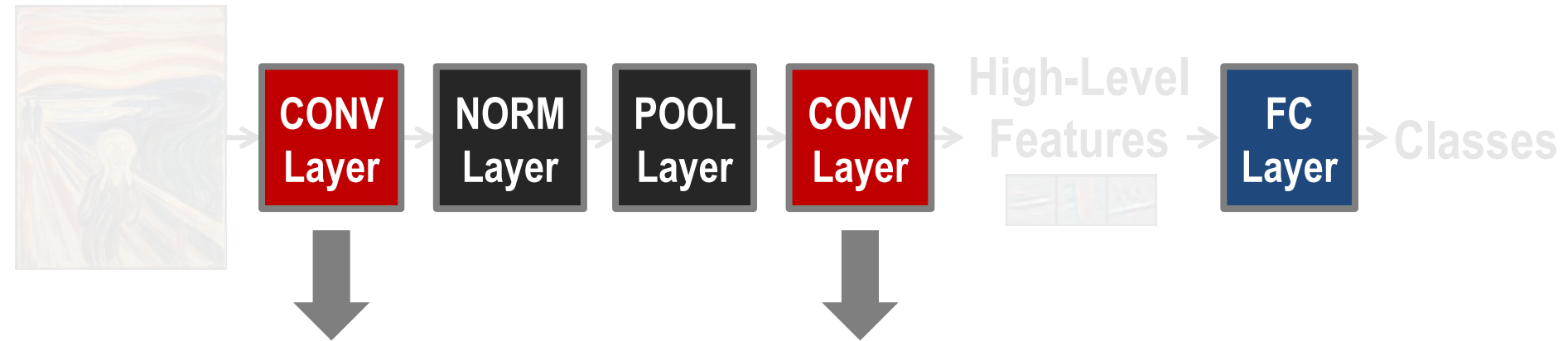


**Pooling**





# Deep Convolutional Neural Networks

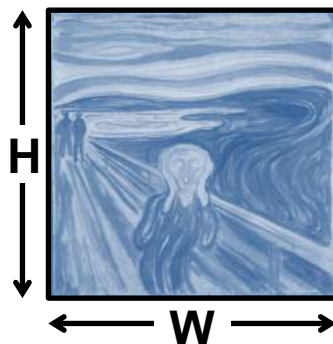
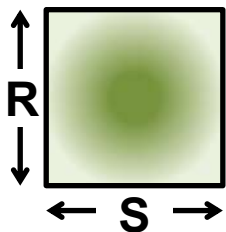


**Convolutions** account for more than 90% of overall computation, dominating **runtime** and **energy consumption**

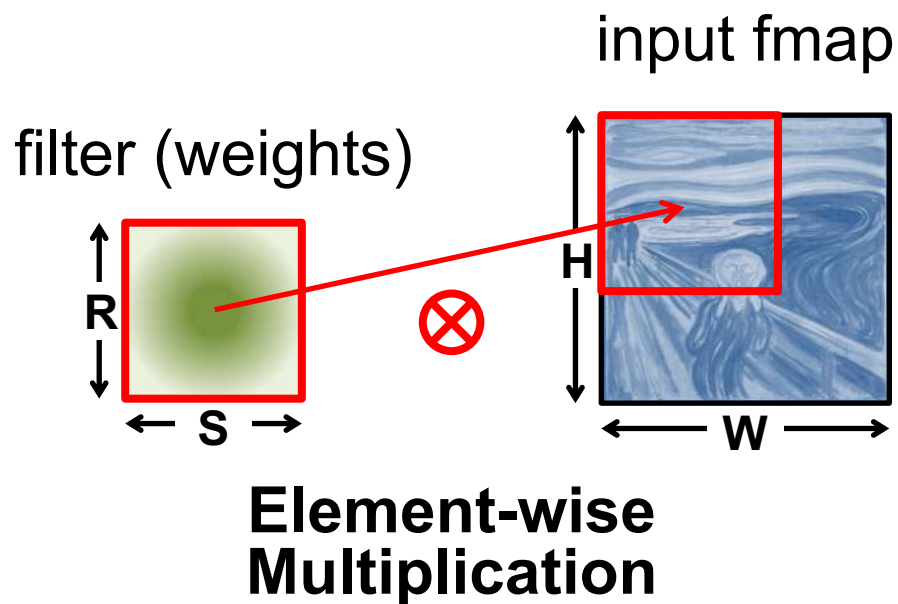
# Convolution (CONV) Layer

a plane of input activations  
a.k.a. **input feature map (fmap)**

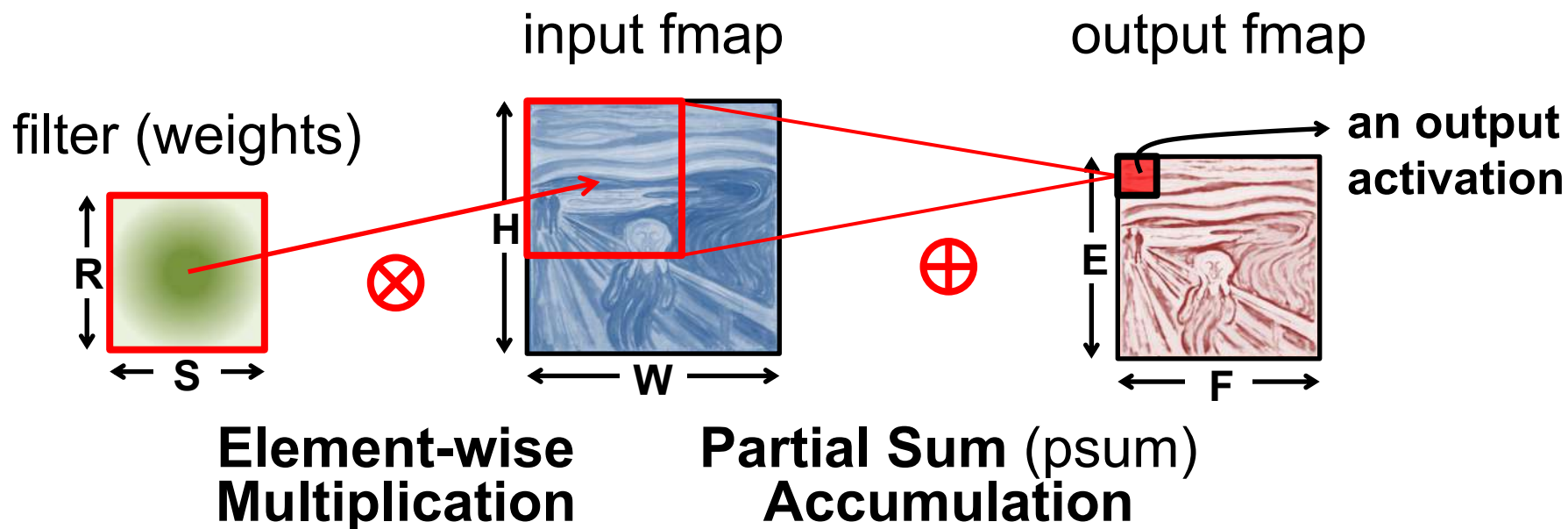
filter (weights)



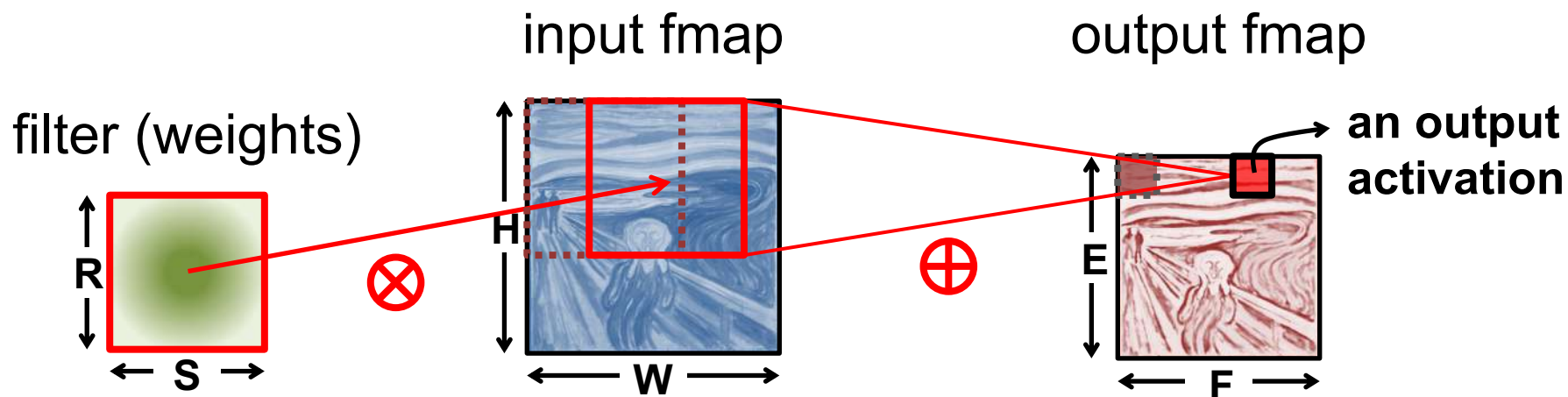
# Convolution (CONV) Layer



# Convolution (CONV) Layer



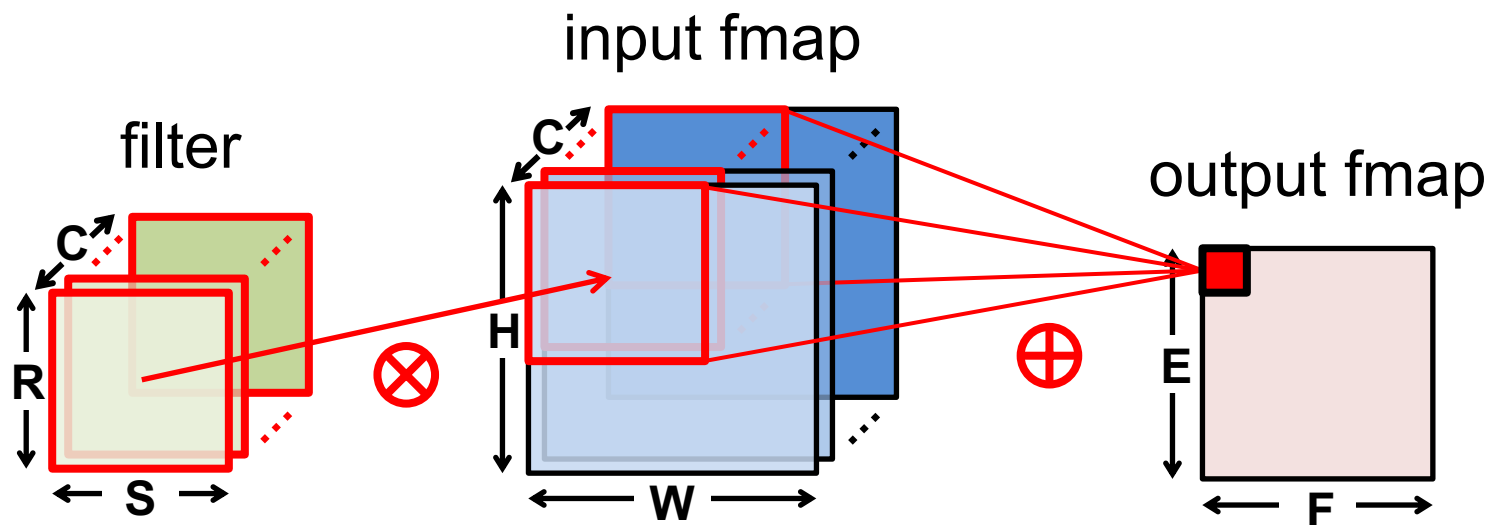
# Convolution (CONV) Layer



## Sliding Window Processing

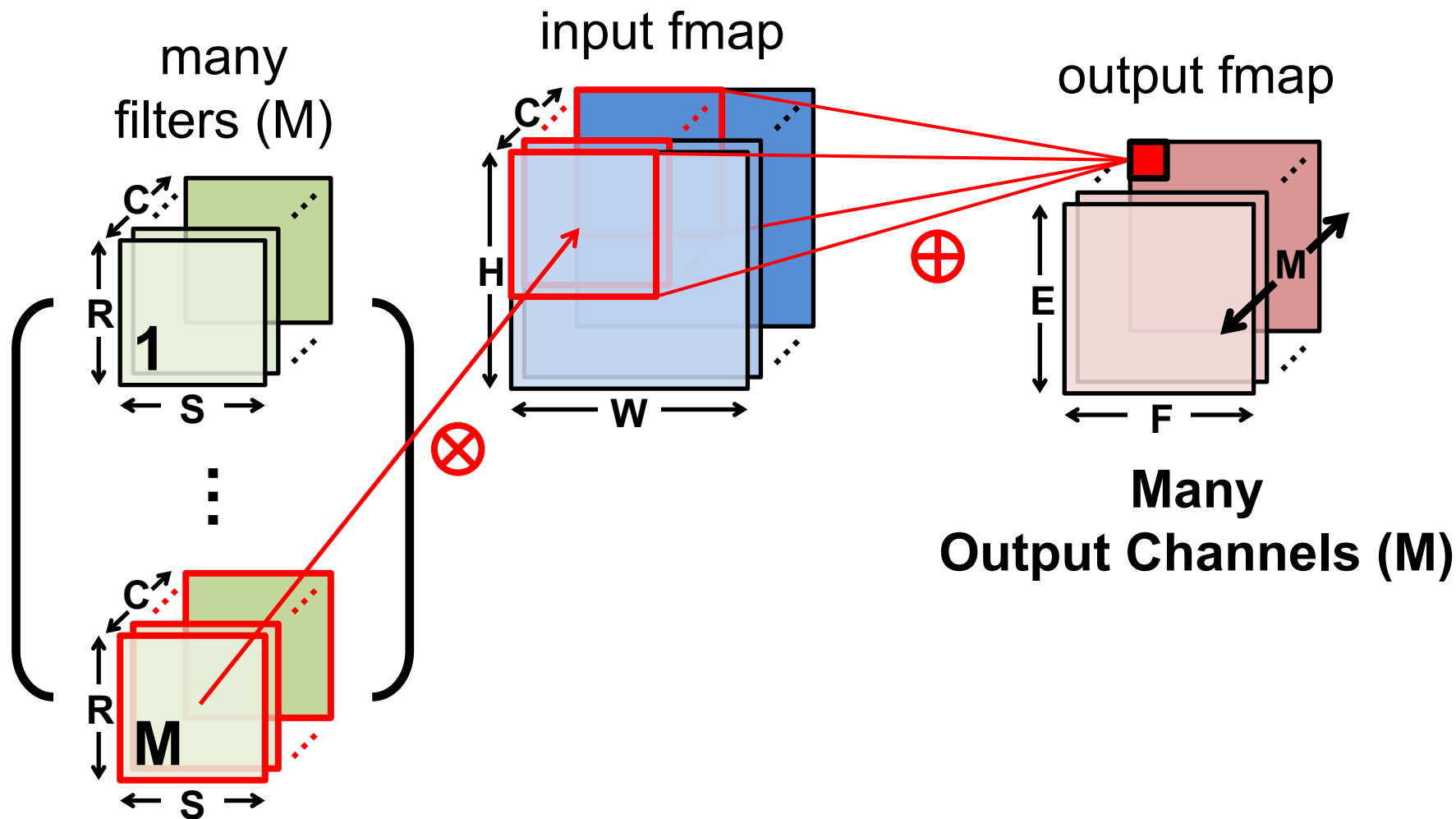


# Convolution (CONV) Layer

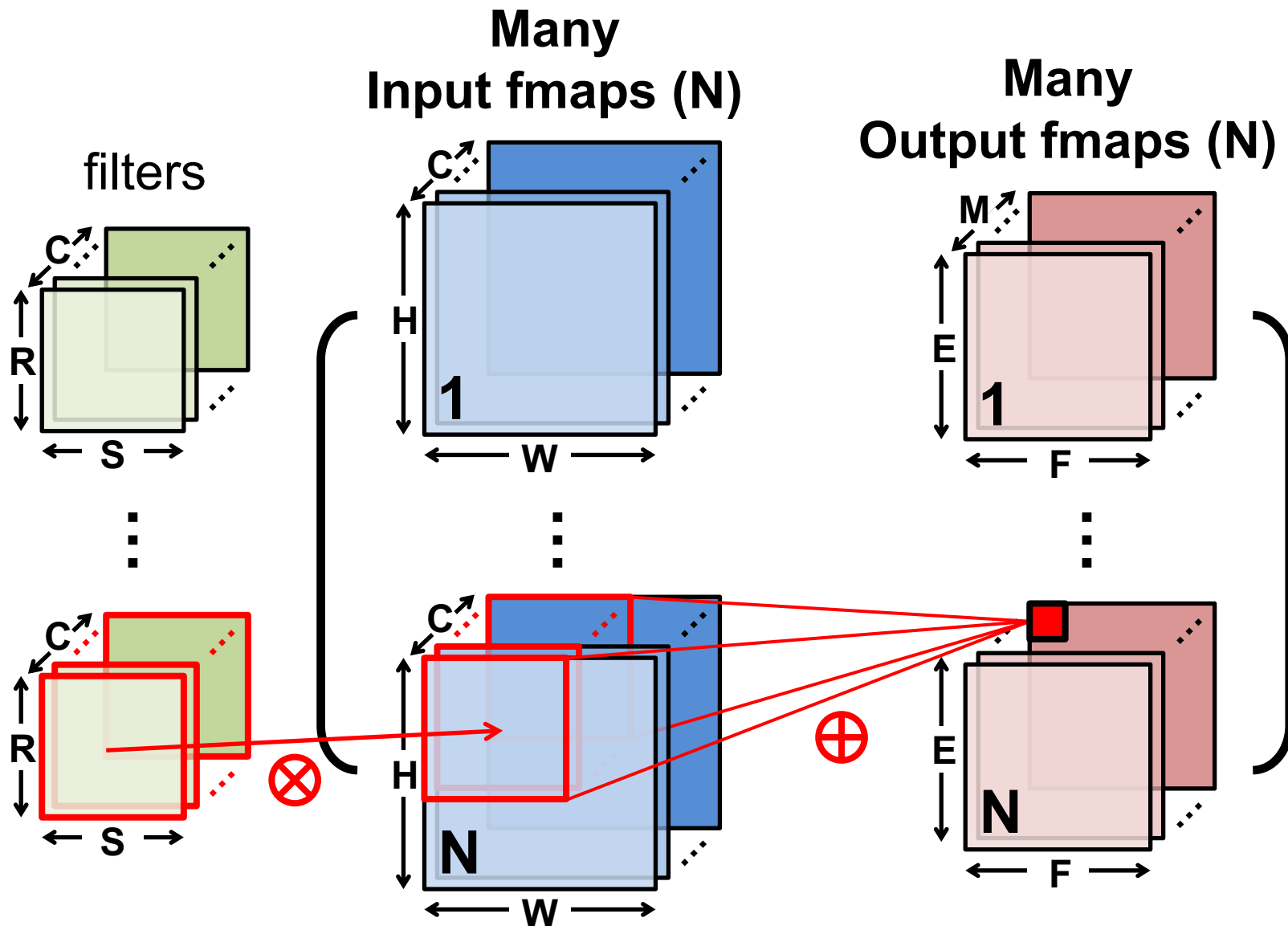


**Many Input Channels (C)**

# Convolution (CONV) Layer



# Convolution (CONV) Layer

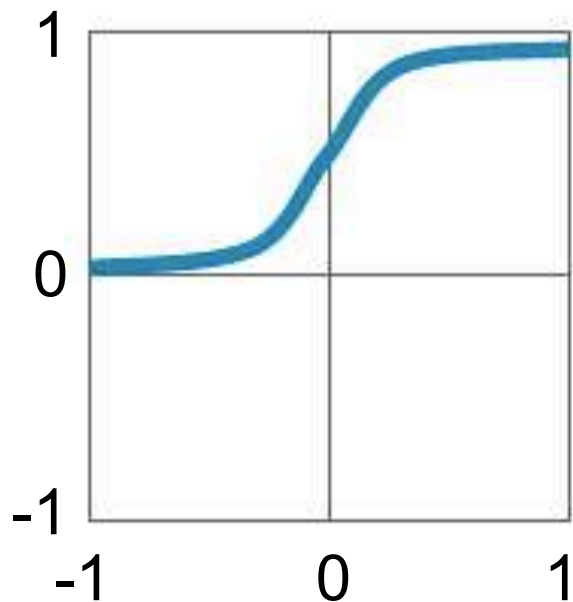


# CNN Decoder Ring

- $N$  – Number of **input fmaps/output fmaps** (batch size)
- $C$  – Number of 2-D **input fmaps /filters** (channels)
- $H$  – Height of **input fmap** (activations)
- $W$  – Width of **input fmap** (activations)
- $R$  – Height of 2-D **filter** (weights)
- $S$  – Width of 2-D **filter** (weights)
- $M$  – Number of 2-D **output fmaps** (channels)
- $E$  – Height of **output fmap** (activations)
- $F$  – Width of **output fmap** (activations)

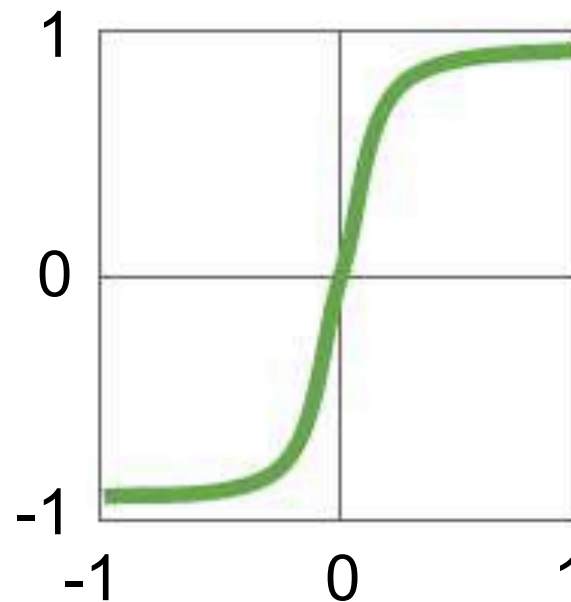
# Traditional Activation Functions

## Sigmoid



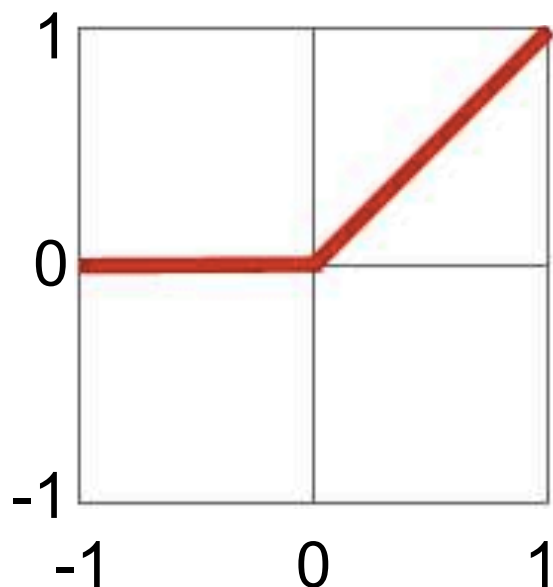
$$y = 1 / (1 + e^{-x})$$

## Hyperbolic Tangent



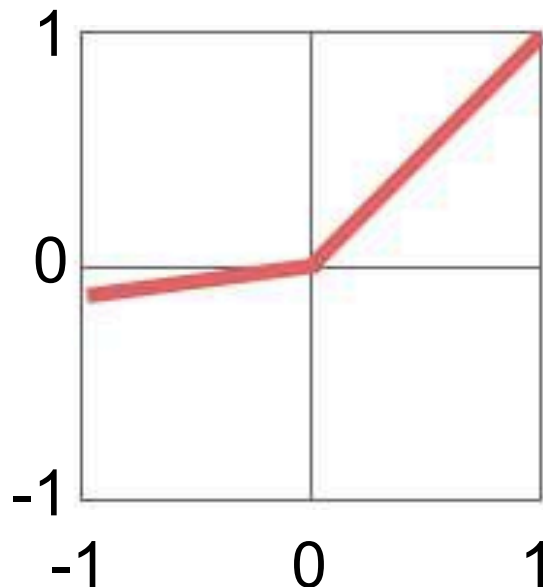
$$y = (e^x - e^{-x}) / (e^x + e^{-x})$$

Rectified Linear Unit  
(ReLU)



$$y = \max(0, x)$$

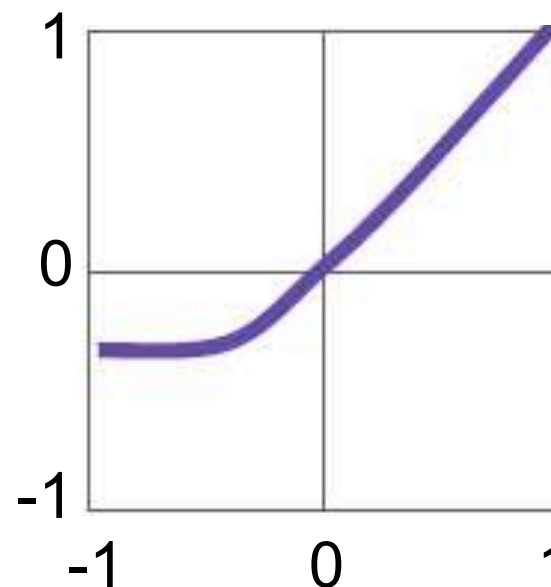
Leaky ReLU



$$y = \max(\alpha x, x)$$

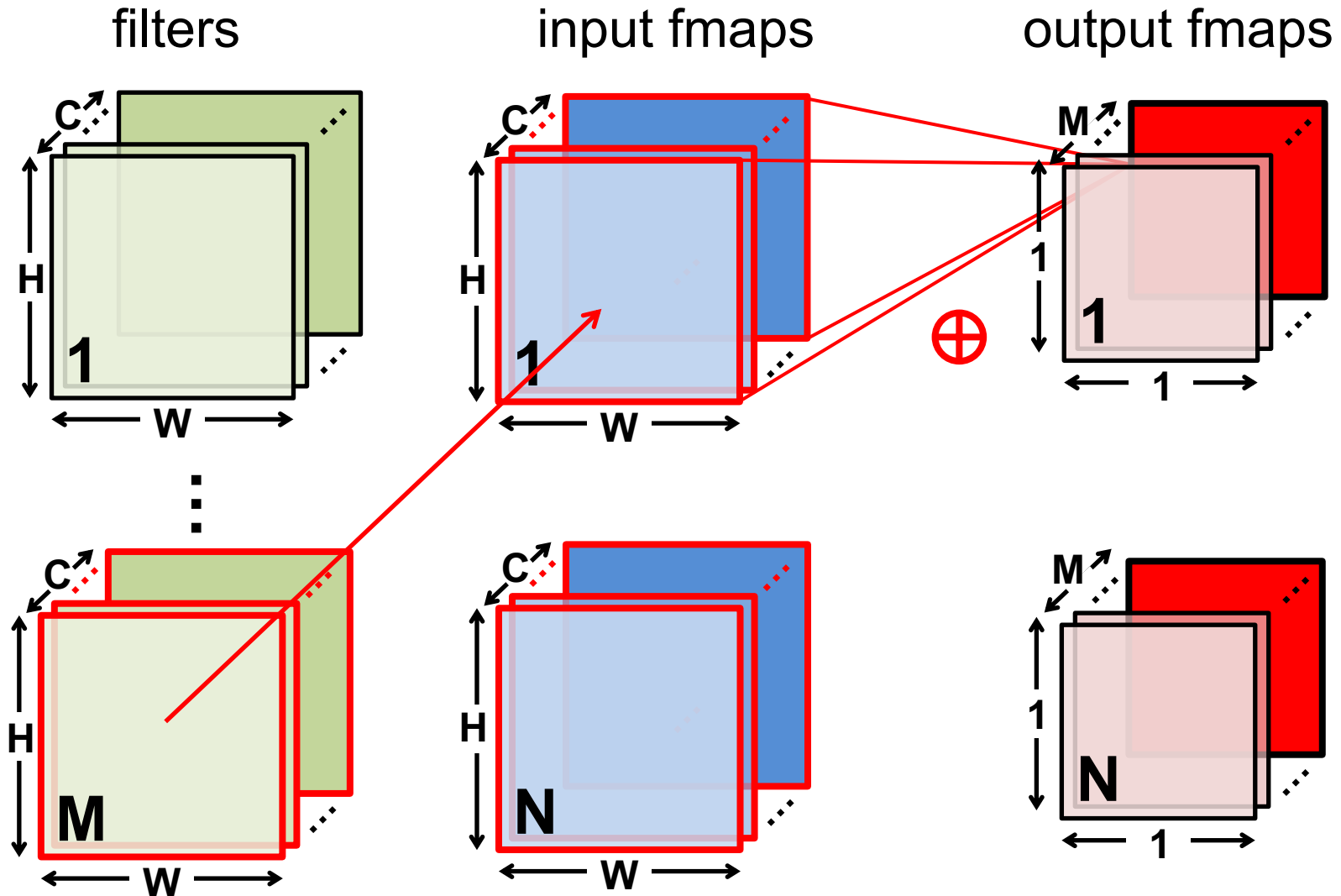
$\alpha = \text{small const. (e.g. 0.1)}$

Exponential LU



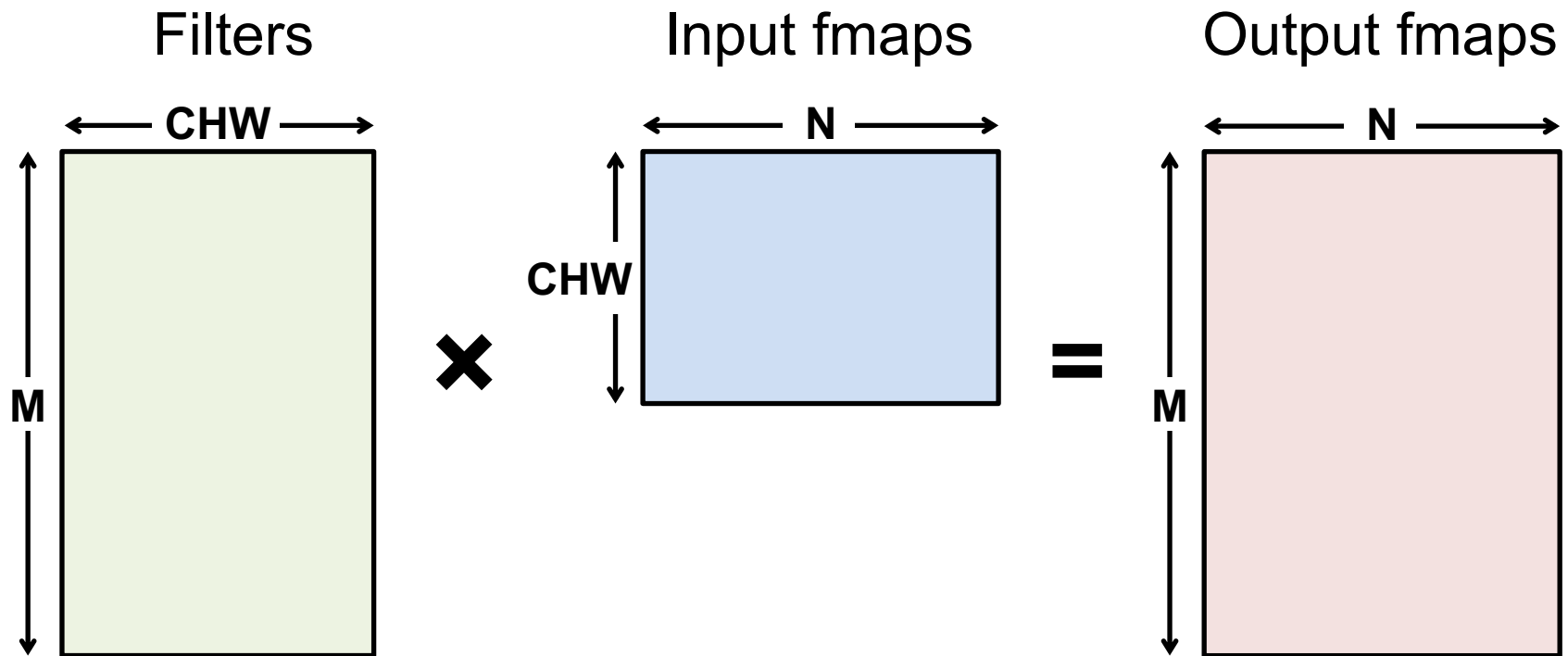
$$y = \begin{cases} x, & x \geq 0 \\ \alpha(e^x - 1), & x < 0 \end{cases}$$

# FC Layer – from CONV Layer POV



## Fully-Connected (FC) Layer

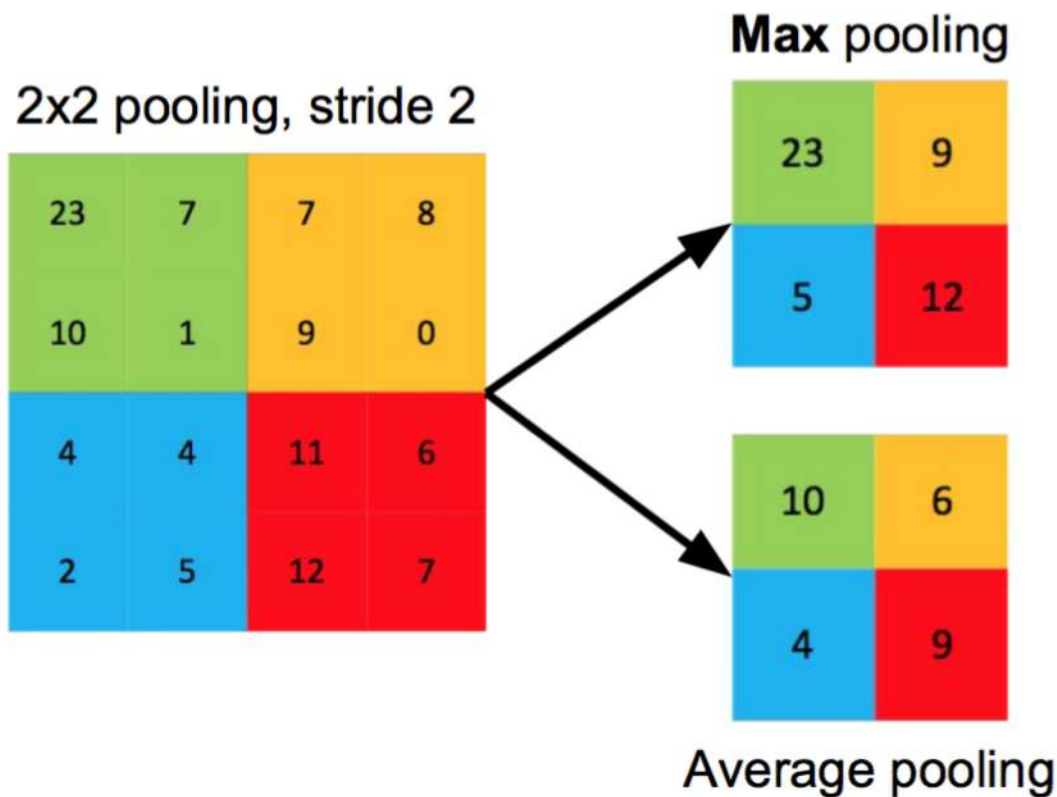
- Height and width of output fmaps are 1 ( $E = F = 1$ )
- Filters as large as input fmaps ( $R = H, S = W$ )
- Implementation: **Matrix Multiplication**





## Pooling (POOL) Layer

- Reduce resolution of each channel independently
- Overlapping or non-overlapping → depending on stride

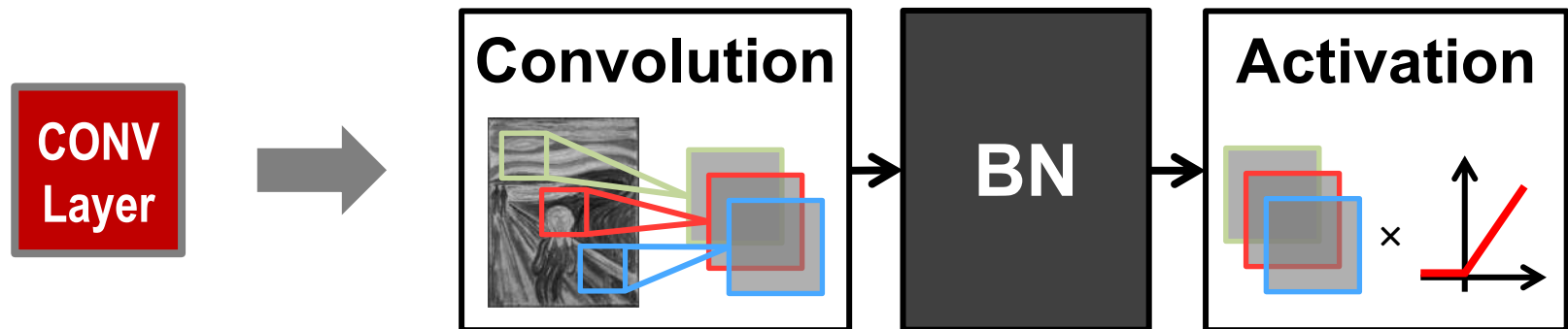


Increases translation-invariance and noise-resilience

# Normalization (NORM) Layer

- **Batch Normalization (BN)**

- Normalize activations towards mean=0 and std. dev.=1 based on the statistics of the training dataset
- put **in between** CONV/FC and **Activation** function



Believed to be key to getting high accuracy and faster training on very deep neural networks.

## BN Layer Implementation

- The normalized value is further scaled and shifted, the parameters of which are learned from training

The diagram illustrates the Batch Normalization (BN) layer implementation formula, showing how data is normalized, scaled, and shifted. The formula is presented as 
$$y = \frac{x - \mu}{\sqrt{\sigma^2 + \epsilon}} \gamma + \beta$$
. Annotations include: a red arrow pointing to  $\mu$  labeled "data mean"; a red arrow pointing to  $\sigma^2$  labeled "data std. dev."; a blue arrow pointing to  $\gamma$  labeled "learned scale factor"; a blue arrow pointing to  $\beta$  labeled "learned shift factor"; and a grey arrow pointing to  $\epsilon$  labeled "small const. to avoid numerical problems".

**data mean**

**learned scale factor**

**data std. dev.**

**learned shift factor**

small const. to avoid numerical problems

# Relevant Components for this Tutorial

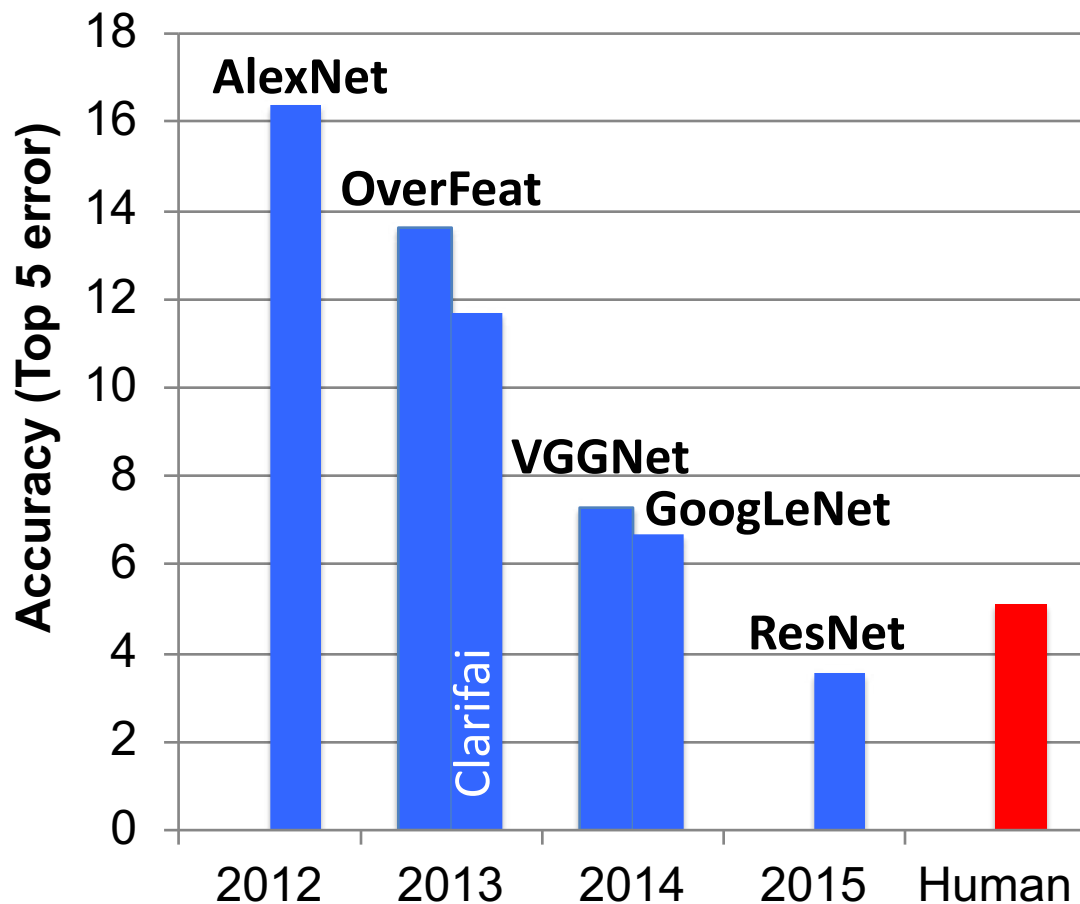
- Typical operations that we will discuss:
  - Convolution (CONV)
  - Fully-Connected (FC)
  - Max Pooling
  - ReLU

# Popular DNN Models

## Popular DNNs

- LeNet (1998)
- AlexNet (2012)
- OverFeat (2013)
- VGGNet (2014)
- GoogLeNet (2014)
- ResNet (2015)

### ImageNet: Large Scale Visual Recognition Challenge (ILSVRC)



**Image Classification**

~256x256 pixels (color)

1000 Classes

1.3M Training

100,000 Testing (50,000 Validation)

**For ImageNet Large Scale Visual Recognition Challenge (ILSVRC)**

accuracy of classification task reported based on top-1 and top-5 error

Image Source: <http://karpathy.github.io/>



<http://www.image-net.org/challenges/LSVRC/>



# AlexNet

CONV Layers: 5

Fully Connected Layers: 3

Weights: 61M

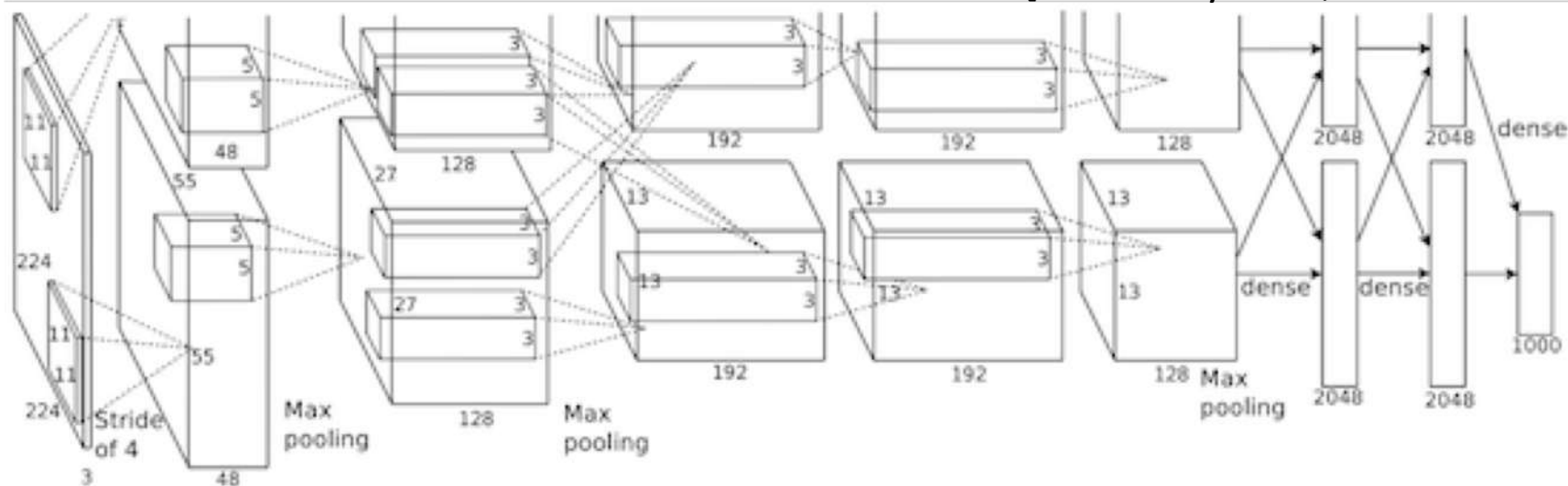
MACs: 724M

ReLU used for non-linearity

ILSCVR12 Winner

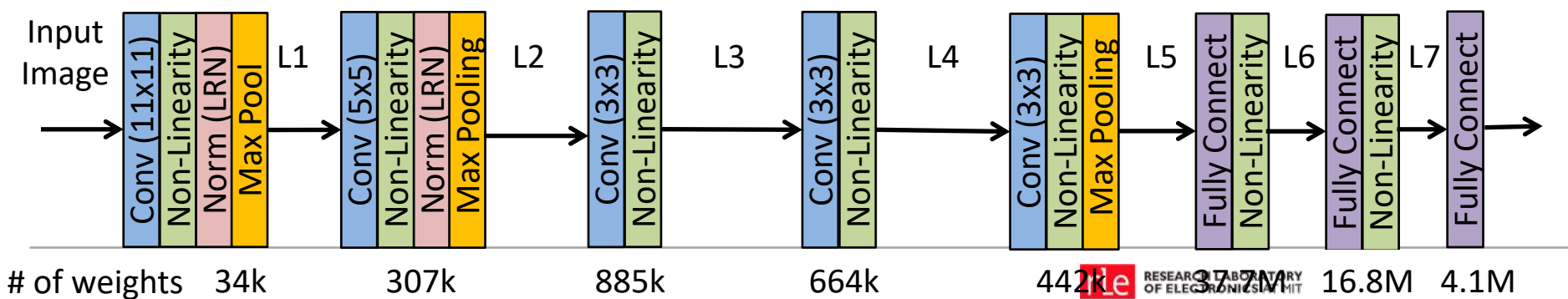
Uses Local Response Normalization (LRN)

[Krizhevsky et al., NeurIPS 2012]



224x224

1000  
scores



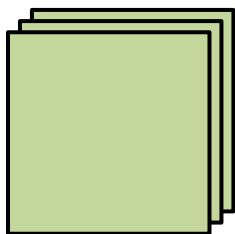


# Large Sizes with Varying Shapes

## AlexNet Convolutional Layer Configurations

Layer	Filter Size (RxS)	# Filters (M)	# Channels (C)	Stride
1	11x11	96	3	4
2	5x5	256	48	1
3	3x3	384	256	1
4	3x3	384	192	1
5	3x3	256	192	1

**Layer 1**



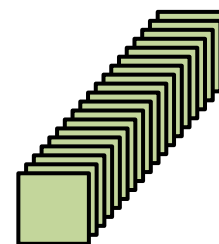
**34k Params**  
**105M MACs**

**Layer 2**



**307k Params**  
**224M MACs**

**Layer 3**



**885k Params**  
**150M MACs**

# VGG-16

CONV Layers: 13

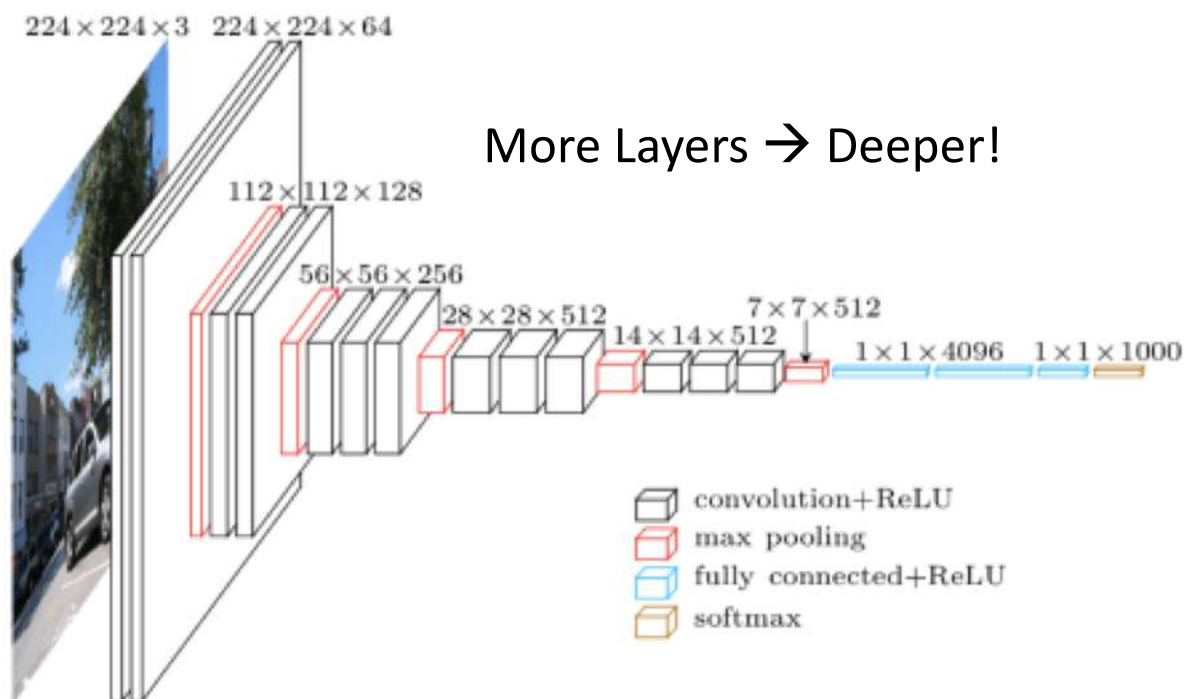
Fully Connected Layers: 3

Weights: 138M

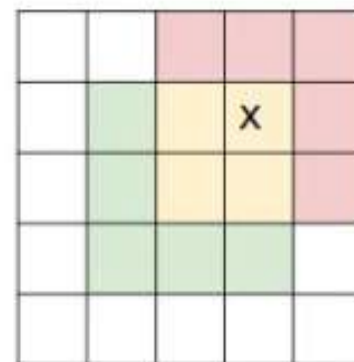
MACs: 15.5G

Also, 19 layer version

Reduce # of weights



stack 2  
3x3 conv



for a 5x5  
receptive field

[figure credit  
A. Karpathy]

Image Source: <http://www.cs.toronto.edu/~frossard/post/vgg16/>

# GoogLeNet/Inception (v1)

CONV Layers: 21 (depth), 57 (total)

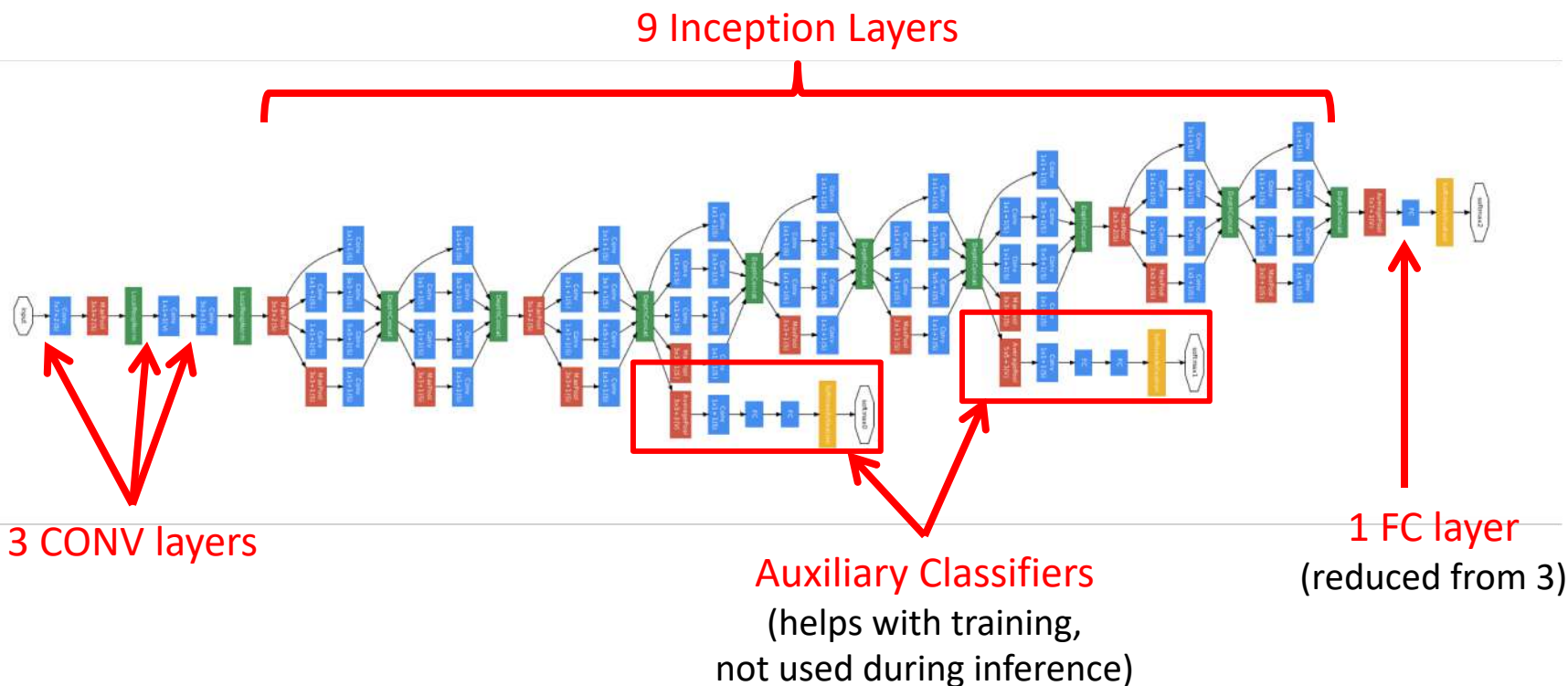
Fully Connected Layers: 1

Weights: 7.0M

MACs: 1.43G

Also, v2, v3 and v4

ILSVRC14 Winner



[Szegedy et al., arXiv 2014, CVPR 2015]

# GoogLeNet/Inception (v1)

CONV Layers: 21 (depth), 57 (total)

Fully Connected Layers: 1

Weights: 7.0M

MACs: 1.43G

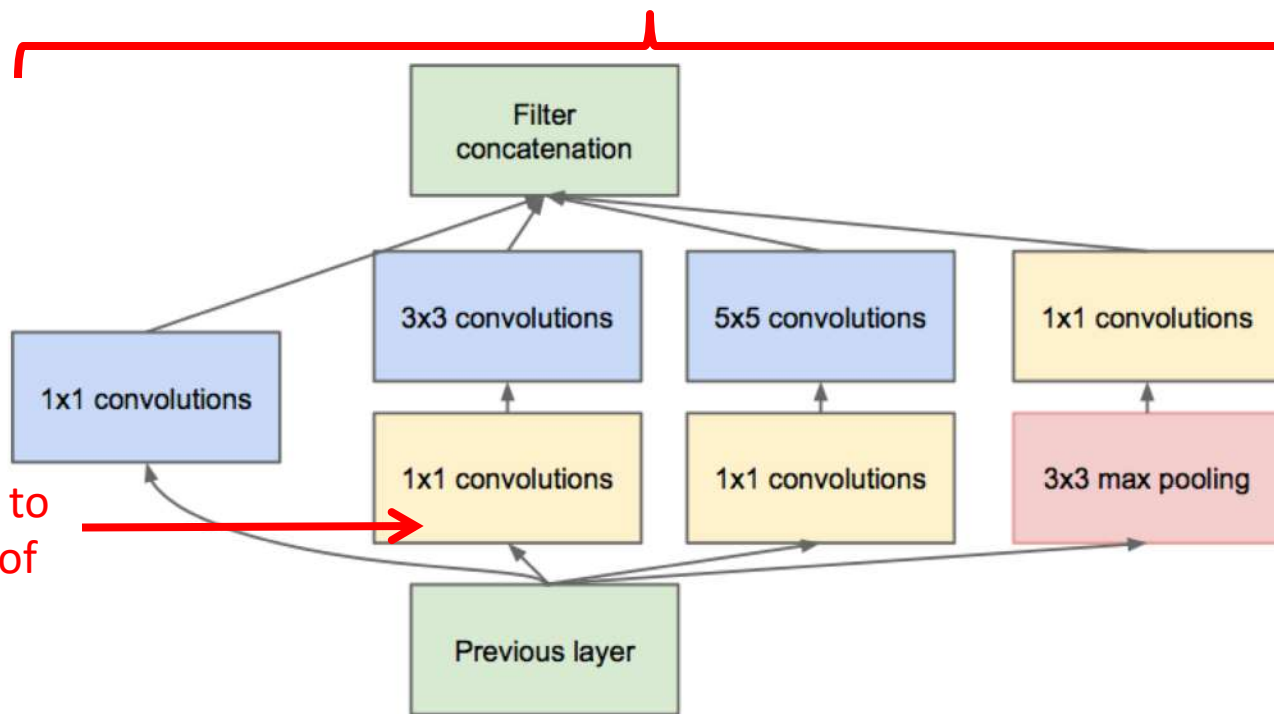
Also, v2, v3 and v4

ILSVRC14 Winner

parallel filters of different size have the effect of  
processing image at different scales

## Inception Module

1x1 'bottleneck' to  
reduce number of  
weights and  
multiplications



[Szegedy et al., arXiv 2014, CVPR 2015]

# ResNet

ILSVRC15 Winner  
(better than human level accuracy!)

Go Deeper!

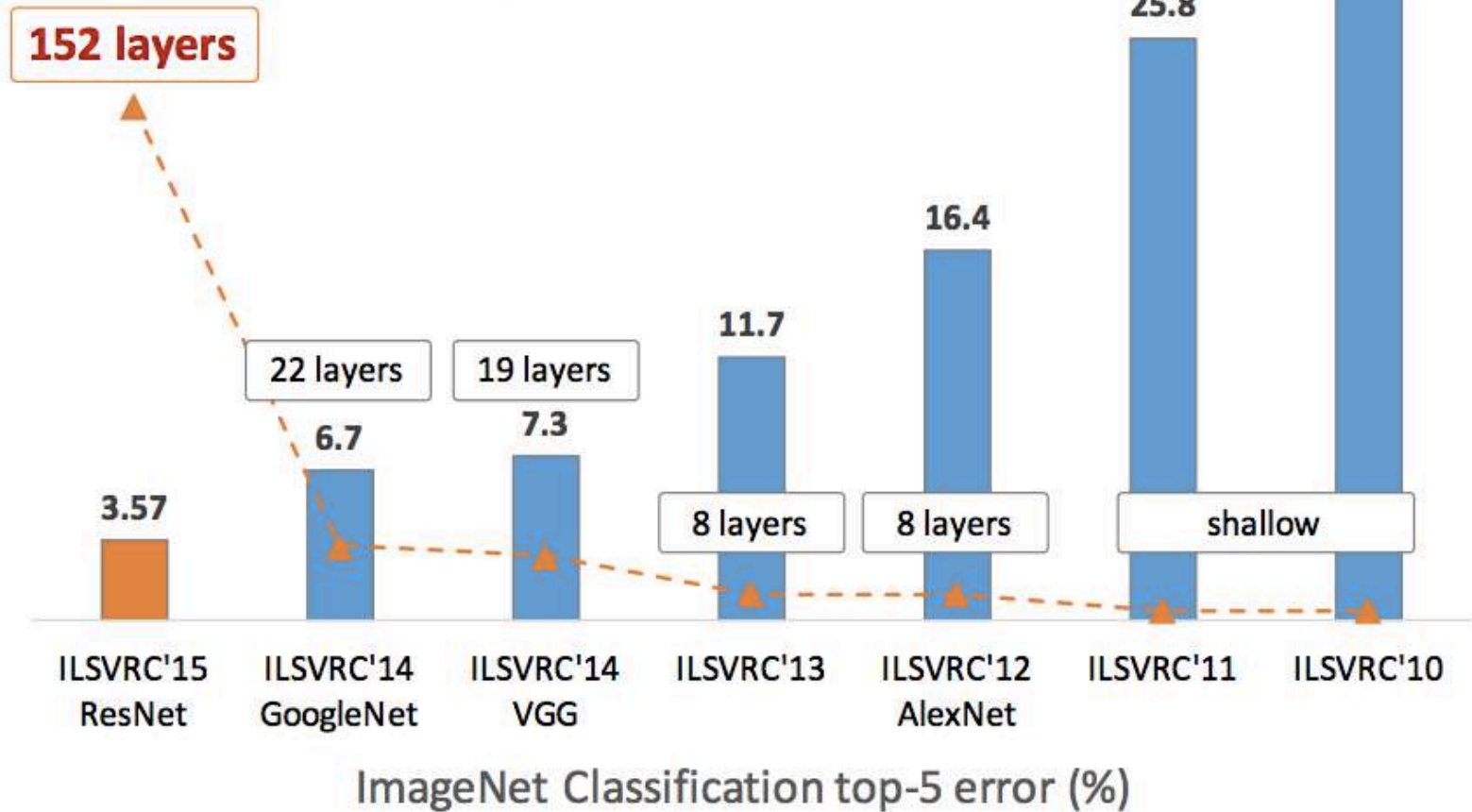


Image Source: [http://icml.cc/2016/tutorials/icml2016\\_tutorial\\_deep\\_residual\\_networks\\_kaiminghe.pdf](http://icml.cc/2016/tutorials/icml2016_tutorial_deep_residual_networks_kaiminghe.pdf)

# ResNet-50

CONV Layers: 49

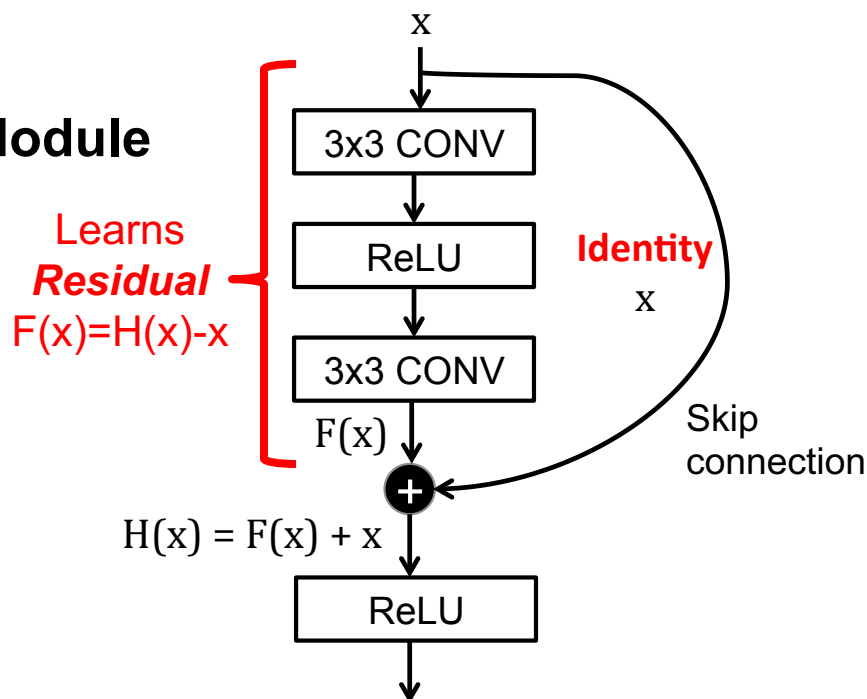
Fully Connected Layers: 1

Weights: 25.5M

MACs: 3.9G

Also, 34, **152** and 1202 layer versions  
ILSVRC15 Winner

## Short Cut Module



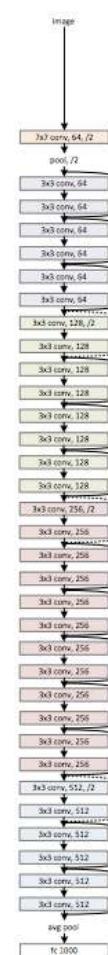
Helps address the vanishing gradient challenge for training very deep networks

## ResNet-34

1 CONV layer

16 Short Cut Layers

1 FC layer



# Summary of Popular CNNs

Metrics	LeNet-5	AlexNet	VGG-16	GoogLeNet (v1)	ResNet-50
Top-5 error	n/a	16.4	7.4	6.7	5.3
Input Size	28x28	227x227	224x224	224x224	224x224
<b># of CONV Layers</b>	<b>2</b>	<b>5</b>	<b>16</b>	<b>21 (depth)</b>	<b>49</b>
Filter Sizes	5	3, 5, 11	3	1, 3, 5, 7	1, 3, 7
# of Channels	1, 6	3 - 256	3 - 512	3 - 1024	3 - 2048
# of Filters	6, 16	96 - 384	64 - 512	64 - 384	64 - 2048
Stride	1	1, 4	1	1, 2	1, 2
# of Weights	2.6k	2.3M	14.7M	6.0M	23.5M
# of MACs	283k	666M	15.3G	1.43G	3.86G
<b># of FC layers</b>	<b>2</b>	<b>3</b>	<b>3</b>	<b>1</b>	<b>1</b>
# of Weights	58k	58.6M	124M	1M	2M
# of MACs	58k	58.6M	124M	1M	2M
<b>Total Weights</b>	<b>60k</b>	<b>61M</b>	<b>138M</b>	<b>7M</b>	<b>25.5M</b>
<b>Total MACs</b>	<b>341k</b>	<b>724M</b>	<b>15.5G</b>	<b>1.43G</b>	<b>3.9G</b>

CONV Layers increasingly important!

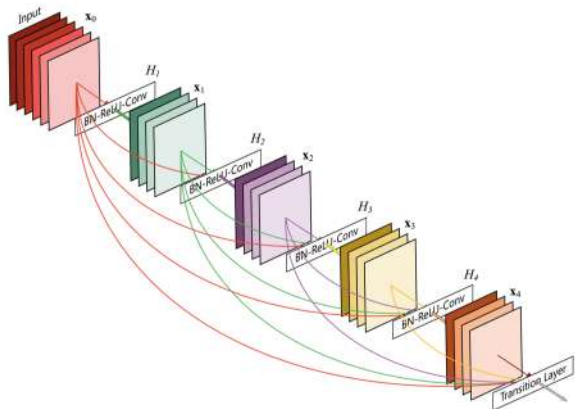
# Summary of Popular CNNs

- **AlexNet**
  - First CNN Winner of ILSVRC
  - Uses LRN (deprecated after this)
- **VGG-16**
  - Goes Deeper (16+ layers)
  - Uses only 3x3 filters (stack for larger filters)
- **GoogLeNet (v1)**
  - Reduces weights with Inception and only one FC layer
  - Inception: 1x1 and DAG (parallel connections)
  - Batch Normalization
- **ResNet**
  - Goes Deeper (24+ layers)
  - Shortcut connections



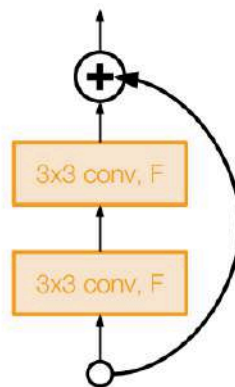
# Beyond ResNet

## DenseNet

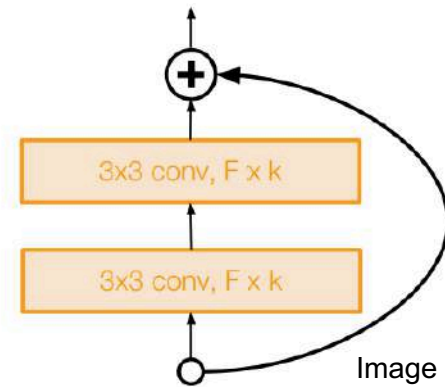


[Huang et al., CVPR 2017]

## Wide ResNet



Basic residual block

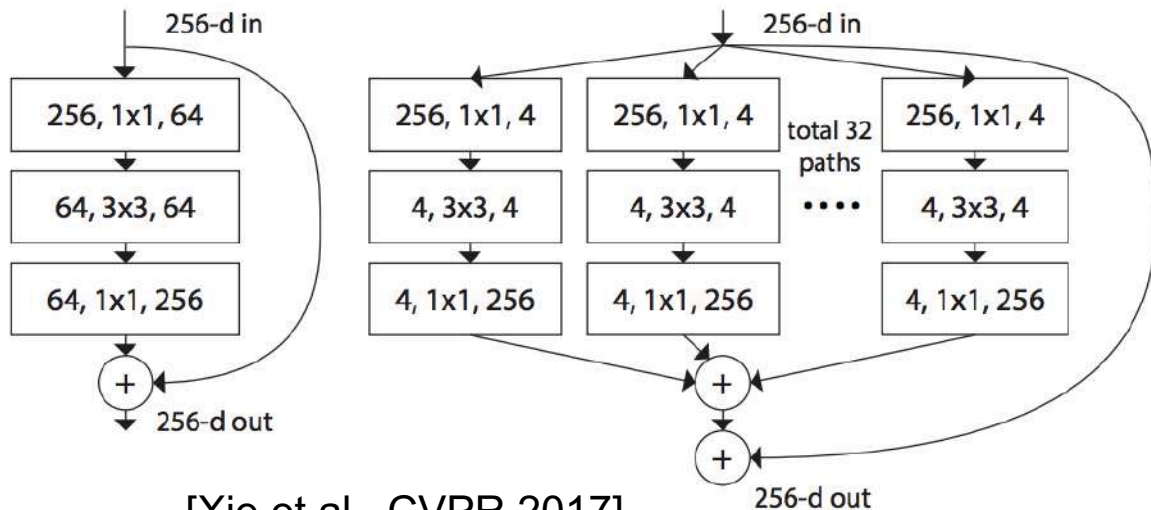


Wide residual block

Image Source:  
Stanford cs231n

## ResNeXt

[Zagoruyko et al., BMVC 2016]



[Xie et al., CVPR 2017]

Increase accuracy  
***without*** going deeper!

# Part 1: Hardware Platforms for DNN Processing

# GPUs and CPUs Targeting Deep Learning

Intel Xeon Scalable CPU (2019)

Nvidia's V100 GPU (2018)



**Use matrix multiplication libraries on CPUs and GPUs**

# Matrix Multiplication Libraries

- Implementation: **Matrix Multiplication (GEMM)**
  - **CPU:** OpenBLAS, Intel MKL, etc
  - **GPU:** cuBLAS, cuDNN, etc
- Library will note shape of the matrix multiply and select implementation optimized for that shape.
- Optimization usually involves proper tiling to storage hierarchy

# Map DNN to a Matrix Multiplication

Convolution:

$$\begin{array}{|c|c|} \hline 1 & 2 \\ \hline 3 & 4 \\ \hline \end{array} * \begin{array}{|c|c|c|} \hline 1 & 2 & 3 \\ \hline 4 & 5 & 6 \\ \hline 7 & 8 & 9 \\ \hline \end{array} = \begin{array}{|c|c|} \hline 1 & 2 \\ \hline 3 & 4 \\ \hline \end{array}$$



Matrix Mult:

$$\begin{array}{|c|c|c|c|} \hline 1 & 2 & 3 & 4 \\ \hline \end{array} \times \begin{array}{|c|c|c|c|} \hline 1 & 2 & 4 & 5 \\ \hline 2 & 3 & 5 & 6 \\ \hline 4 & 5 & 7 & 8 \\ \hline 5 & 6 & 8 & 9 \\ \hline \end{array} = \begin{array}{|c|c|c|c|} \hline 1 & 2 & 3 & 4 \\ \hline \end{array}$$

Toeplitz Matrix  
(w/ redundant data)

Data is repeated

**Goal:** Reduced number of operations to **increase throughput**

# Analogy: Gauss's Multiplication Algorithm

$$(a + bi)(c + di) = (ac - bd) + (bc + ad)i.$$

4 multiplications + 3 additions

$$k_1 = c \cdot (a + b)$$

$$k_2 = a \cdot (d - c)$$

$$k_3 = b \cdot (c + d)$$

$$\text{Real part} = k_1 - k_3$$

$$\text{Imaginary part} = k_1 + k_2.$$

3 multiplications + 5 additions

**Reduce** number of multiplications,  
but **increase** number of additions

# Reduce Operations in Matrix Multiplication

- **Fast Fourier Transform** [Mathieu, ICLR 2014]
  - **Pro:** Direct convolution  $O(N_o^2 N_f^2)$  to  $O(N_o^2 \log_2 N_o)$
  - **Con:** Increase storage requirements
- **Strassen** [Cong, ICANN 2014]
  - **Pro:**  $O(N^3)$  to  $(N^{2.807})$
  - **Con:** Numerical stability
- **Winograd** [Lavin, CVPR 2016]
  - **Pro:** 2.25x speed up for 3x3 filter
  - **Con:** Specialized processing depending on filter size

# Specialized Hardware (Accelerators)



# Properties We Can Leverage

- Operations exhibit **high parallelism**  
→ **high throughput** possible
- Memory Access is the Bottleneck

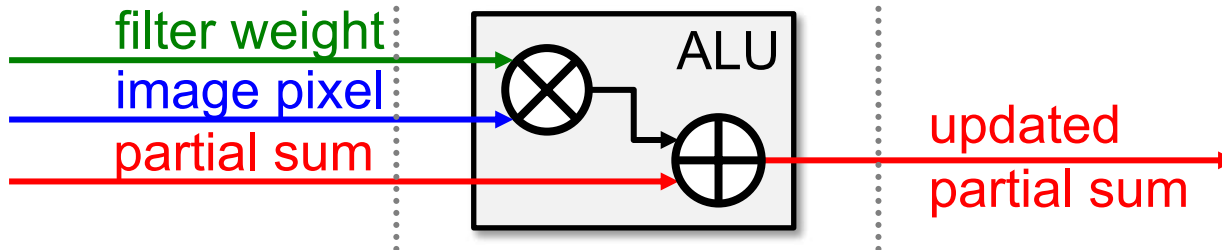
# Properties We Can Leverage

- Operations exhibit **high parallelism**  
→ **high throughput** possible
- Memory Access is the Bottleneck

Memory Read

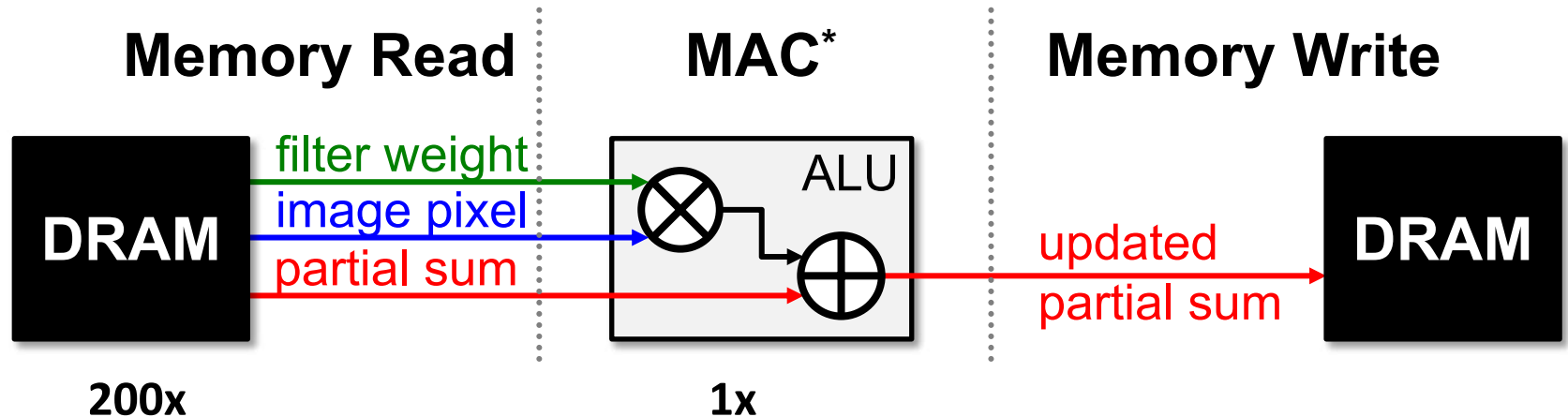
MAC\*

Memory Write



# Properties We Can Leverage

- Operations exhibit **high parallelism**  
→ **high throughput** possible
- Memory Access is the Bottleneck

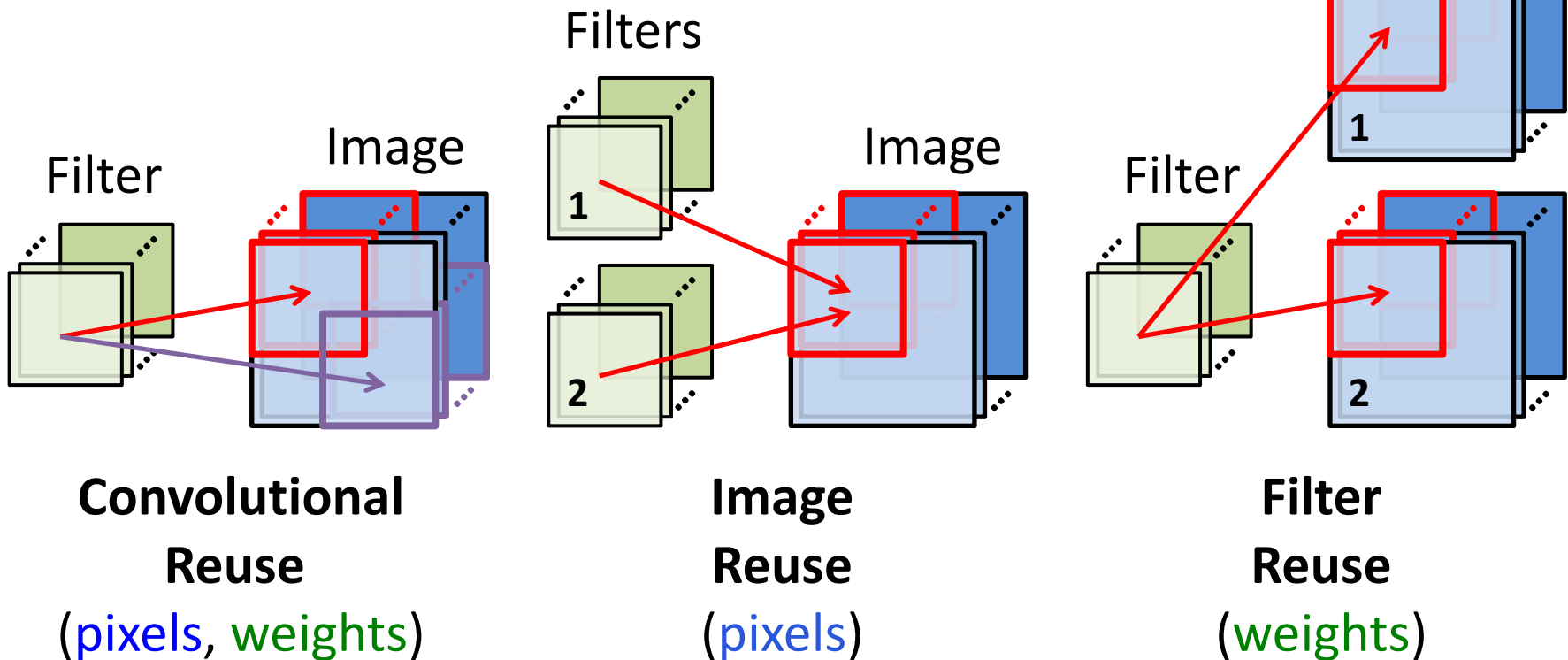


Worst Case: all memory R/W are **DRAM** accesses

- Example: AlexNet [NeurIPS 2012] has **724M** MACs  
→ **2896M** DRAM accesses required

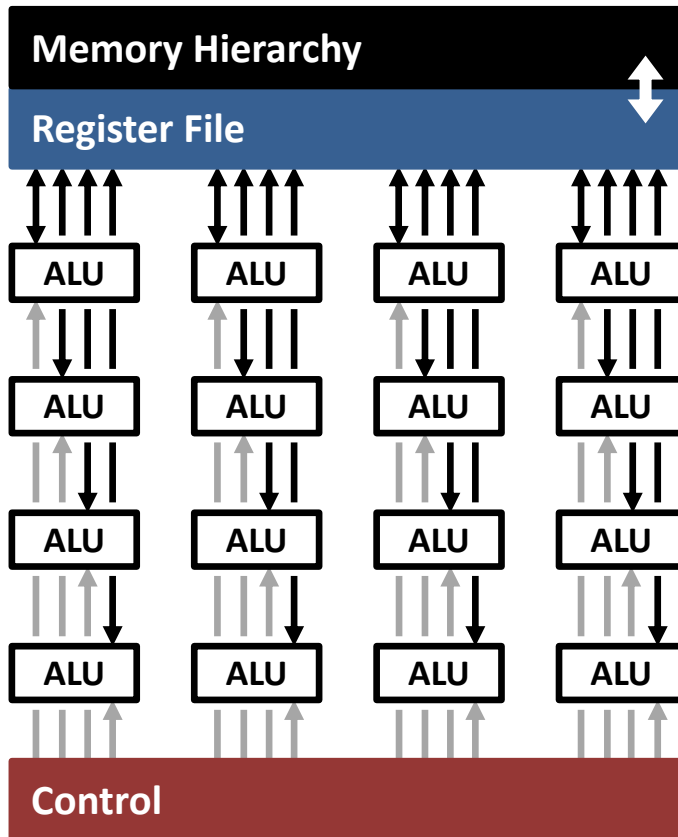
# Properties We Can Leverage

- Operations exhibit **high parallelism**  
→ **high throughput** possible
- Input data reuse** opportunities (**up to 500x**)  
→ exploit **low-cost memory**

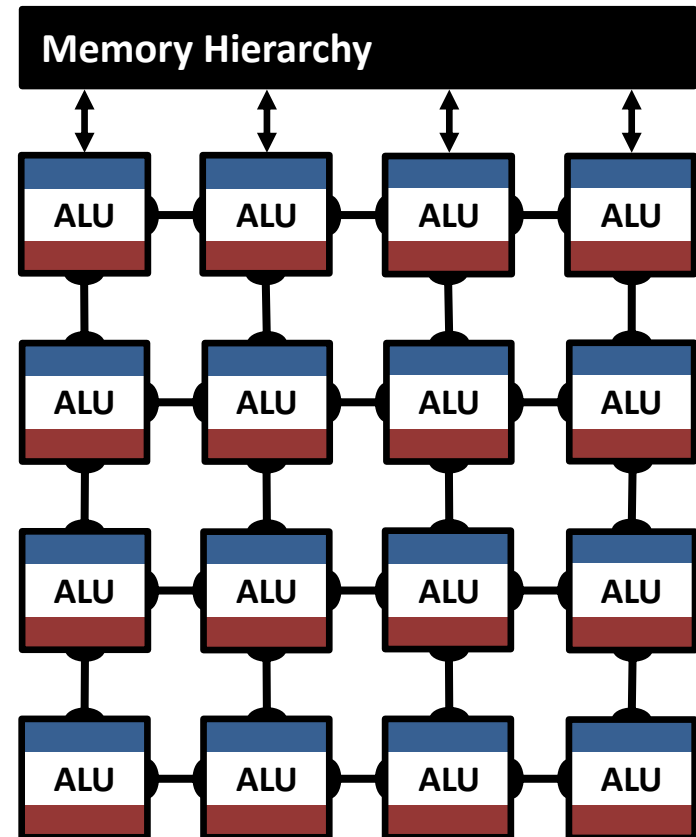


# Highly-Parallel Compute Paradigms

Temporal Architecture  
(SIMD/SIMT)



Spatial Architecture  
(Dataflow Processing)



# Advantages of Spatial Architecture

Temporal Architecture  
(SIMD/SIMT)

## Efficient Data Reuse

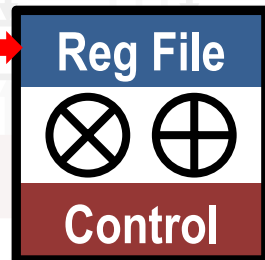
Distributed local storage (RF)

## Inter-PE Communication

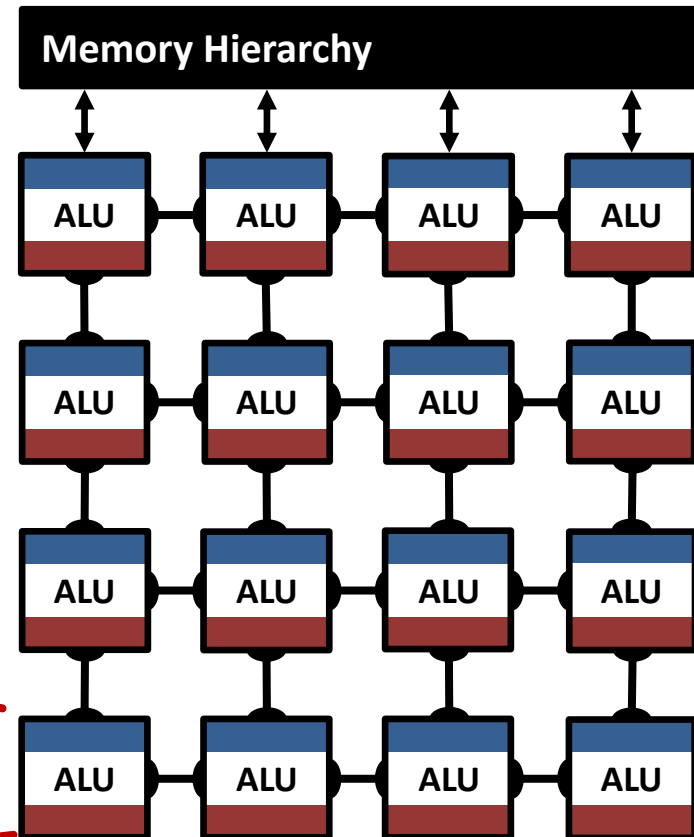
Sharing among regions of PEs

Processing  
Element (PE)

0.5 – 1.0 kB

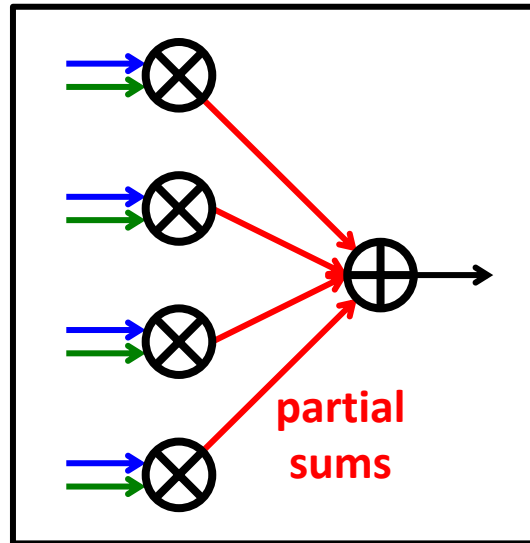


Spatial Architecture  
(Dataflow Processing)

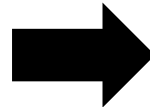


# How to Map the Dataflow?

## CNN Convolution

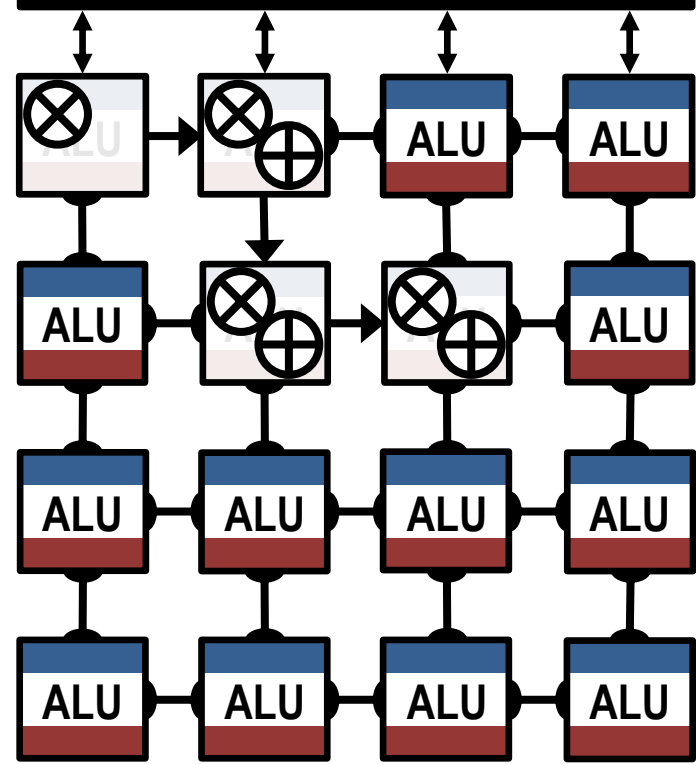


?



## Spatial Architecture (Dataflow Processing)

### Memory Hierarchy



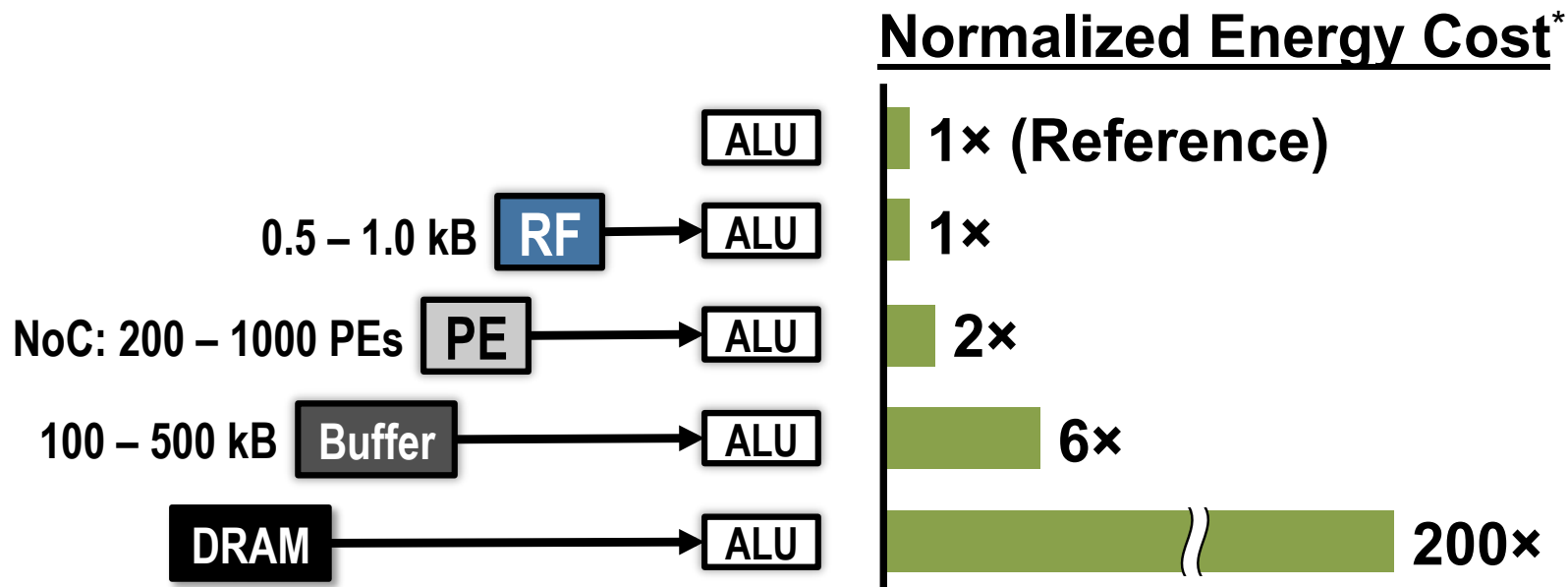
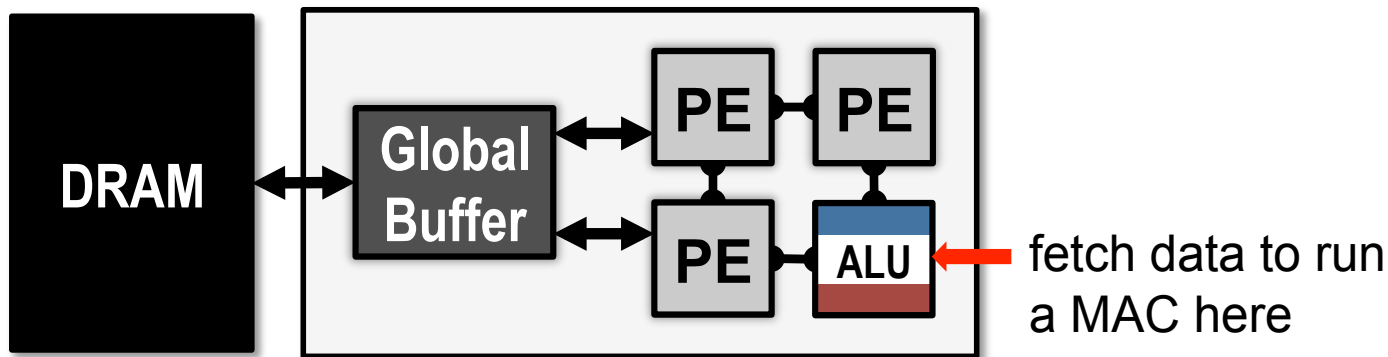
**Goal:** Increase reuse of input data  
(**weights** and **pixels**) and local  
**partial sums** accumulation

# Energy-Efficient Dataflow

Y.-H. Chen, J. Emer, V. Sze, “Eyeriss: A Spatial Architecture for Energy-Efficient Dataflow for Convolutional Neural Networks,” ISCA 2016



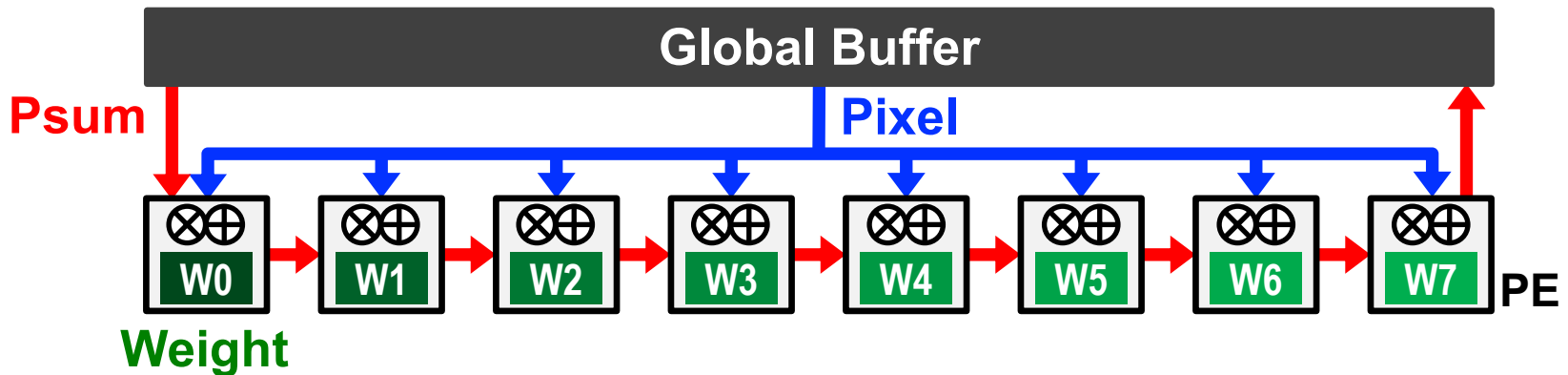
# Data Movement is Expensive



\* measured from a commercial 65nm process

**Maximize data reuse at low cost levels of hierarchy**

# Weight Stationary (WS)

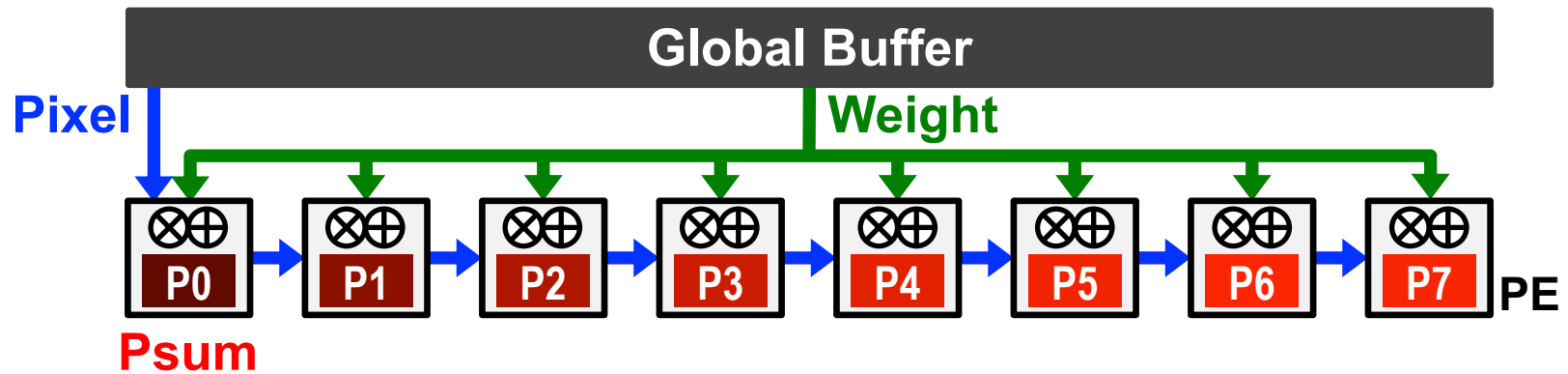


- **Minimize **weight**** read energy consumption
  - maximize convolutional and filter reuse of weights

- **Examples:**

[Chakradhar, *ISCA* 2010]    [nn-X (NeuFlow), *CVPRW* 2014]  
 [Park, *ISSCC* 2015]        [Origami, *GLSVLSI* 2015]

# Output Stationary (OS)



- Minimize **partial sum** R/W energy consumption
  - maximize local accumulation

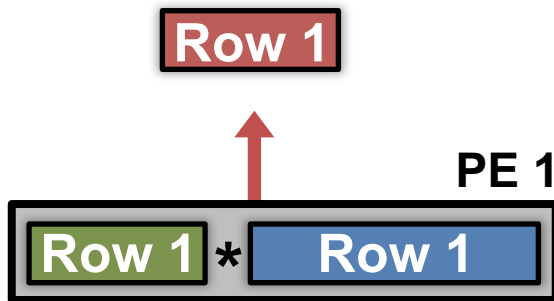
- **Examples:**

[Gupta, *ICML* 2015]

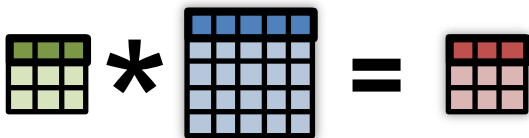
[ShiDianNao, *ISCA* 2015]

[Peemen, *ICCD* 2013]

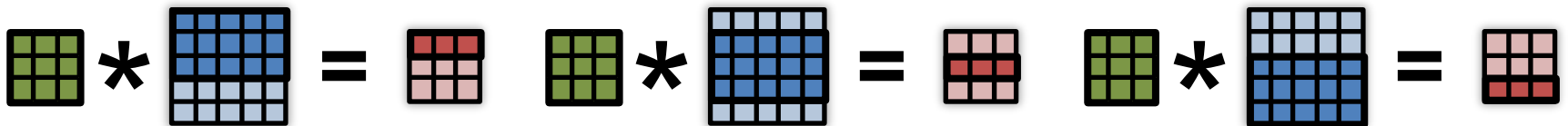
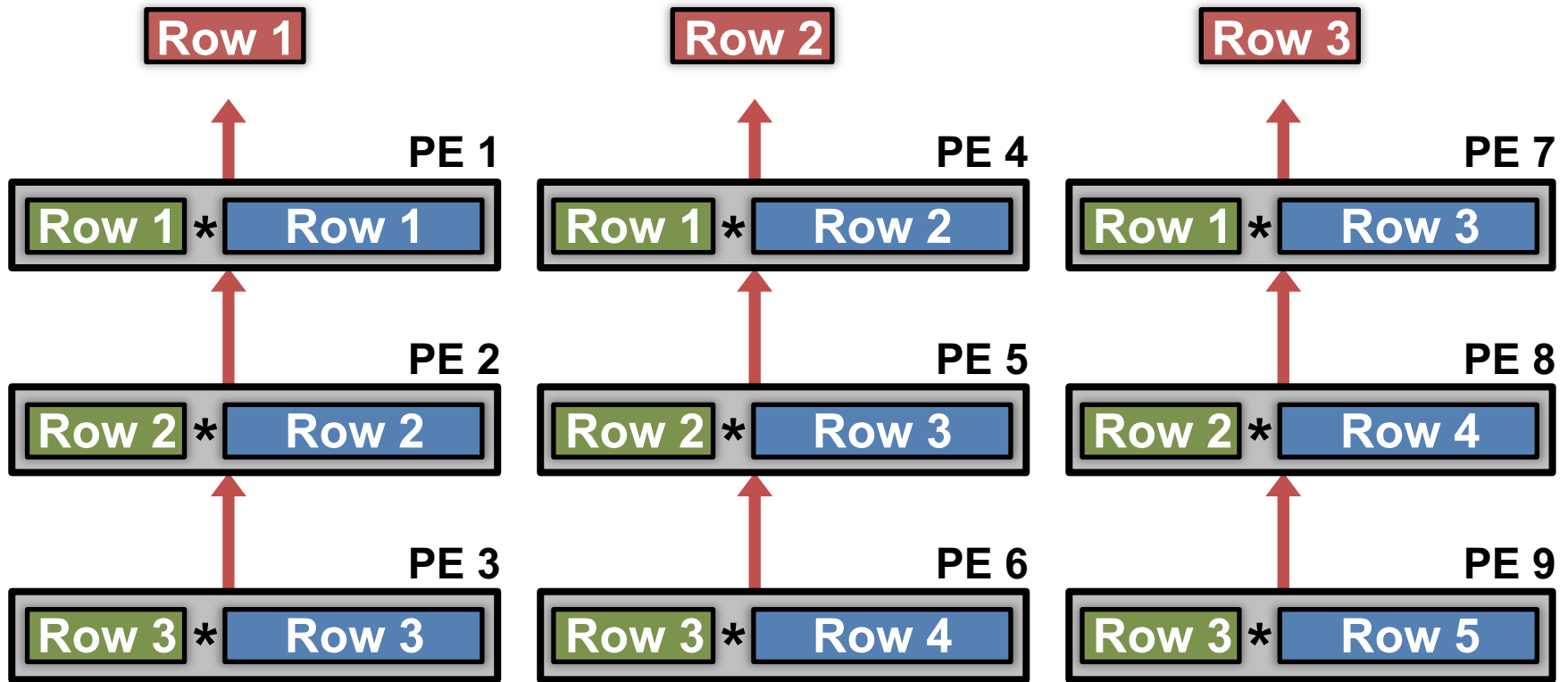
# Row Stationary Dataflow



- Maximize row **convolutional reuse** in RF
  - Keep a **filter** row and **fmap** sliding window in RF
- Maximize row **psum accumulation** in RF



# Row Stationary Dataflow



Optimize for **overall energy efficiency** instead  
for only a certain data type

# Evaluate Reuse in Different Dataflows

- **Weight Stationary**

- Minimize movement of filter weights

- **Output Stationary**

- Minimize movement of partial sums

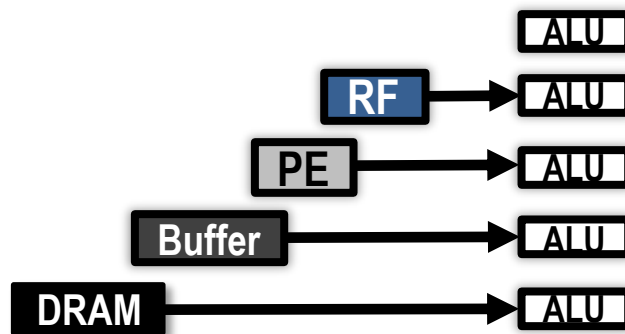
- **No Local Reuse**

- Don't use any local PE storage. Maximize global buffer size.

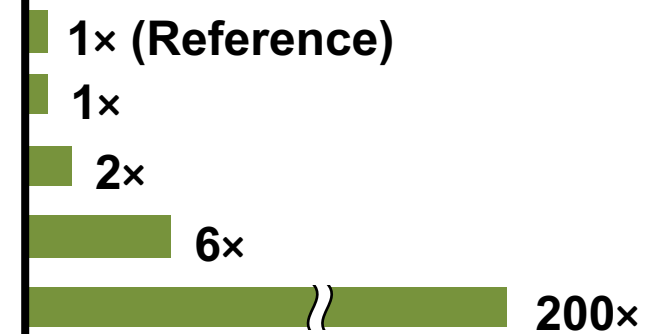
- **Row Stationary**

## Evaluation Setup

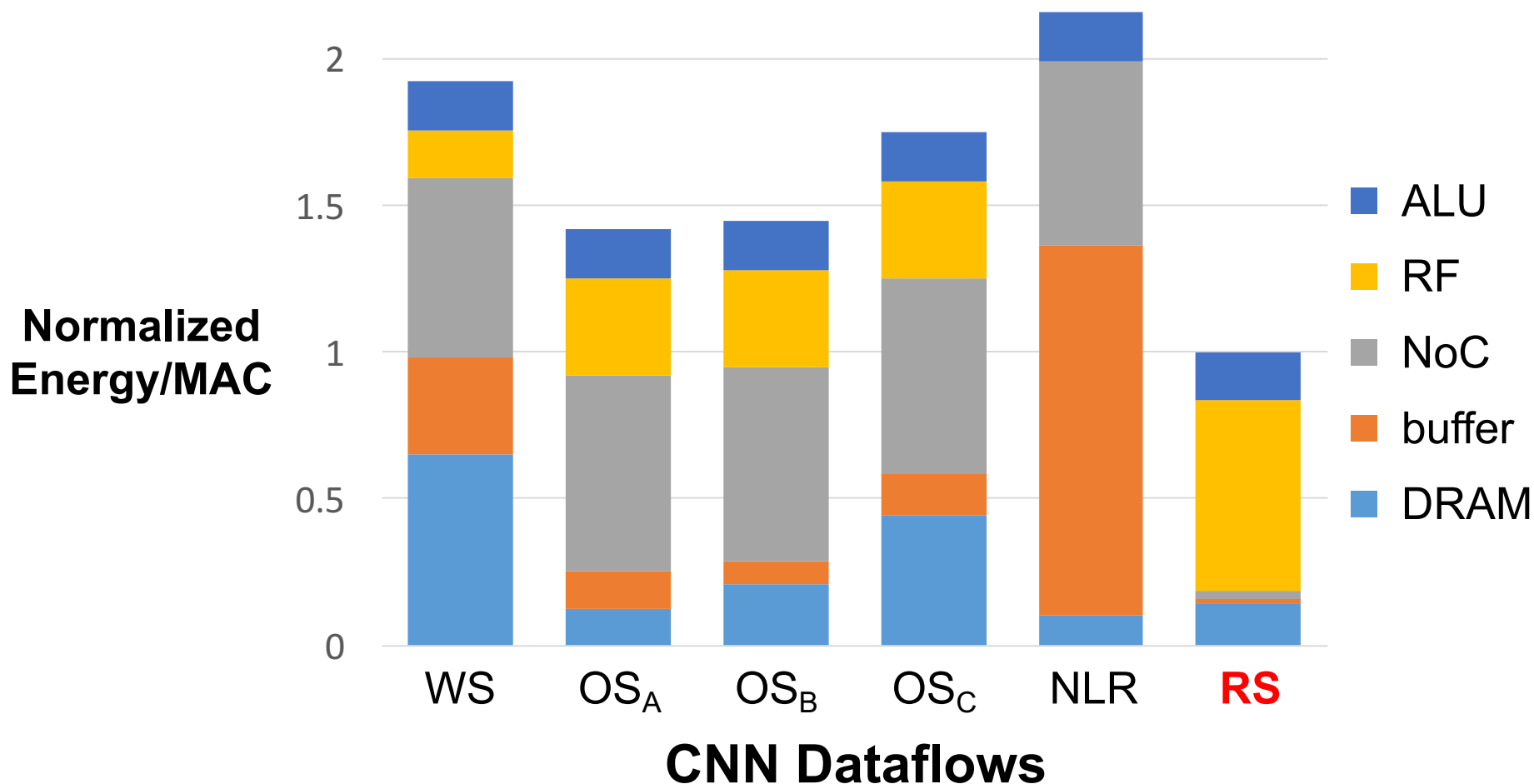
- Same Total Area
- AlexNet
- 256 PEs
- Batch size = 16



## Normalized Energy Cost\*

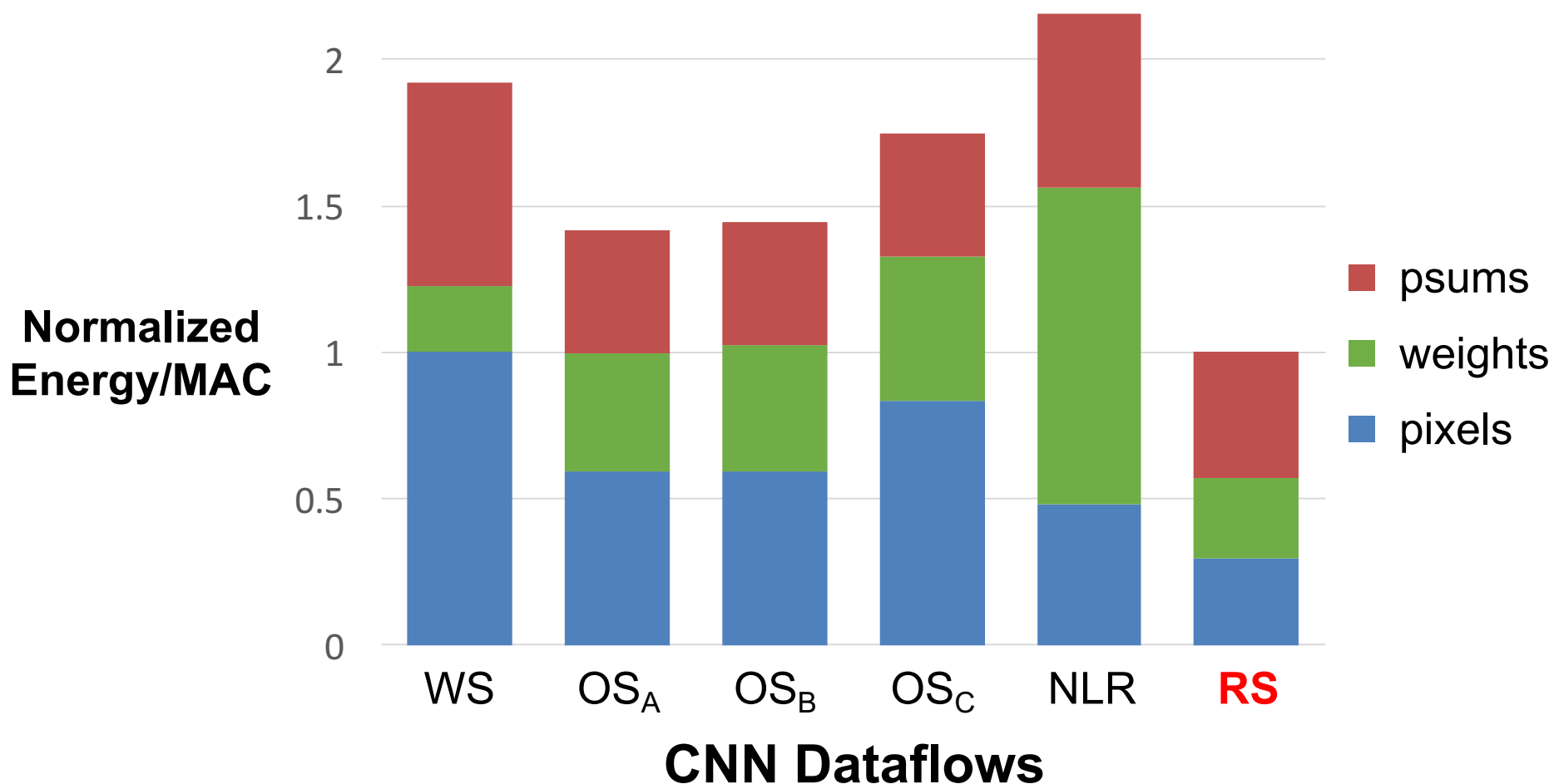


# Dataflow Comparison: CONV Layers



RS uses **1.4× – 2.5× lower** energy than other dataflows

# Dataflow Comparison: CONV Layers

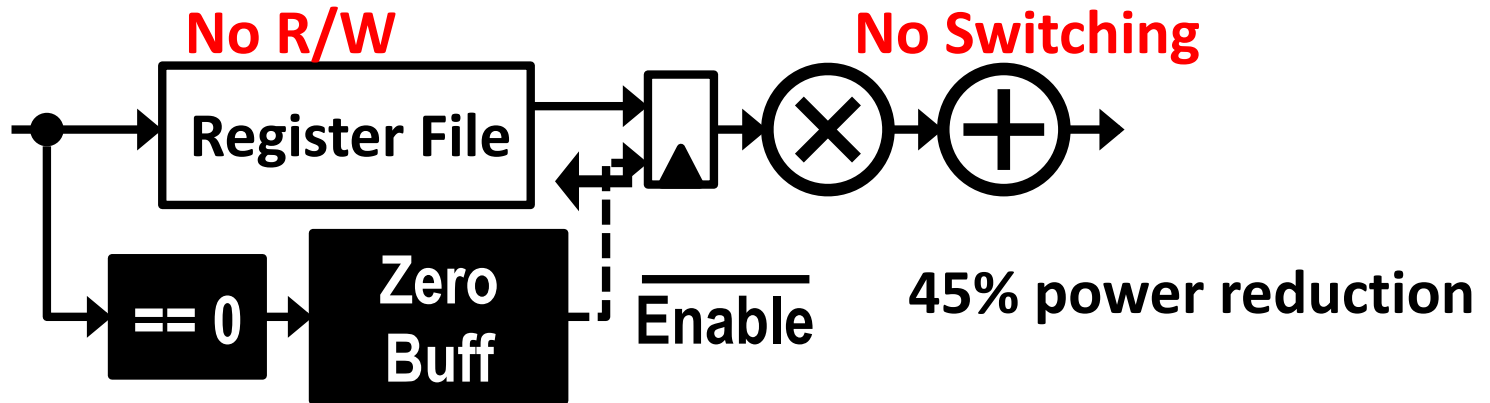


RS optimizes for the best **overall** energy efficiency

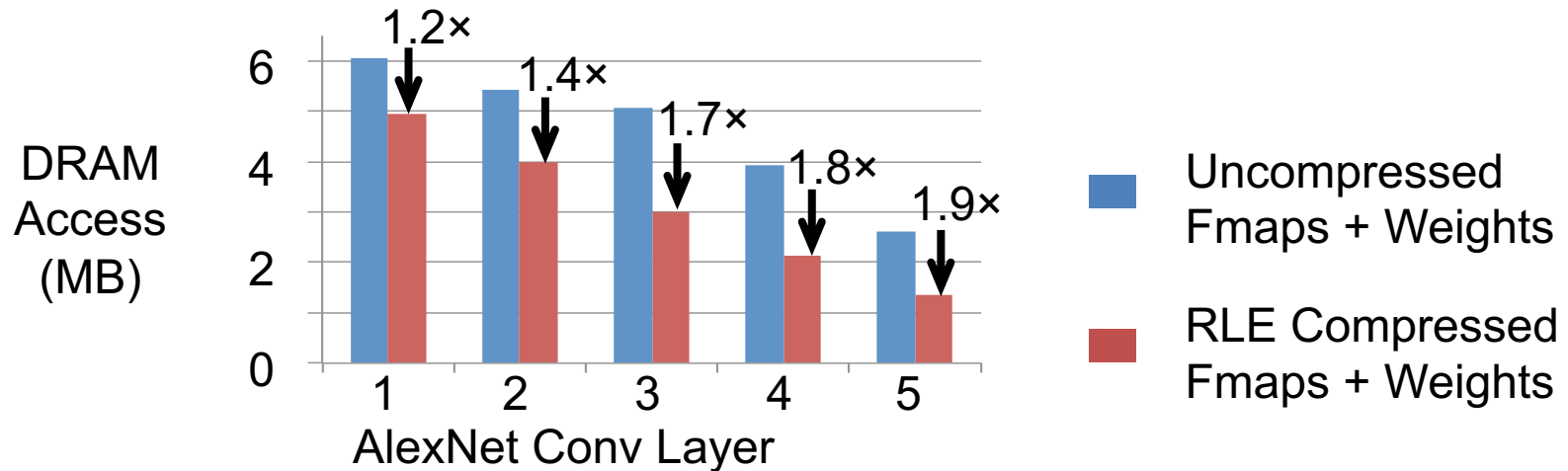


# Exploit Sparsity

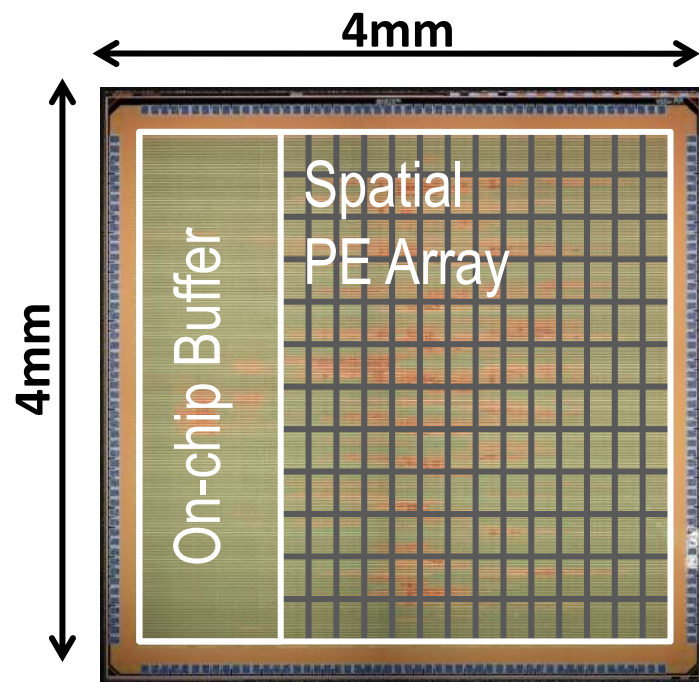
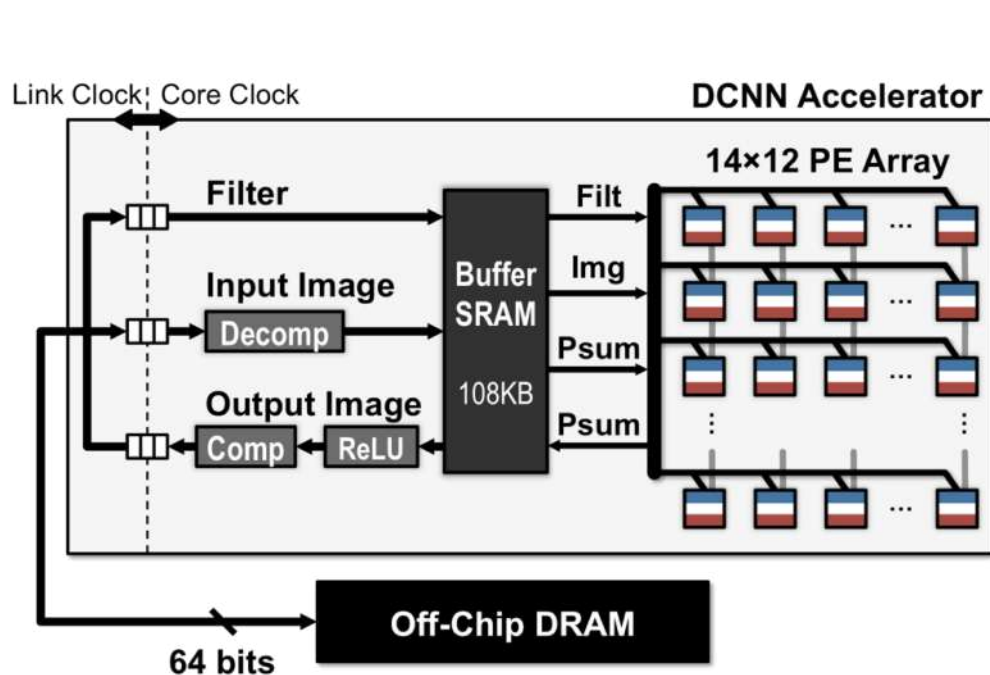
Method 1. Skip memory access and computation



Method 2. Compress data to reduce storage and data movement



# Eyeriss: Deep Neural Network Accelerator



[Chen et al., ISSCC 2016, ISCA 2016]

Exploits data reuse for **100x** reduction in memory accesses from global buffer and **1400x** reduction in memory accesses from off-chip DRAM

**Overall >10x energy reduction** compared to a mobile GPU (Nvidia TK1)

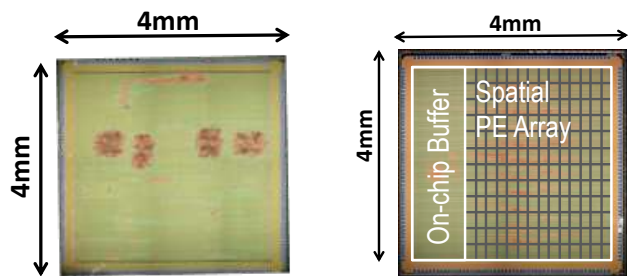
Results for AlexNet

# Features: Energy vs. Accuracy

*Exponential*

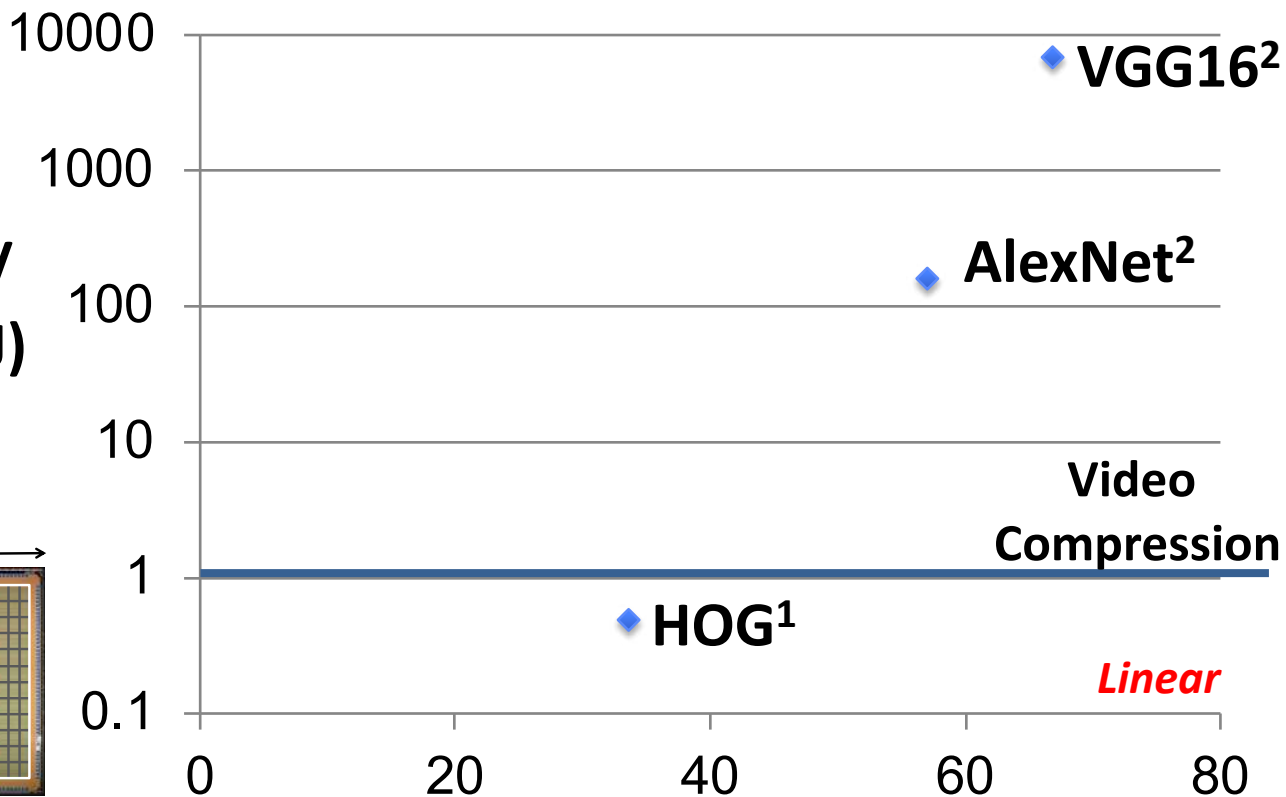
Energy/  
Pixel (nJ)

*Measured in 65nm\**



① [Suleiman, VLSI 2016]    ② [Chen, ISSCC 2016]

\* Only feature extraction. Does not include data, classification energy, augmentation and ensemble, etc.



Accuracy (Average Precision)

*Measured in on VOC 2007 Dataset*

1. DPM v5 [Girshick, 2012]
2. Fast R-CNN [Girshick, CVPR 2015]

# Benchmarking Metrics for DNN Hardware

*How can we compare designs?*

V. Sze, Y.-H. Chen, T.-J. Yang, J. Emer,

***“Efficient Processing of Deep Neural Networks: A Tutorial and Survey,”***

Proceedings of the IEEE, Dec. 2017

# Metrics for DNN Hardware

- **Accuracy**
  - Quality of result for a given task
- **Throughput**
  - Analytics on high volume data
  - Real-time performance (e.g., video at 30 fps)
- **Latency**
  - For interactive applications (e.g., autonomous navigation)
- **Energy and Power**
  - Edge and embedded devices have limited battery capacity
  - Data centers have stringent power ceilings due to cooling costs
- **Hardware Cost**
  - \$\$\$

# Specifications to Evaluate Metrics

- **Accuracy**
  - Difficulty of dataset and/or task should be considered
- **Throughput**
  - Number of cores (include utilization along with peak performance)
  - Runtime for running specific DNN models
- **Latency**
  - Include batch size used in evaluation
- **Energy and Power**
  - Power consumption for running specific DNN models
  - Include external memory access
- **Hardware Cost**
  - On-chip storage, number of cores, chip area + process technology

## Example: Metrics of Eyeriss Chip

ASIC Specs	Input
Process Technology	65nm LP TSMC (1.0V)
Total Core Area (mm <sup>2</sup> )	12.25
Total On-Chip Memory (kB)	192
Number of Multipliers	168
Clock Frequency (MHz)	200
Core area (mm <sup>2</sup> ) / multiplier	0.073
On-Chip memory (kB) / multiplier	1.14
Measured or Simulated	Measured

Metric	Units	Input
Name of CNN Model	Text	AlexNet
Top-5 error classification on ImageNet	#	19.8
Supported Layers		All CONV
Bits per weight	#	16
Bits per input activation	#	16
Batch Size	#	4
Runtime	ms	115.3
Power	mW	278
Off-chip Access per Image Inference	MBytes	3.85
Number of Images Tested	#	100

## Comprehensive Coverage

- **All metrics** should be reported for fair evaluation of design tradeoffs
- Examples of what can happen if certain metric is omitted:
  - **Without the accuracy given for a specific dataset and task**, one could run a simple DNN and claim low power, high throughput, and low cost – however, the processor might not be usable for a meaningful task
  - **Without reporting the off-chip bandwidth**, one could build a processor with only multipliers and claim low cost, high throughput, high accuracy, and low chip power – however, when evaluating system power, the off-chip memory access would be substantial
- Are results measured or simulated? On what test data?



# Evaluation Process

The evaluation process for whether a DNN system is a viable solution for a given application might go as follows:

1. **Accuracy** determines if it can perform the given task
2. **Latency and throughput** determine if it can run fast enough and in real-time
3. **Energy and power consumption** will primarily dictate the form factor of the device where the processing can operate
4. **Cost**, which is primarily dictated by the chip area, determines how much one would pay for this solution

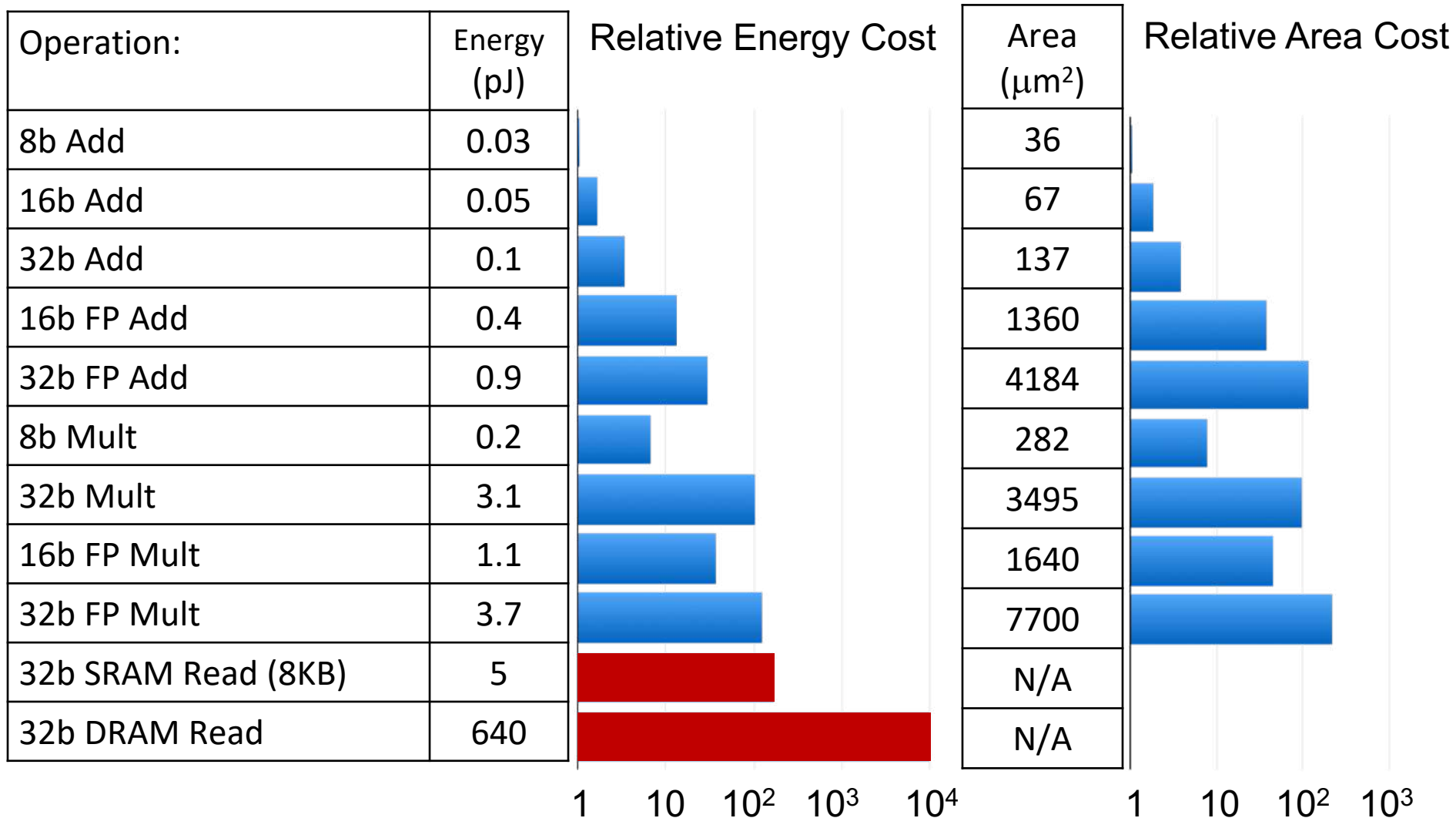
# Part 2: Co-Design of Algorithms and Hardware for DNNs

# Approaches

- **Reduce size of operands for storage/compute**
  - Floating point → Fixed point
  - Bit-width reduction
  - Non-linear quantization
- **Reduce number of operations for storage/compute**
  - Exploit Activation Statistics (Compression)
  - Network Pruning
  - Compact Network Architectures

# Reduced Precision

# Cost Per Operation



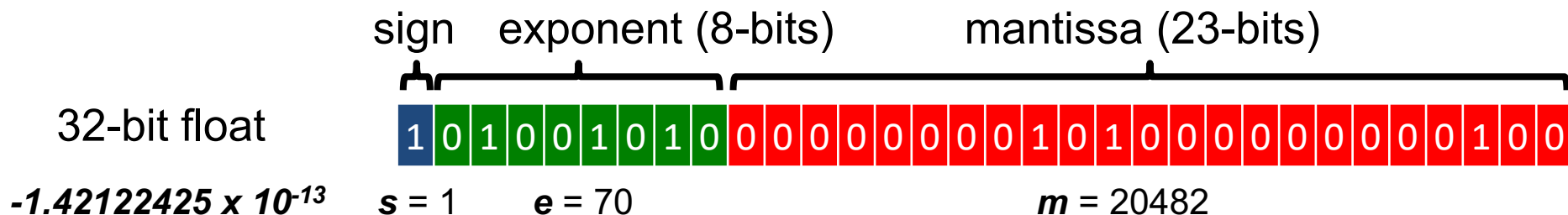
# 81 Floating Point → Fixed Point

Mantissa (**m**): number of levels

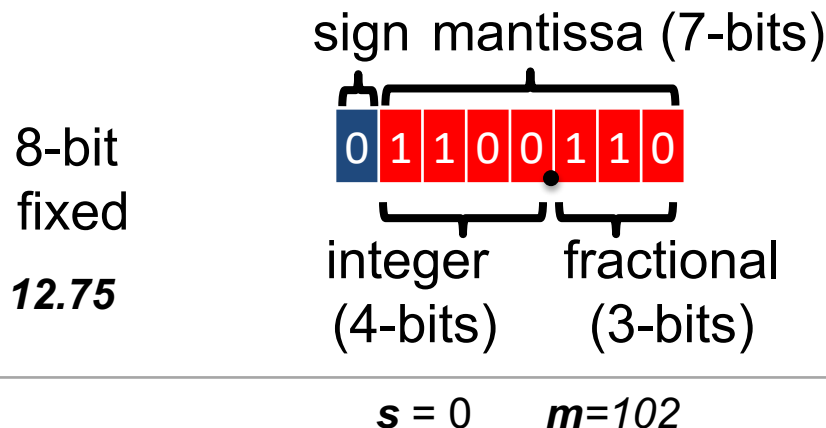
Exponent (**e**): scale to a target range

Sign (**s**): indicates if number is positive or negative

**Floating Point**  $(-1)^s \times m \times 2^{(e-127)}$



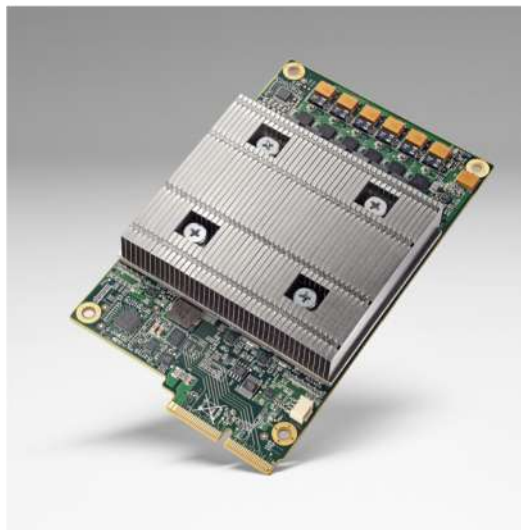
**Fixed Point**  $(-1)^s \times m$



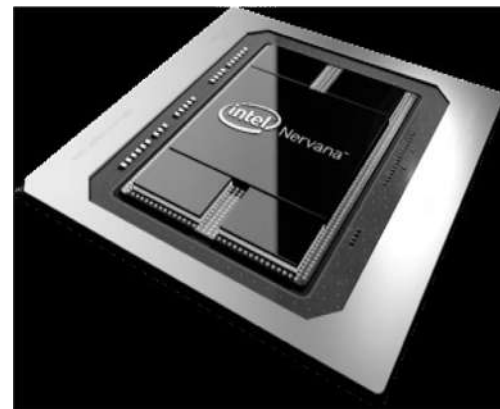
# Commercial Products Support Reduced Precision



Nvidia's Pascal (2016)

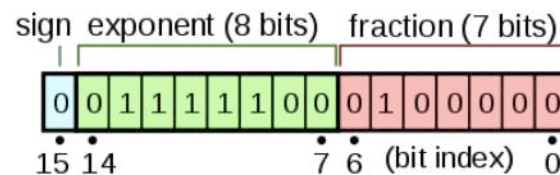


Google's TPU (2016)



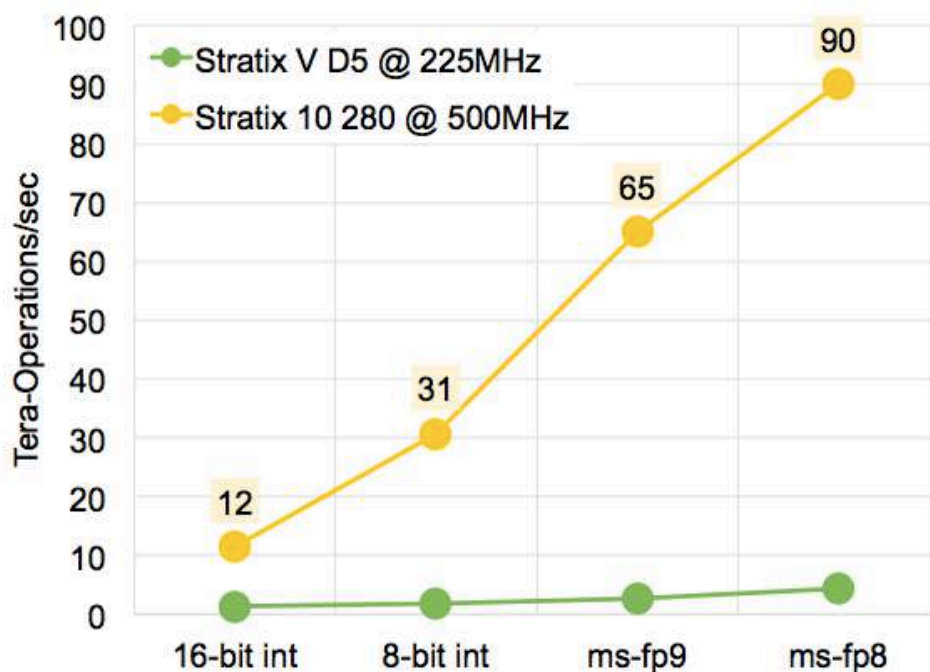
Intel's NNP-L (2019)

8-bit Inference & bfloat16 for Training

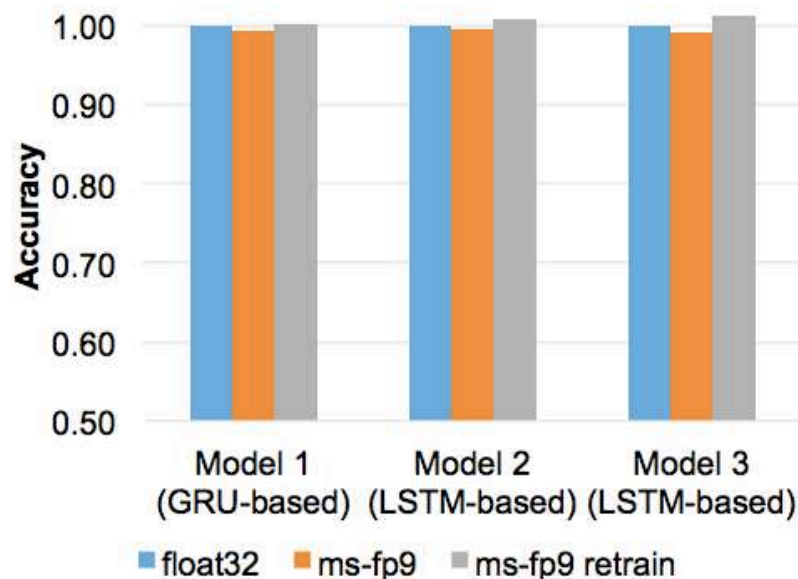


## Narrow Precision for Inference

FPGA Performance vs. Data Type



Impact of Narrow Precision on Accuracy



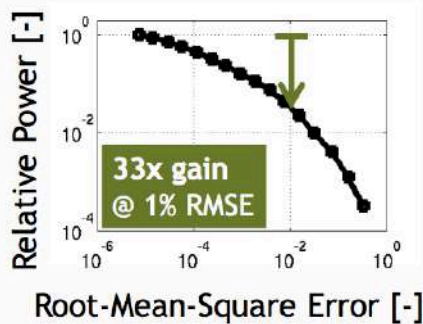
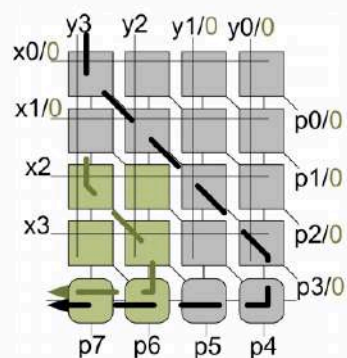
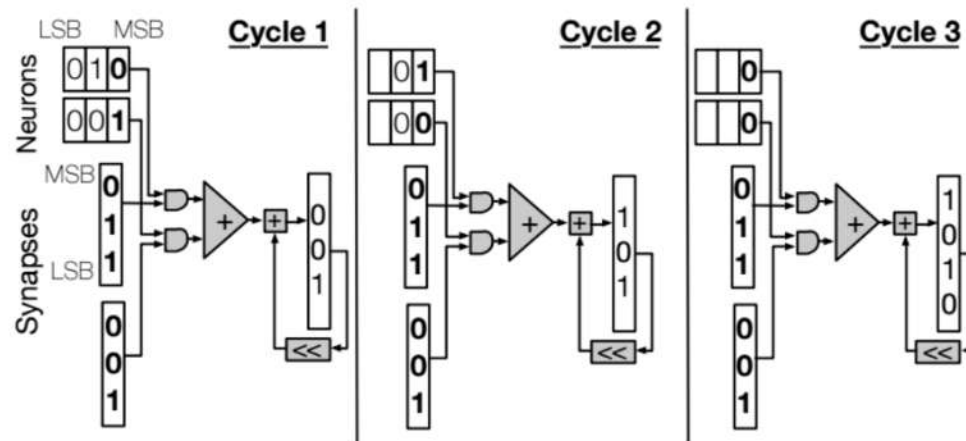
*Custom 8-bit floating point format (“ms-fp8”)*



## Stripes

[Judd et al., MICRO 2016]

Bit-serial processing for speed



$$P_{\text{precise}} = \alpha C f V^2 \Rightarrow P_{\text{imprecise}} = \frac{\alpha}{k_1} C f \left(\frac{V}{k_2}\right)^2$$

KU Leuven

[Moons et al., VLSI 2016]

Voltage scaling for energy savings

# Binary Nets

- **Binary Connect (BC)**

- Weights  $\{-1,1\}$ , Activations 32-bit float
- MAC  $\rightarrow$  addition/subtraction
- Accuracy loss: **19%** on AlexNet

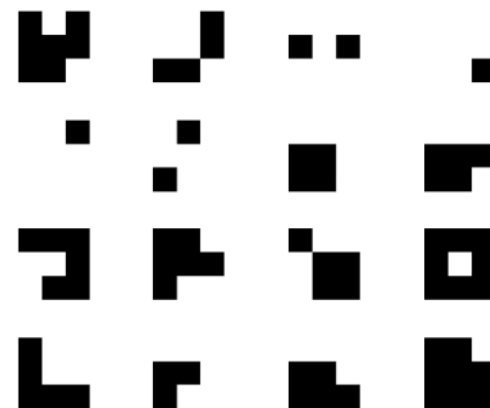
[Courbariaux, NeurIPS 2015]

- **Binarized Neural Networks (BNN)**

- Weights  $\{-1,1\}$ , Activations  $\{-1,1\}$
- MAC  $\rightarrow$  XNOR
- Accuracy loss: **29.8%** on AlexNet

[Courbariaux, arXiv 2016]

*Binary Filters*



# Scale the Weights and Activations

- **Binary Weight Nets (BWN)**

- Weights  $\{-\alpha, \alpha\} \rightarrow$  except first and last layers are 32-bit float
- Activations: 32-bit float
- $\alpha$  determined by the  $l_1$ -norm of all weights in a filter
- Accuracy loss: **0.8%** on AlexNet

- **XNOR-Net**

- Weights  $\{-\alpha, \alpha\}$
- Activations  $\{-\beta_i, \beta_i\} \rightarrow$  except first and last layers are 32-bit float
- $\beta_i$  determined by the  $l_1$ -norm of all activations across channels **for given position  $i$**  of the input feature map
- Accuracy loss: **11%** on AlexNet

Hardware needs to support both activation precisions

Scale factors ( $\alpha, \beta_i$ ) can change per filter or position in filter

[Rastegari et al., BWN & XNOR-Net, ECCV 2016]

# Ternary Nets

- **Allow for weights to be zero**
  - Increase sparsity, but also increase number of bits (2-bits)
- **Ternary Weight Nets (TWN)** [Li et al., arXiv 2016]
  - Weights  $\{-w, 0, w\} \rightarrow$  except first and last layers are 32-bit float
  - Activations: 32-bit float
  - Accuracy loss: 3.7% on AlexNet
- **Trained Ternary Quantization (TTQ)** [Zhu et al., ICLR 2017]
  - Weights  $\{-w_1, 0, w_2\} \rightarrow$  except first and last layers are 32-bit float
  - Activations: 32-bit float
  - Accuracy loss: 0.6% on AlexNet

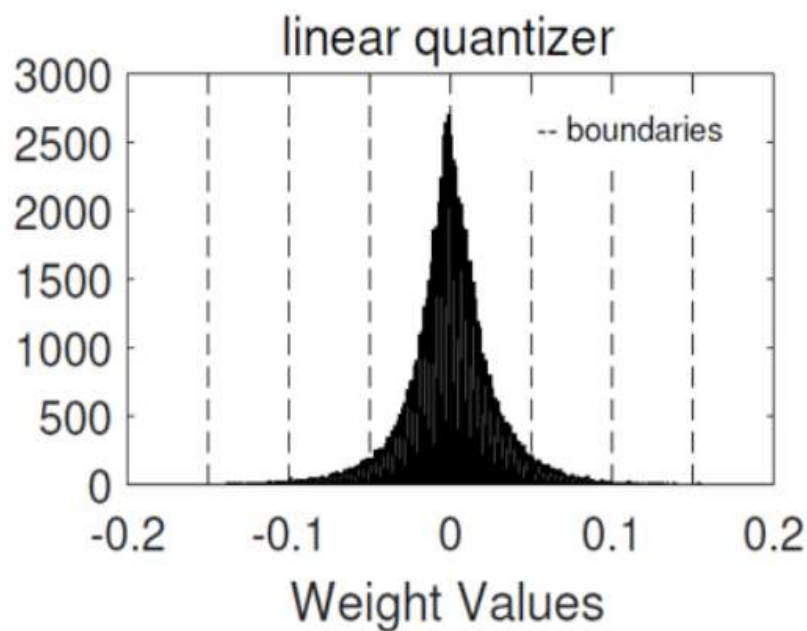
# Non-Linear Quantization

- **Precision** refers to the **number of levels**
  - Number of bits =  $\log_2$  (number of levels)
- **Quantization:** mapping data to a smaller set of **levels**
  - Linear, e.g., fixed-point
  - Non-linear
    - Computed
    - Table lookup

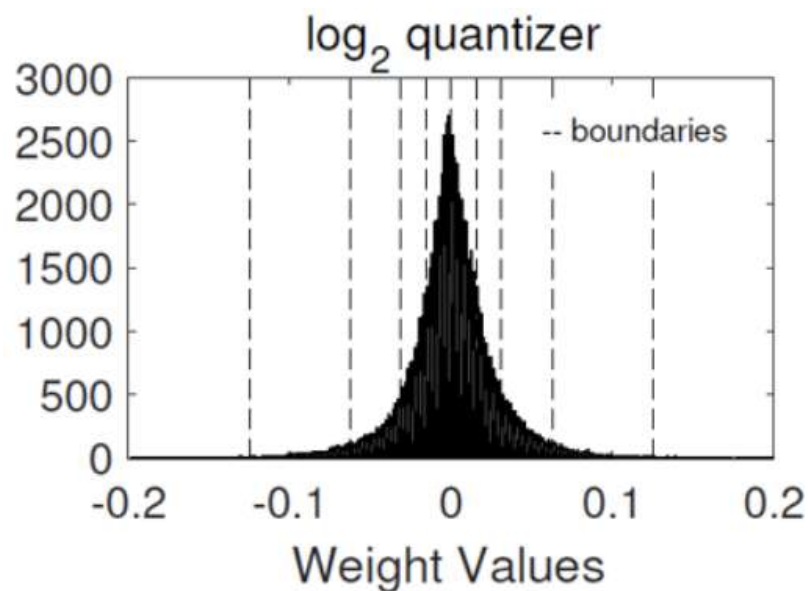
Objective: Reduce size to improve speed and/or reduce energy while preserving accuracy

# Computed Non-linear Quantization

## Log Domain Quantization



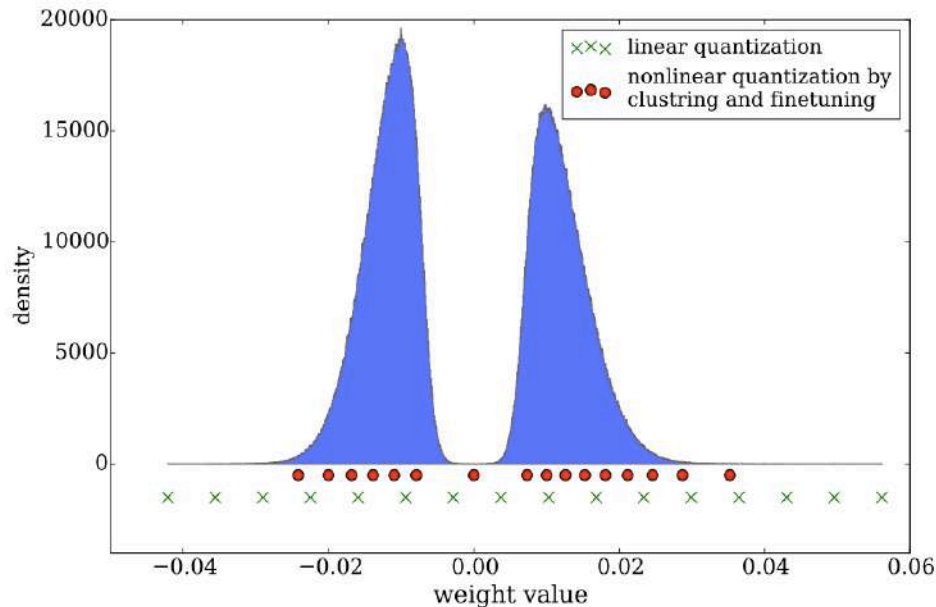
$$\text{Product} = X * W$$



$$\text{Product} = X \ll W$$

# Reduce Precision Overview

- Learned mapping of data to quantization levels (e.g., k-means)



*Implement with  
look up table*

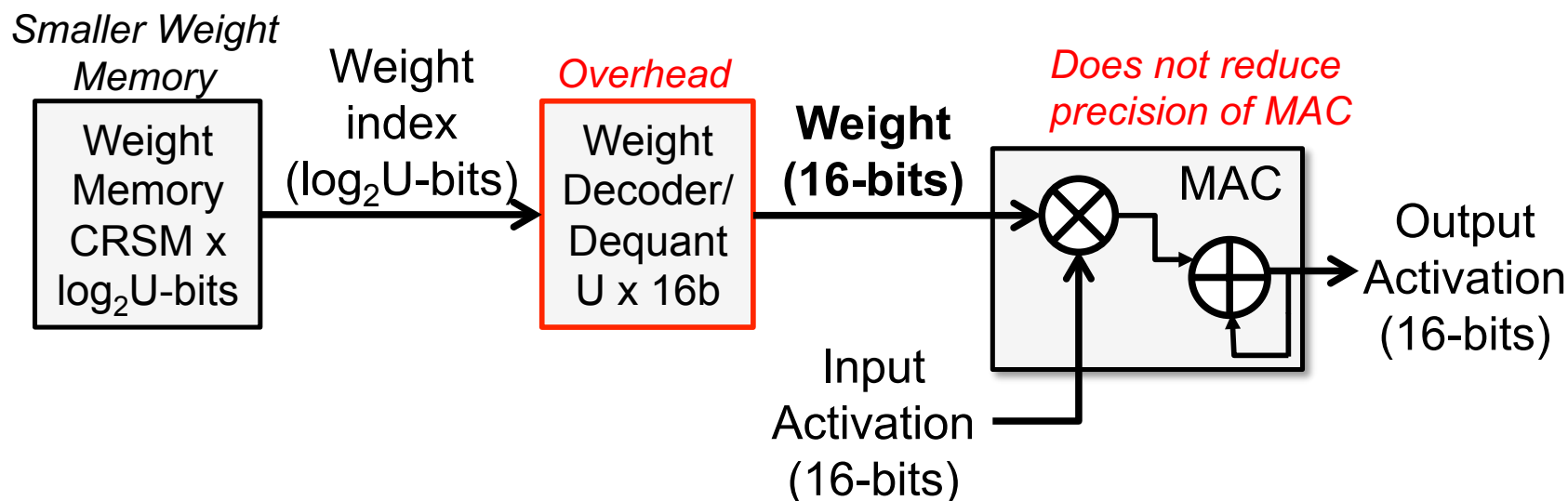
[Han et al., ICLR 2016]

- Additional Properties
  - Fixed or Variable (across data types, layers, channels, etc.)

# Non-Linear Quantization Table Lookup

**Trained Quantization:** Find  $K$  weights via  $K$ -means clustering to reduce number of unique weights *per layer* (weight sharing)

**Example:** AlexNet (no accuracy loss)  
**256 unique weights** for CONV layer  
**16 unique weights** for FC layer



Consequences: Narrow weight memory and second access from (small) table



# Summary of Reduce Precision

Category	Method	Weights (# of bits)	Activations (# of bits)	Accuracy Loss vs. 32-bit float (%)
Dynamic Fixed Point	w/o fine-tuning	8	10	0.4
	w/ fine-tuning	8	8	0.6
Reduce weight	Ternary weights Networks (TWN)	2*	32	3.7
	Trained Ternary Quantization (TTQ)	2*	32	0.6
	Binary Connect (BC)	1	32	19.2
	Binary Weight Net (BWN)	1*	32	0.8
Reduce weight and activation	Binarized Neural Net (BNN)	1	1	29.8
	XNOR-Net	1*	1	11
Non-Linear	LogNet	5(conv), 4(fc)	4	3.2
	Weight Sharing	8(conv), 4(fc)	16	0

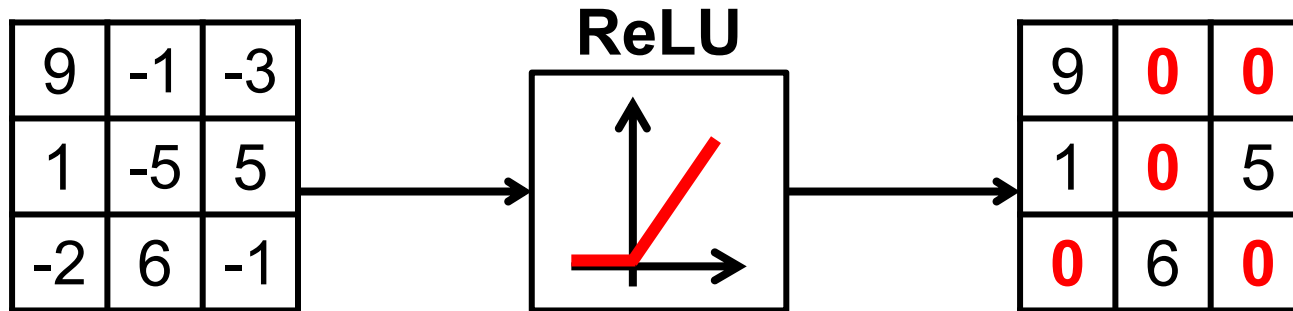
# Approaches

- **Reduce size of operands for storage/compute**
  - Floating point → Fixed point
  - Bit-width reduction
  - Non-linear quantization
- **Reduce number of operations for storage/compute**
  - Exploit Activation Statistics (Compression)
  - Network Pruning
  - Compact Network Architectures

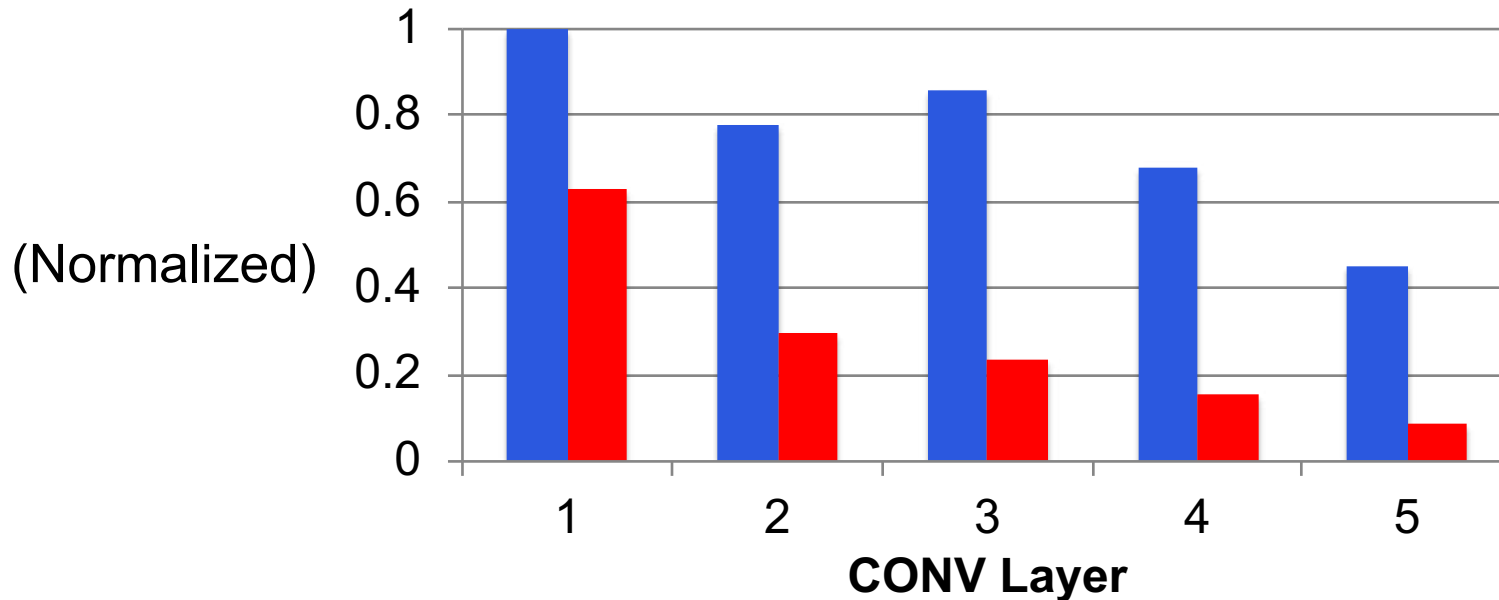
# Exploit Sparsity

# Sparsity in Feature Maps

Many **zeros** in output fmaps after ReLU

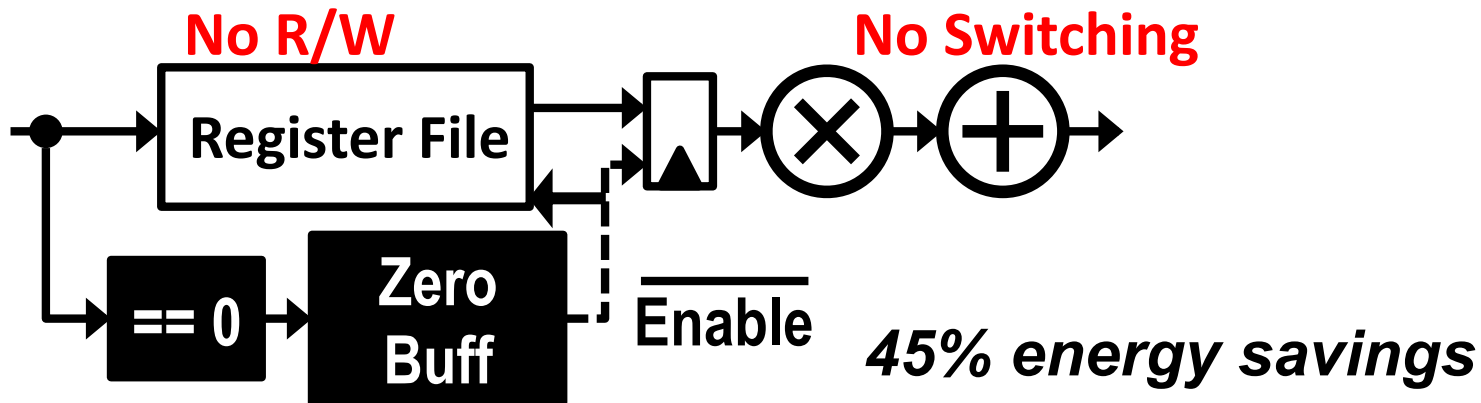


■ # of activations    ■ # of non-zero activations

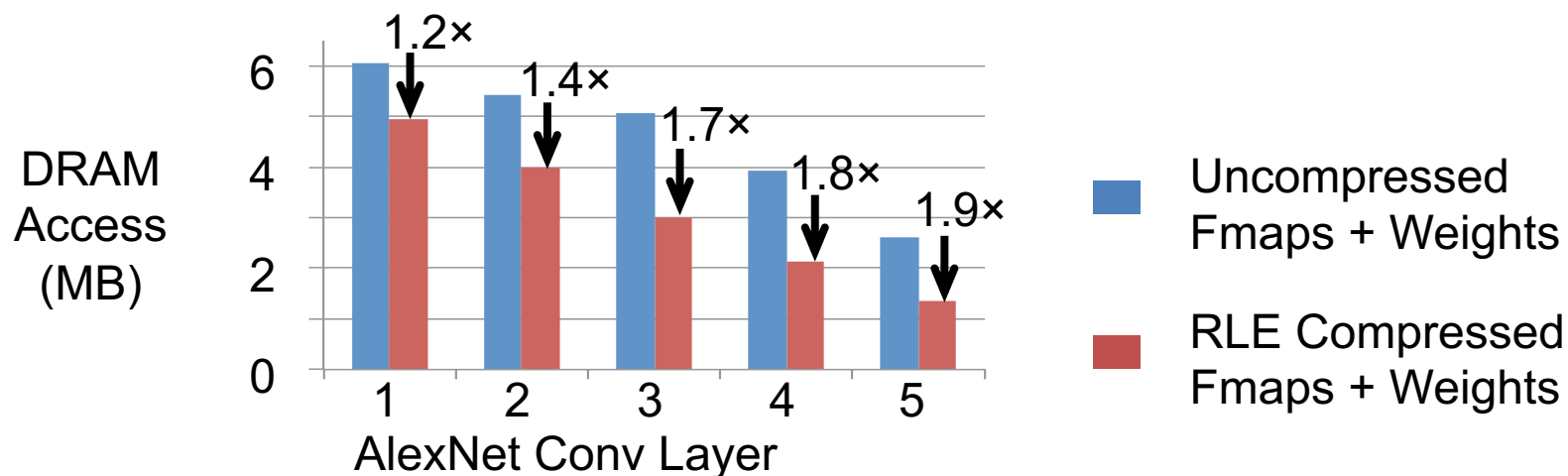


# Exploit Sparsity

Method 1: Skip memory access and computation



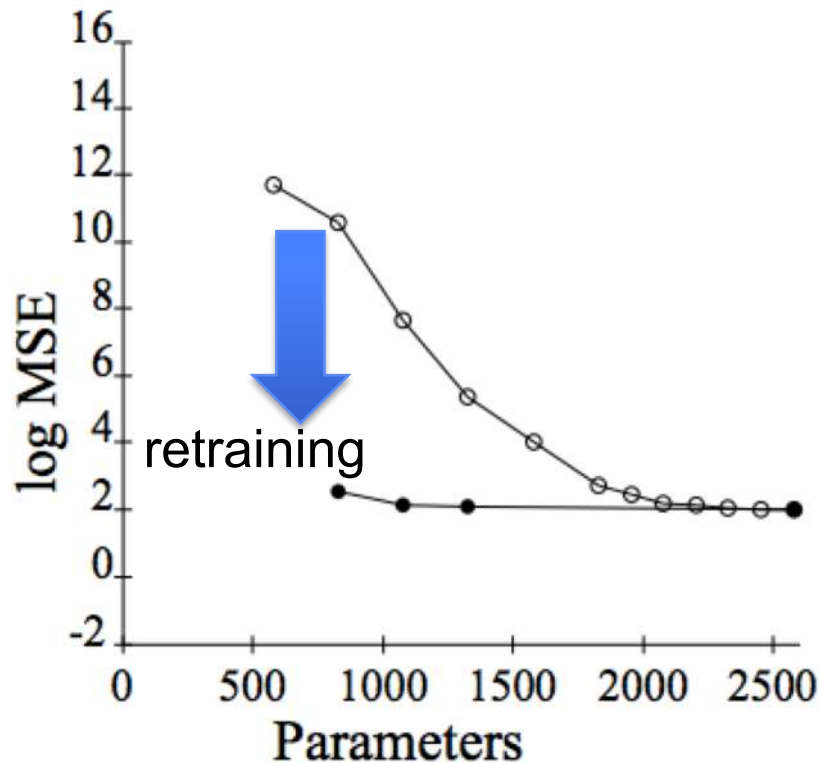
Method 2: Compress data to reduce storage and data movement



# Pruning – Make Weights Sparse

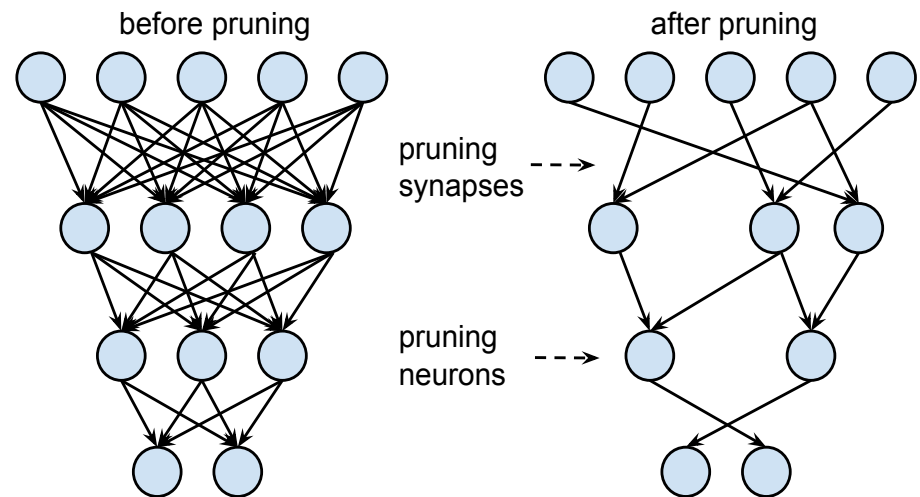
## Optimal Brain Damage

[Lecun et al., NeurIPS 1989]



Prune DNN based on  
***magnitude*** of weights

[Han et al., NeurIPS 2015]



**Example: AlexNet**

**Weight Reduction:**

CONV layers 2.7x, **FC layers 9.9x**

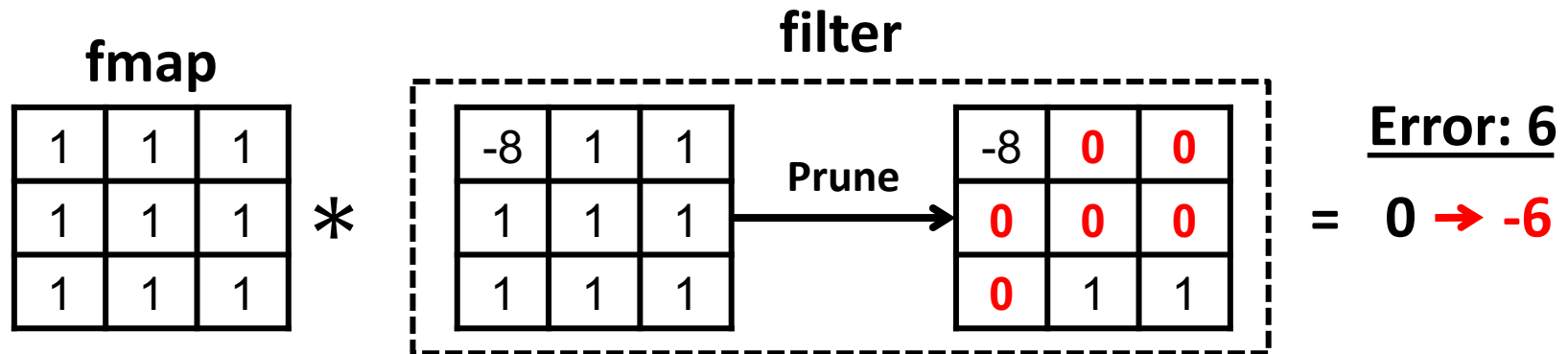
**Overall Reduction:**

Weights 9x, MACs 3x

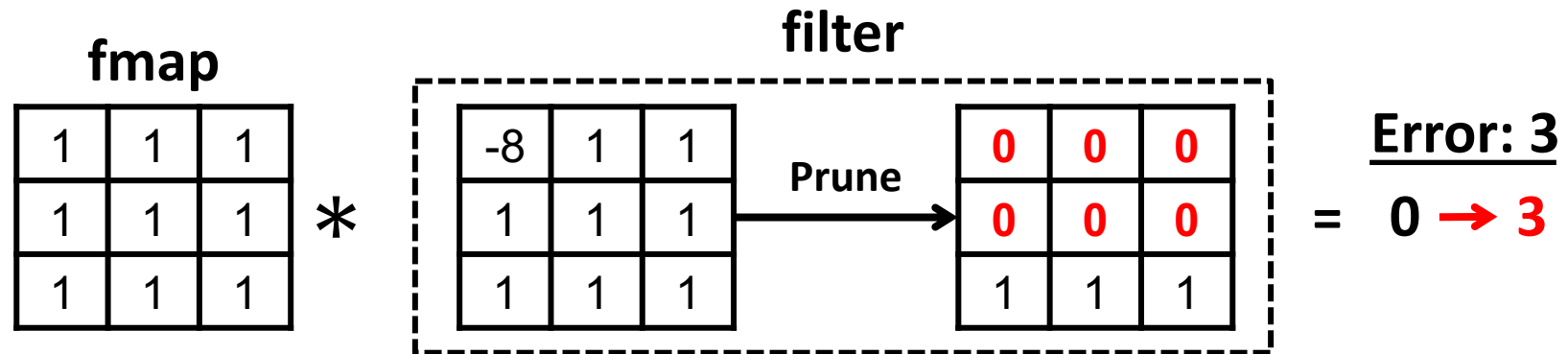
# Pruning – Make Weights Sparse

Remove the weights with the **smallest joint impact** on the output feature map instead of that with the **smallest magnitude**

## Magnitude-Based Method



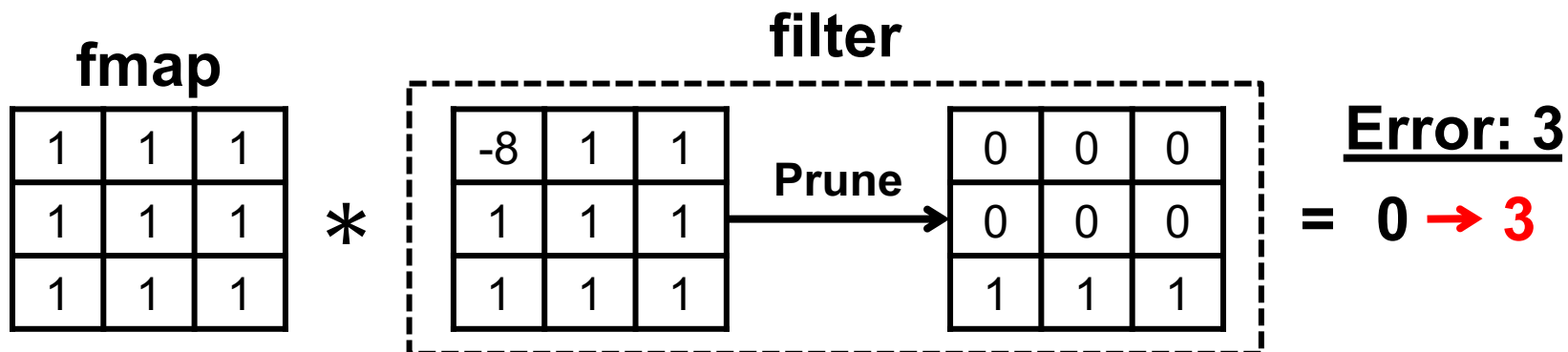
## Feature-Map-Based Method



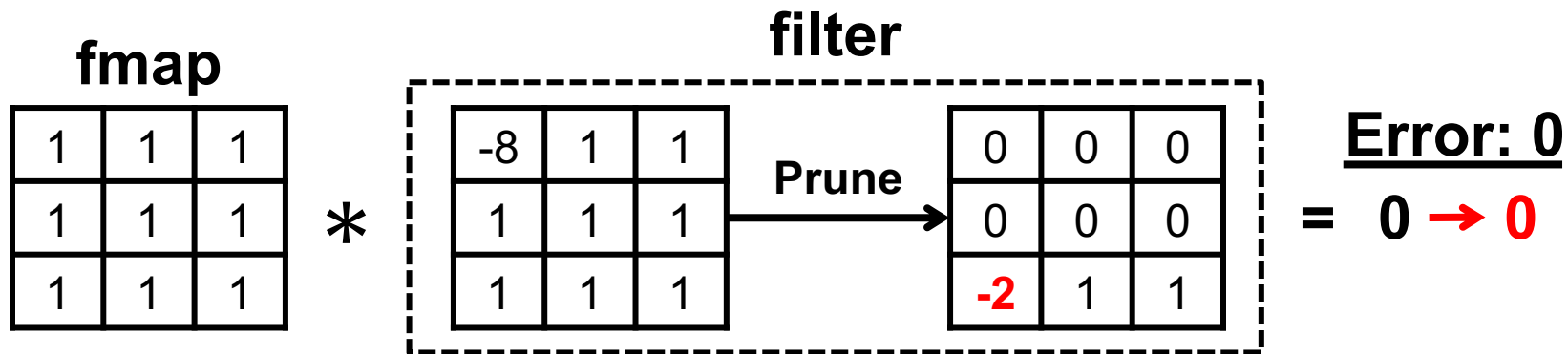
# Fast Local Fine-Tuning

We then **locally fine-tune** the remaining weights, which is much faster than performing end-to-end training

**After Pruning**



**After Local Fine-Tuning**





# Compression of Weights & Activations

- Compress weights and activations between DRAM and accelerator
- Variable Length / Huffman Coding

Example:

Value: **16'b0** → Compressed Code: {**1'b0**}

Value: **16'bx** → Compressed Code: {**1'b1**, **16'bx**}

- Tested on AlexNet → 2× overall BW Reduction

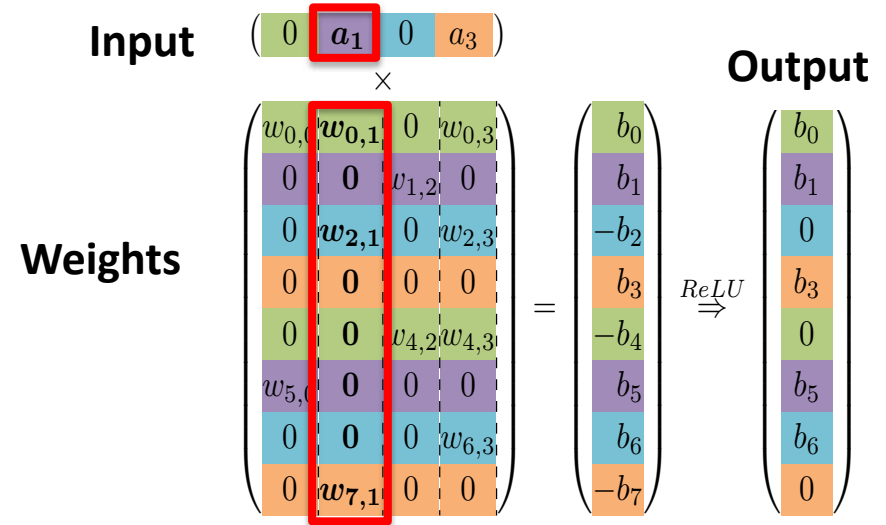
Layer	Filter / Image bits (0%)	Filter / Image BW Reduc.	IO / HuffIO (MB/frame)	Voltage (V)	MMACs/ Frame	Power (mW)	Real (TOPS/W)
General CNN	16 (0%) / 16 (0%)	1.0x		1.1	—	<b>288</b>	<b>0.3</b>
AlexNet l1	7 (21%) / 4 (29%)	1.17x / 1.3x	1 / 0.77	0.85	105	85	0.96
AlexNet l2	7 (19%) / 7 (89%)	1.15x / <b>5.8x</b>	3.2 / 1.1	0.9	224	55	1.4
AlexNet l3	8 (11%) / 9 (82%)	1.05x / 4.1x	6.5 / 2.8	0.92	150	77	0.7
AlexNet l4	9 (04%) / 8 (72%)	1.00x / 2.9x	5.4 / 3.2	0.92	112	95	0.56
AlexNet l5	9 (04%) / 8 (72%)	1.00x / 2.9x	3.7 / 2.1	0.92	75	95	0.56
Total / avg.	—	—	19.8 / <b>10</b>	—	—	<b>76</b>	<b>0.94</b>
LeNet-5 l1	3 (35%) / 1 (87%)	1.40x / 5.2x	0.005 / 0.001	0.7	0.3	25	1.07
LeNet-5 l2	4 (26%) / 6 (55%)	1.25x / 1.9x	0.050 / 0.042	0.8	1.6	35	1.75
Total / avg.	—	—	0.053 / <b>0.043</b>	—	—	<b>33</b>	<b>1.6</b>

# Sparse Hardware

## EIE

[Han et al., ISCA 2016]

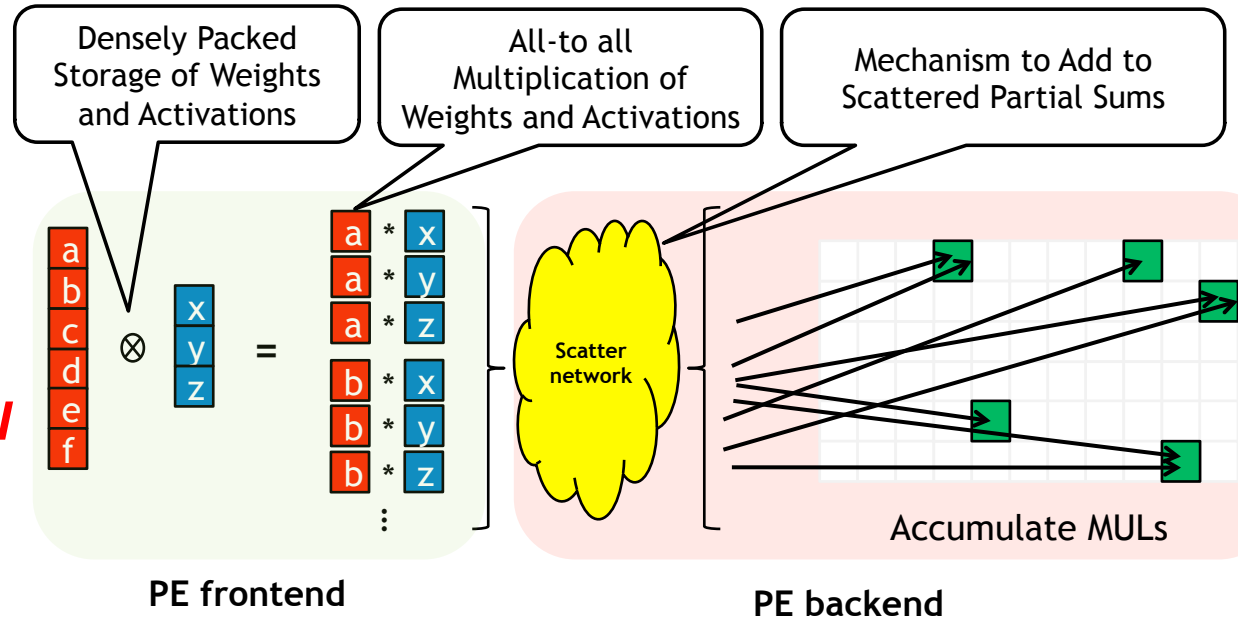
*Supports Fully  
Connected Layers Only*



## SCNN

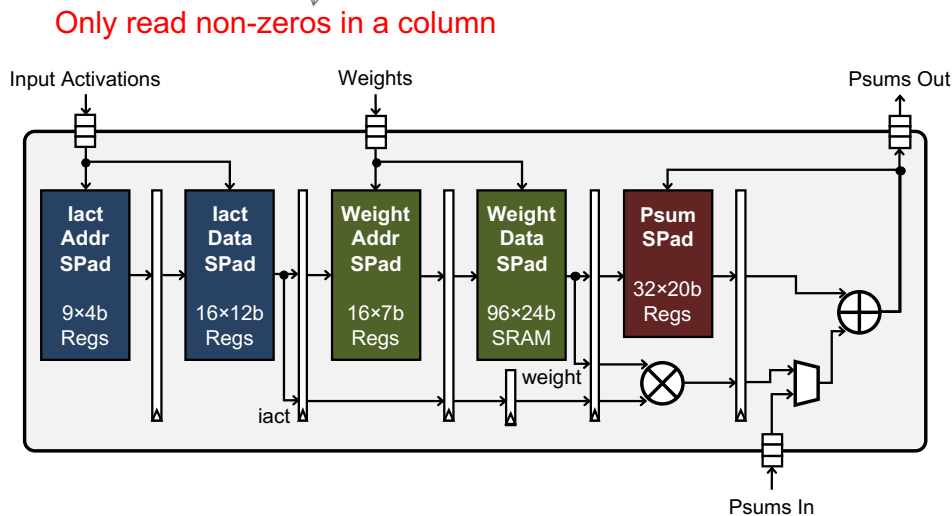
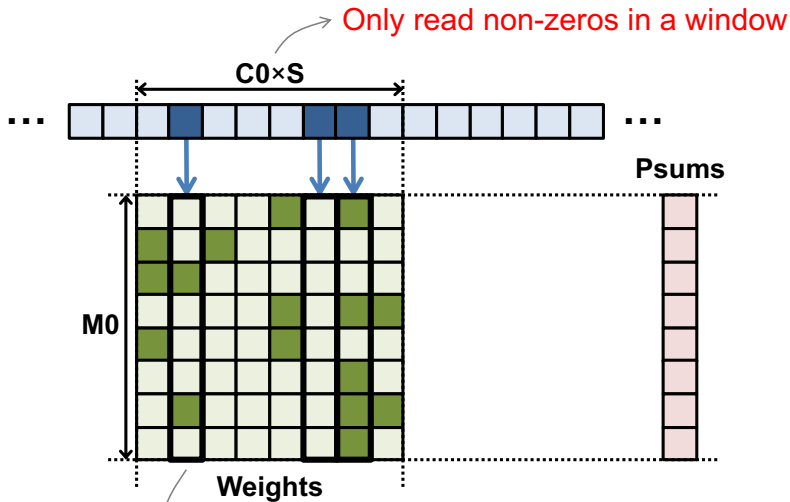
[Parashar et al.,  
ISCA 2017]

*Supports Convolutional  
Layers Only*



# Sparse Hardware – Eyeriss v2

*Supports both Convolutional and Fully Connected Layers*

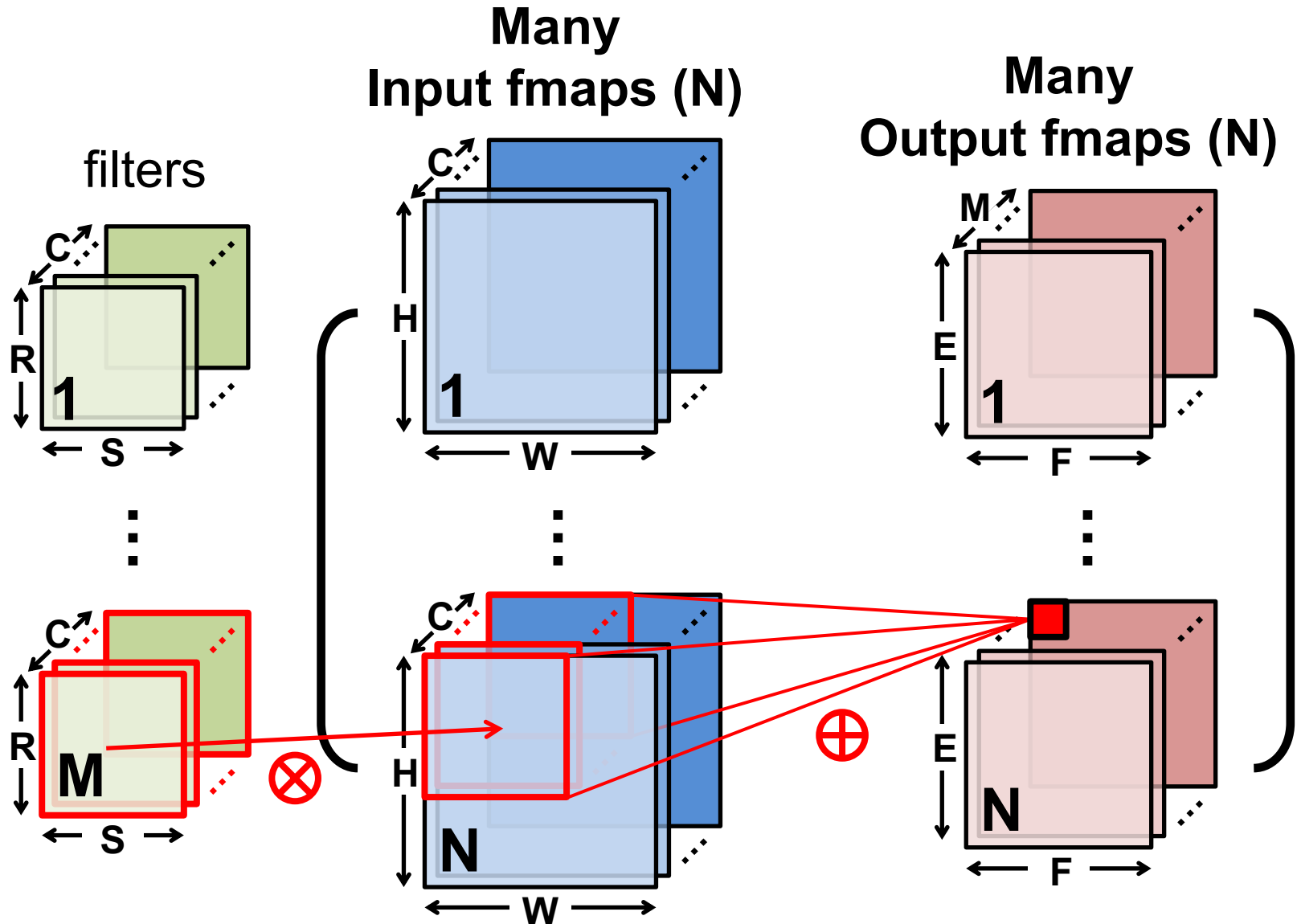


	AlexNet	sparse-AlexNet
<b>GOPS</b>	148.3	<b>405.8</b>
<b>fps</b>	102.4	280.1
<b>Over v1</b>	<b>15.5×</b>	<b>42.5×</b>
<b>GOPS/W</b>	277.9	<b>1028.1</b>
<b>Inferences/J</b>	191.8	709.7
<b>Over v1</b>	<b>3.0×</b>	<b>11.3×</b>

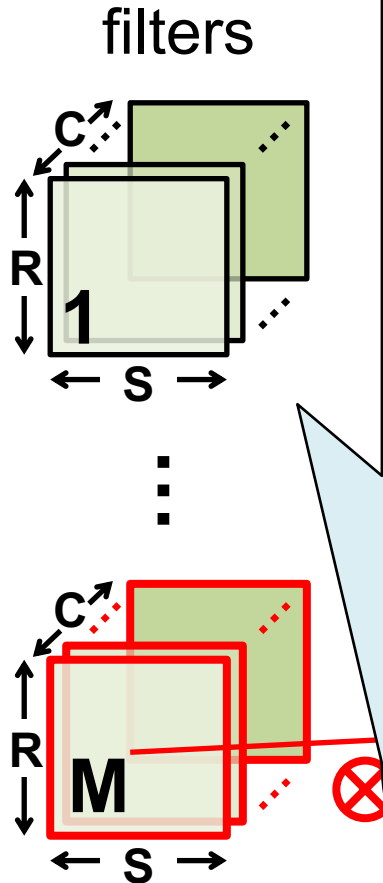
[Chen et al., JETCAS 2019]

# Manual Network Architecture Design

# Simplify CONV Layers



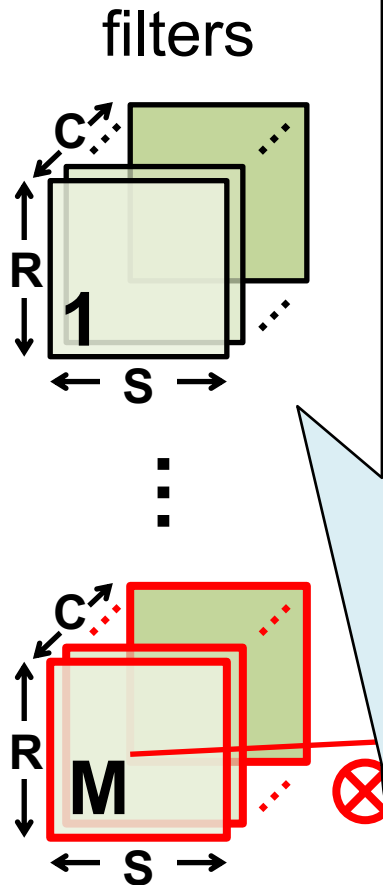
# Simplify CONV Layers



Methods can be roughly categorized by how the filters are simplified:

- Reduce spatial size ( $R, S$ ): stacked filters
- Reduce channels ( $C$ ): 1x1 convolution, group of filters
- Reduce filters ( $M$ ): feature map reuse

# Simplify CONV Layers



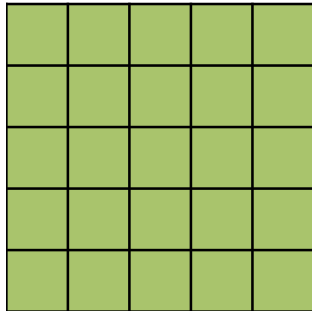
Methods can be roughly categorized by how the filters are simplified:

- Reduce spatial size ( $R, S$ ): stacked filters
- Reduce channels ( $C$ ): 1x1 convolution, group of filters
- Reduce filters ( $M$ ): feature map reuse

# Stacked Filters

## GoogLeNet/Inception v3

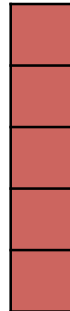
5x5 filter



decompose



5x1 filter

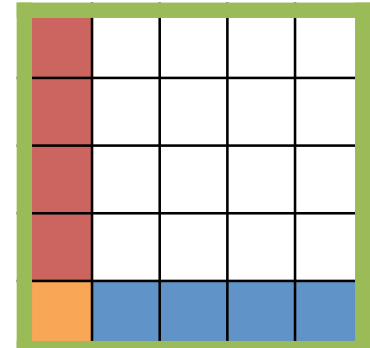


1x5 filter



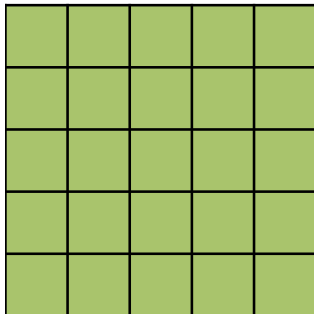
*separable  
filters*

Apply sequentially



## VGG-16

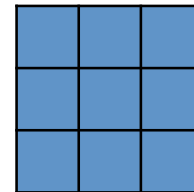
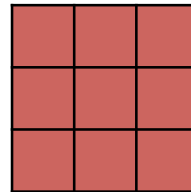
5x5 filter



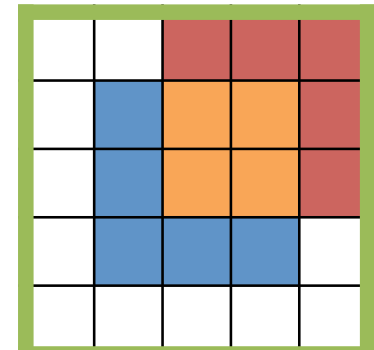
decompose



Two 3x3 filters



Apply sequentially



Replace a large filter with a series of smaller filters



# Stacked Filters

- Use stack of smaller filters (3x3) to cover the same receptive field with fewer filter weights

Example

5x5 filter

	0	1	2	3	2	
	1	2	2	2	0	
	0	1	0	1	3	
	1	2	2	1	0	
	0	1	0	3	1	

0	1	2	3	2
1	2	2	2	0
0	1	0	1	3
1	2	2	1	0
0	1	0	3	1

			31			

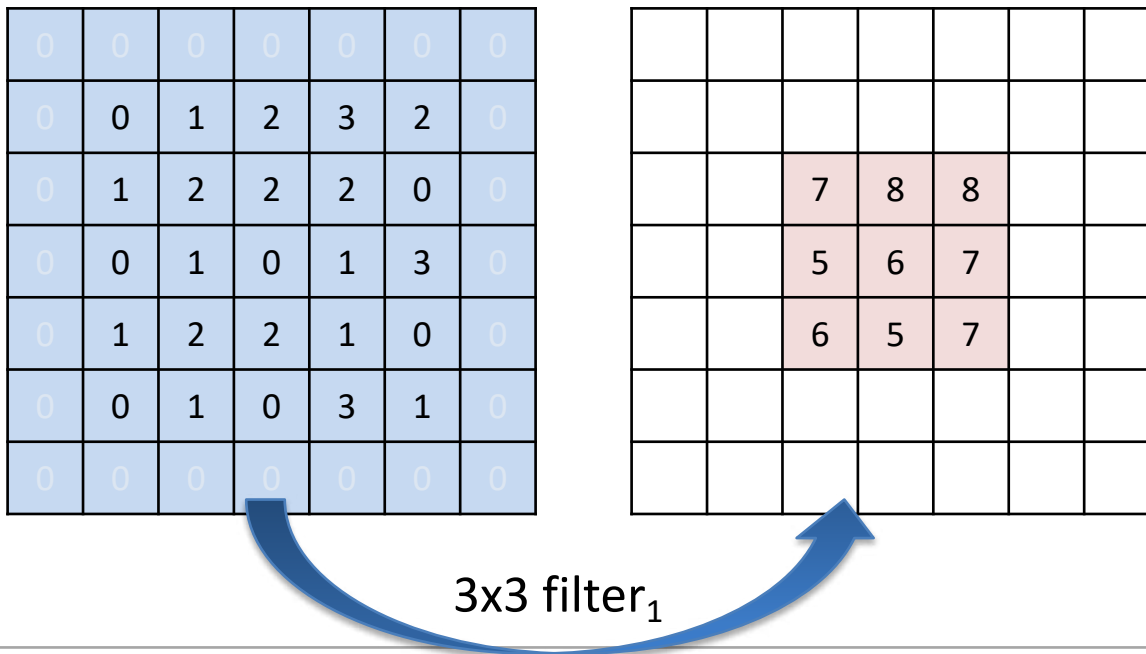
# Stacked Filters

- Use stack of smaller filters (3x3) to cover the same receptive field with fewer filter weights

filter (3x3)

0	1	0
1	1	1
0	1	0

Example



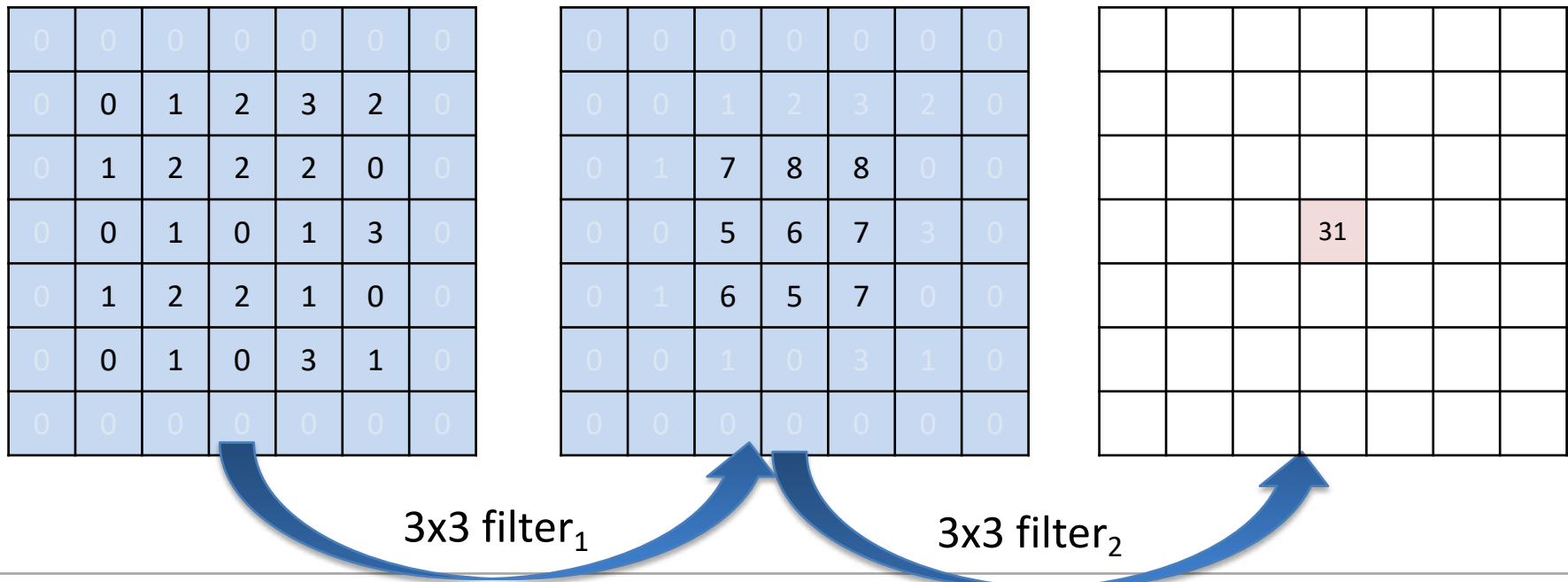
# Stacked Filters

- Use stack of smaller filters (3x3) to cover the same receptive field with fewer filter weights

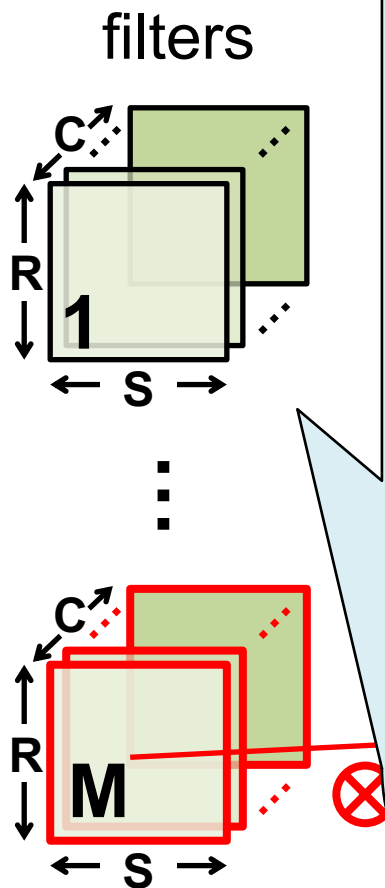
filter (3x3)

0	1	0
1	1	1
0	1	0

Example: 5x5 filter (25 weights) → two 3x3 filters (18 weights)



# Simplify CONV Layers

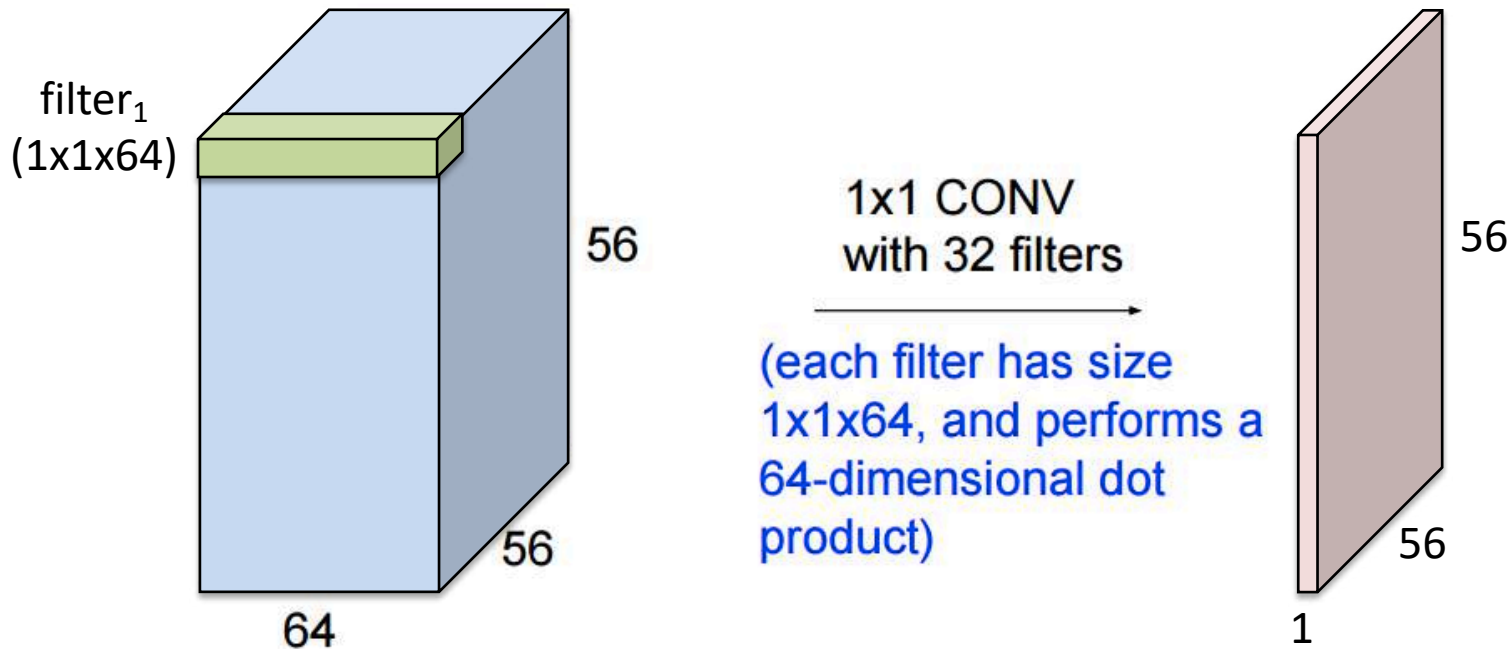


Methods can be roughly categorized by how the filters are simplified:

- Reduce spatial size ( $R, S$ ): stacked filters
- Reduce channels ( $C$ ): 1x1 convolution, group of filters
- Reduce filters ( $M$ ): feature map reuse

# 1x1 Convolution

Use **1x1 filter** to condense the cross-channel information.

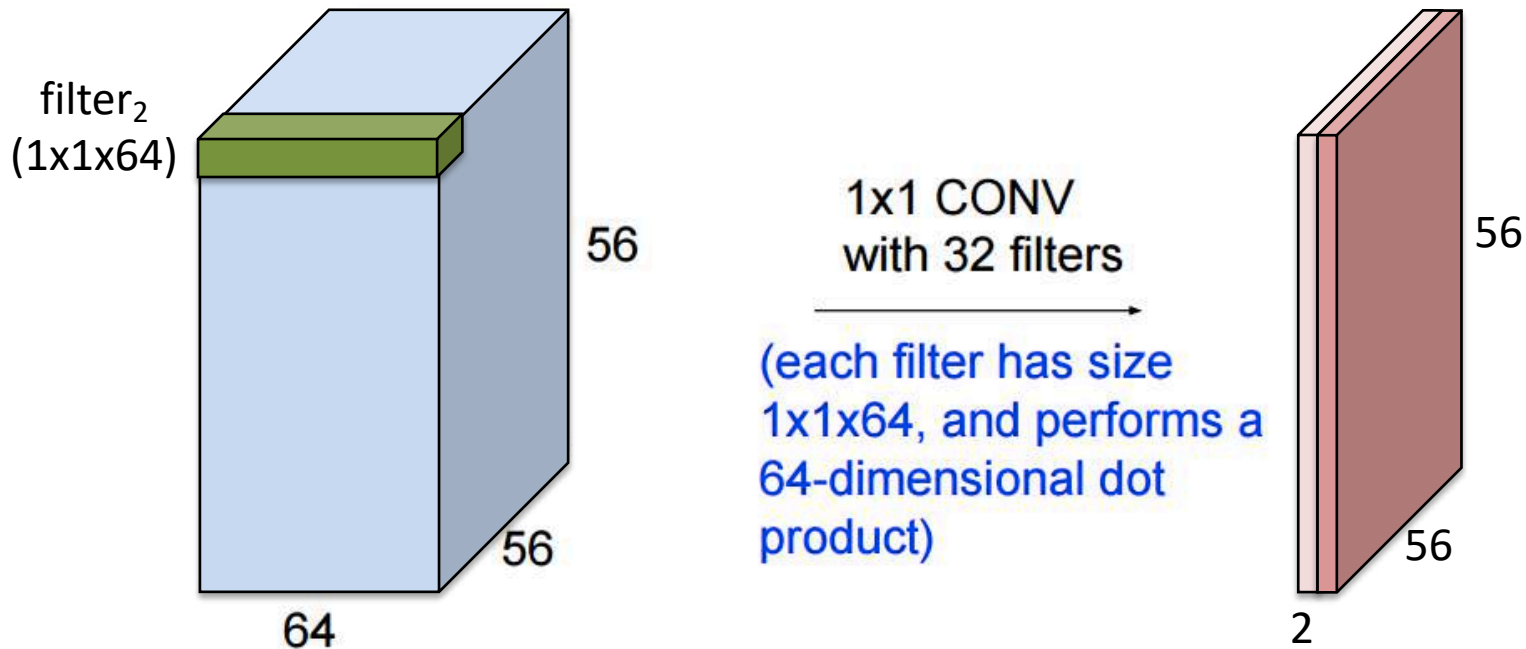


Modified image from source:  
Stanford cs231n

[Lin et al., Network in Network, arXiv 2013, ICLR 2014]

# 1x1 Convolution

Use **1x1 filter** to condense the cross-channel information.

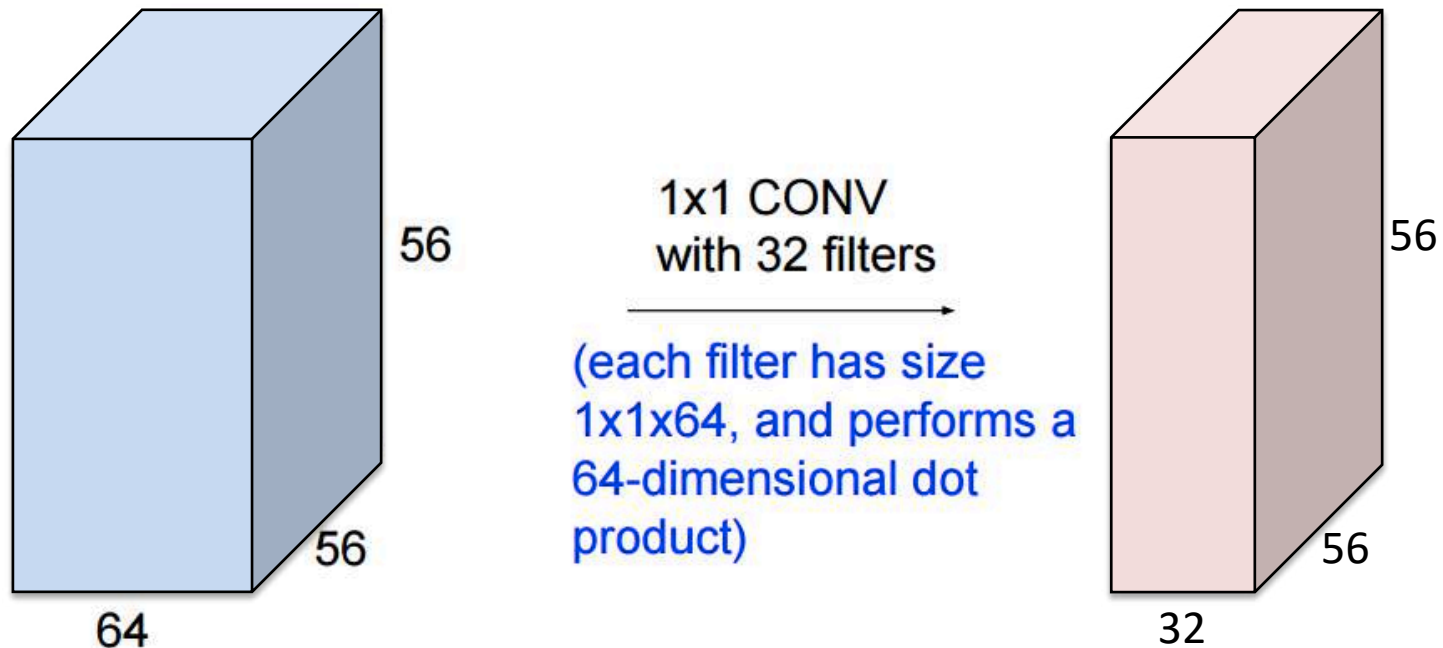


Modified image from source:  
Stanford cs231n

[Lin et al., Network in Network, arXiv 2013, ICLR 2014]

# 1x1 Convolution

Use **1x1 filter** to condense the cross-channel information.



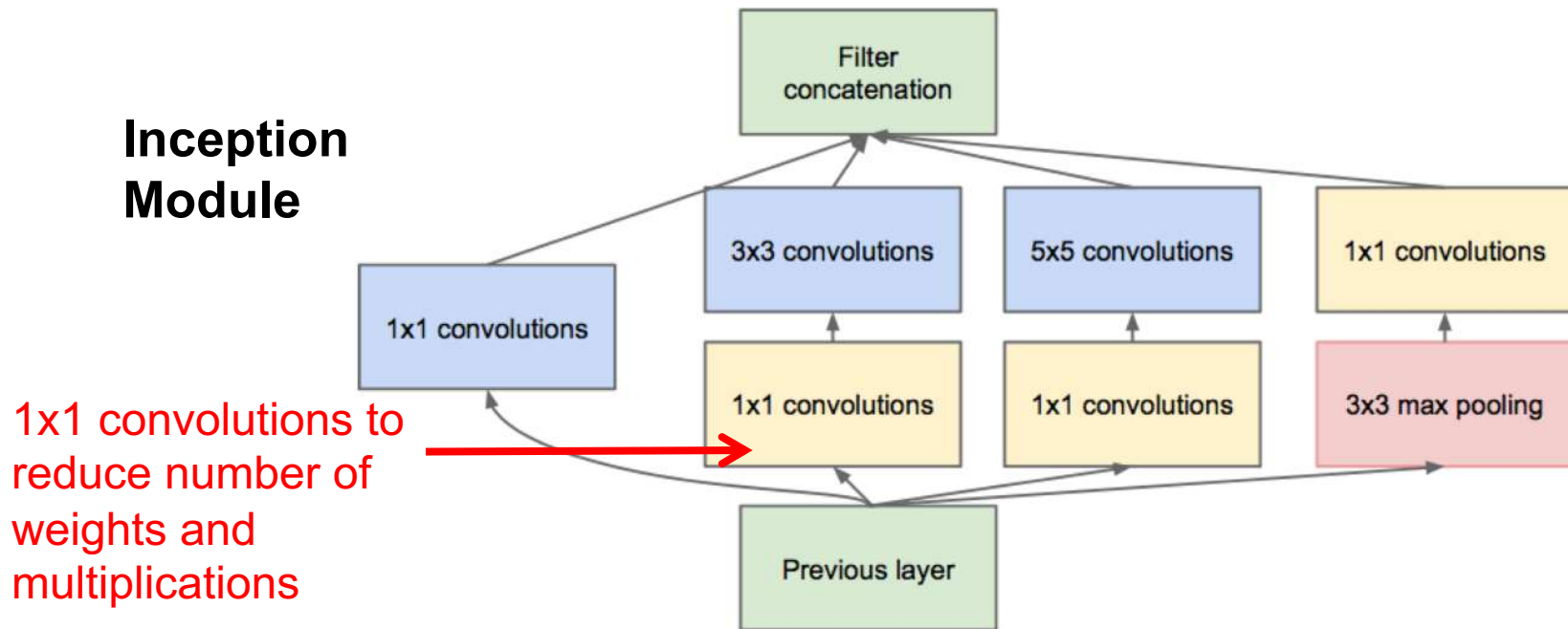
Modified image from source:  
Stanford cs231n

[Lin et al., Network in Network, arXiv 2013, ICLR 2014]

# GoogLeNet:1x1 Convolution

Apply 1x1 convolution before 'large' convolution filters.  
Reduce weights such that **entire CNN can be trained on one GPU**.  
Number of multiplications reduced from 854M  $\rightarrow$  358M

## Inception Module



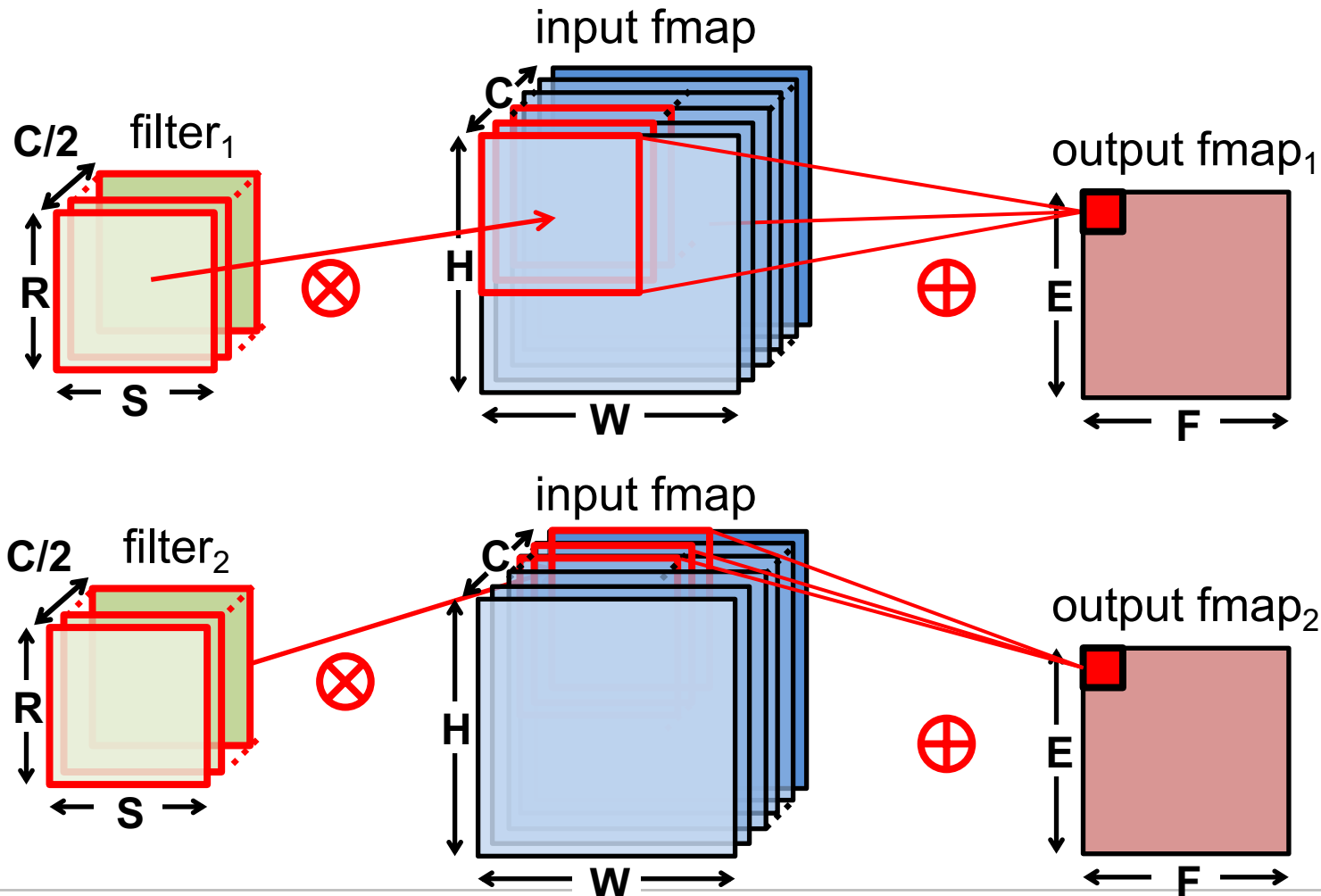
[Szegedy et al., arXiv 2014, CVPR 2015]



# Group of Filters

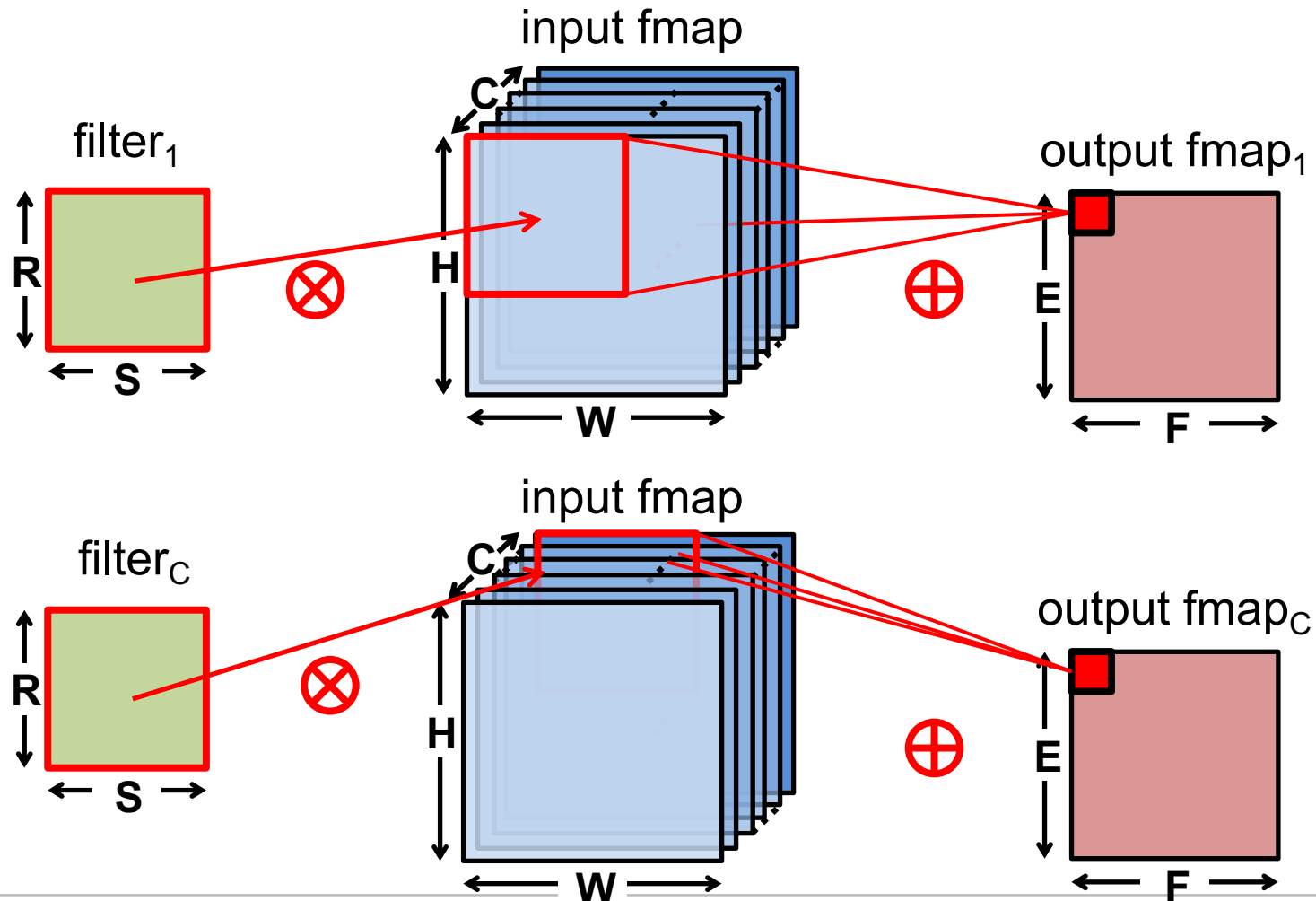
Idea: split filters and channels of feature map into different groups

Example: 2 groups, each filter requires **2x fewer weights and multiplications**.



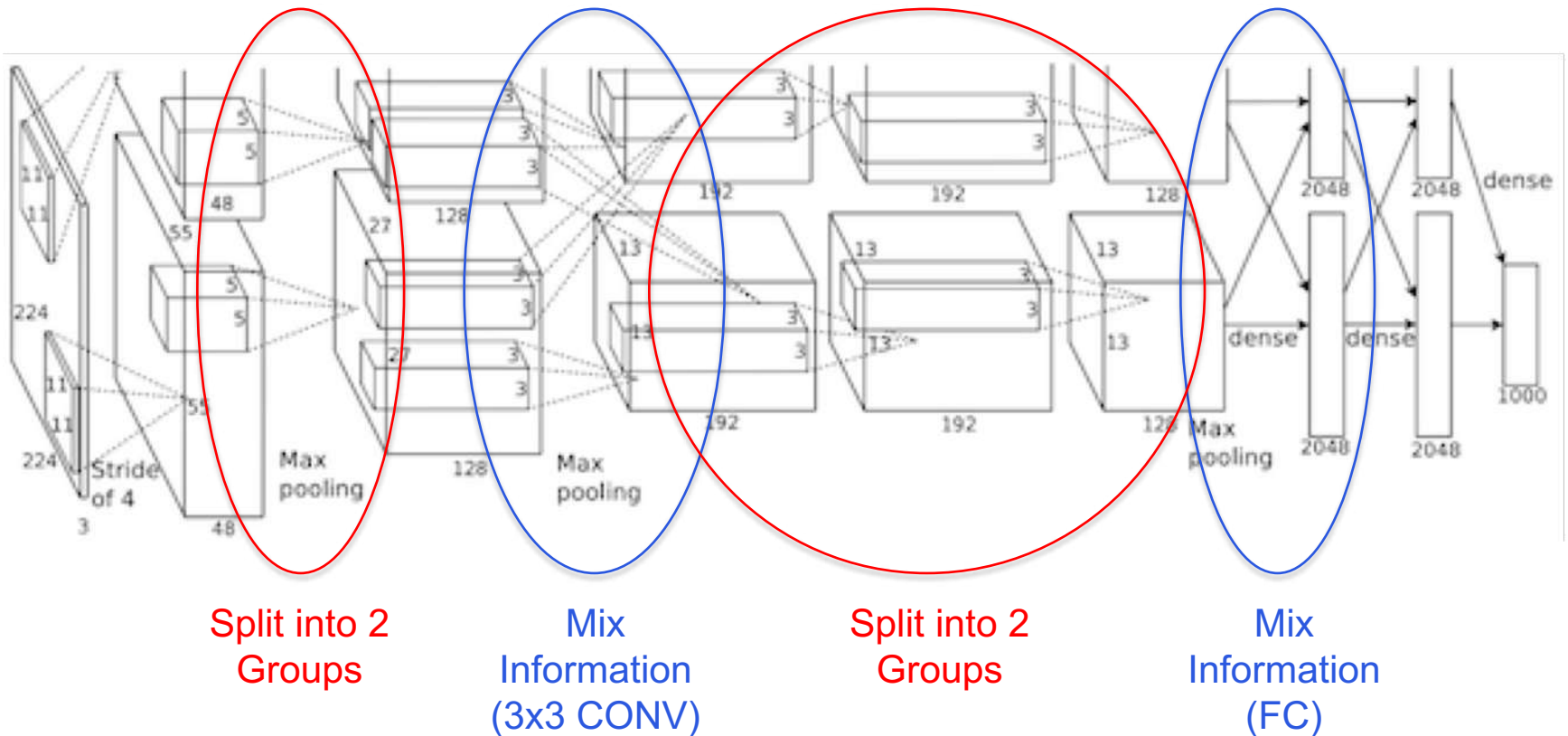
# Group of Filters

The extreme case is **depthwise convolution** – each group contains only one channel.



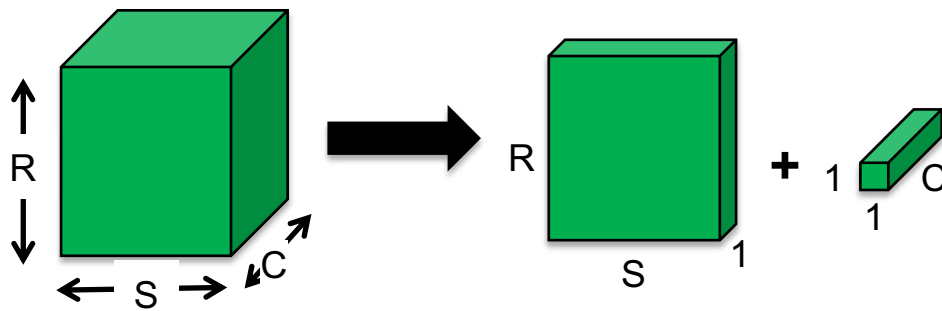
# Group of Filters

**AlexNet uses group of filters to train on two separate GPUs**  
 (Drawback: correlation between channels of different groups is not used)

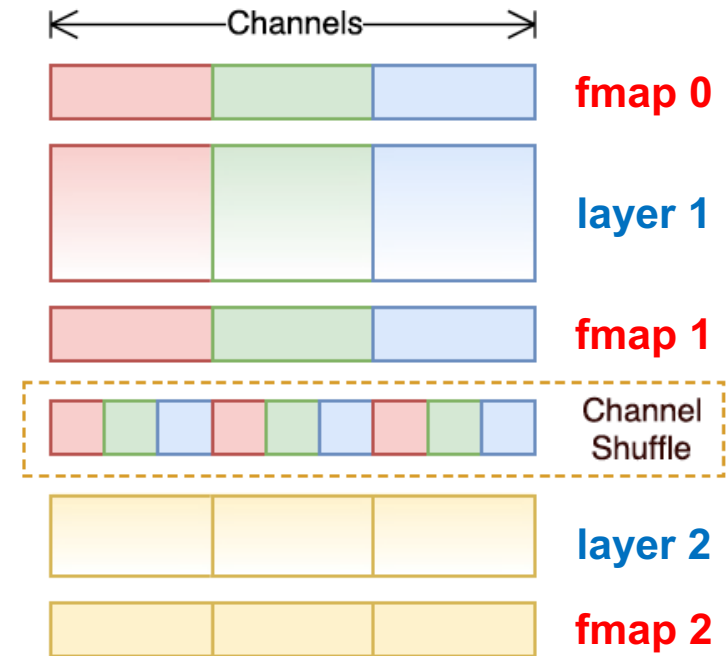


# Group of Filters

## Two ways of mixing information from groups



Pointwise (1x1) Convolution  
(Mix in one step)  
MobileNet



Shuffle Operation  
(Mix in multiple steps)  
ShuffleNet

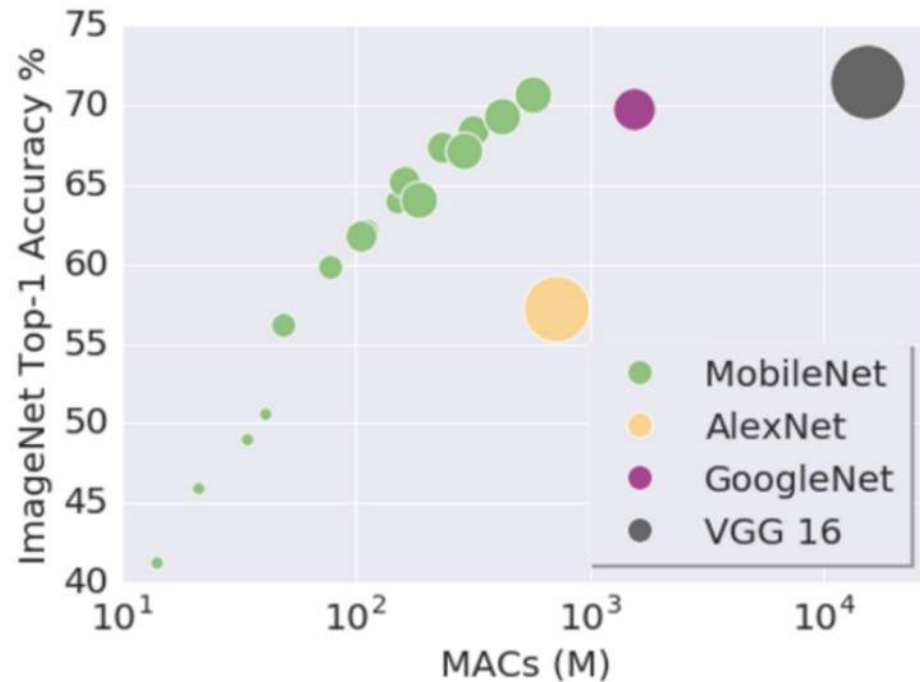
# MobileNets: Comparison

Table 8. MobileNet Comparison to Popular Models

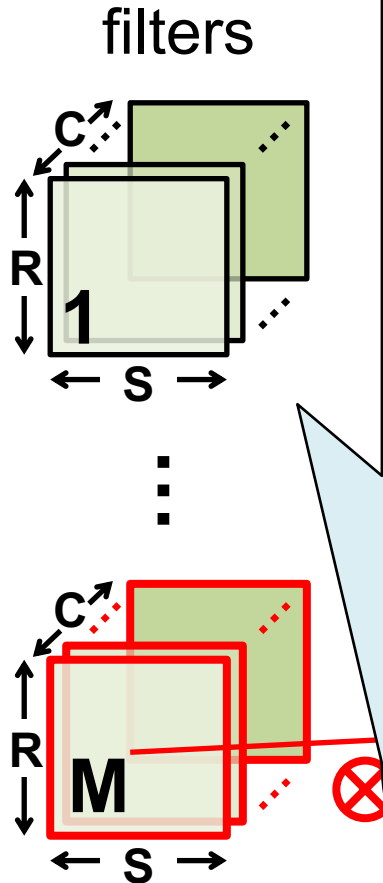
Model	ImageNet Accuracy	Million Mult-Adds	Million Parameter
1.0 MobileNet-224	70.6%	569	4.2
GoogleNet	69.8%	1550	6.8
VGG 16	71.5%	15300	138

Table 9. Smaller MobileNet Comparison to Popular Models

Model	ImageNet Accuracy	Million Mult-Adds	Million Parameter
0.50 MobileNet-160	60.2%	76	1.32
Squeezenet	57.5%	1700	1.25
AlexNet	57.2%	720	60



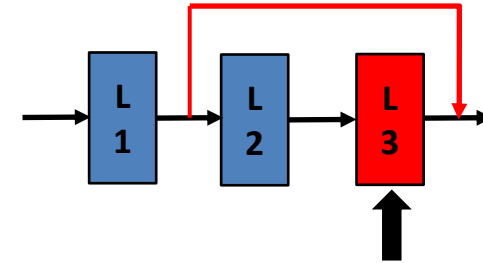
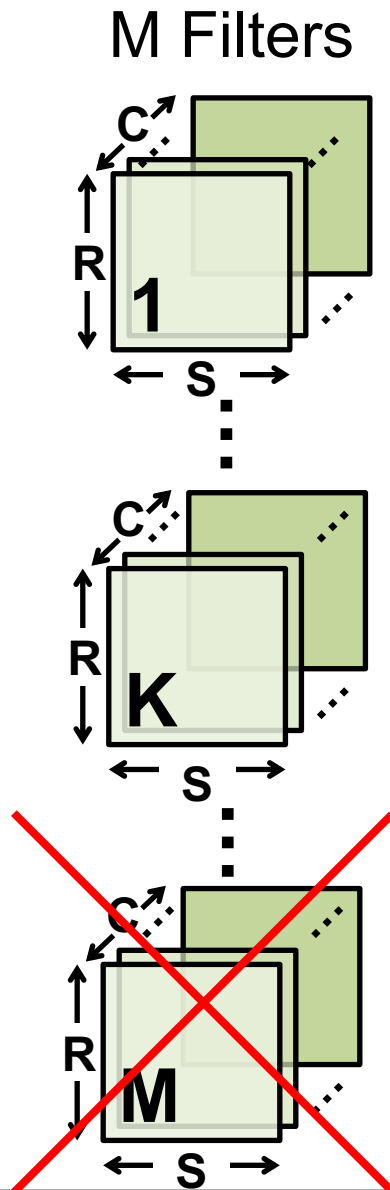
# Simplify CONV Layers



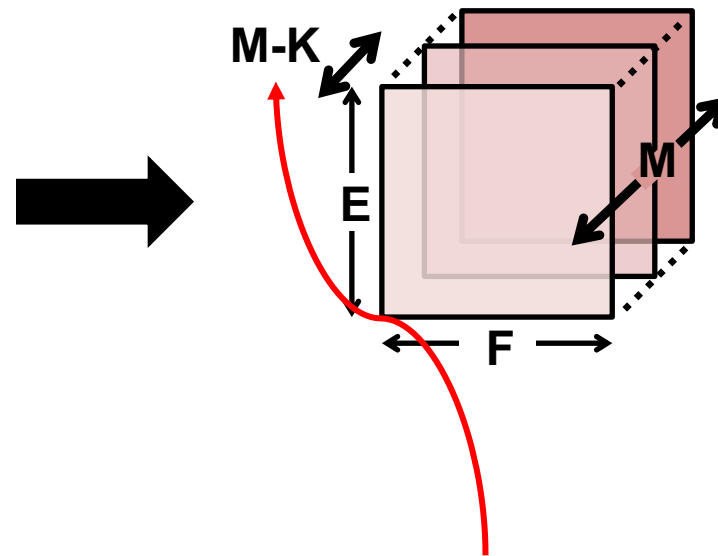
Methods can be roughly categorized by how the filters are simplified:

- Reduce spatial size ( $R, S$ ): stacked filters
- Reduce channels ( $C$ ): 1x1 convolution, group of filters
- Reduce filters ( $M$ ): feature map reuse

# Feature Map Reuse

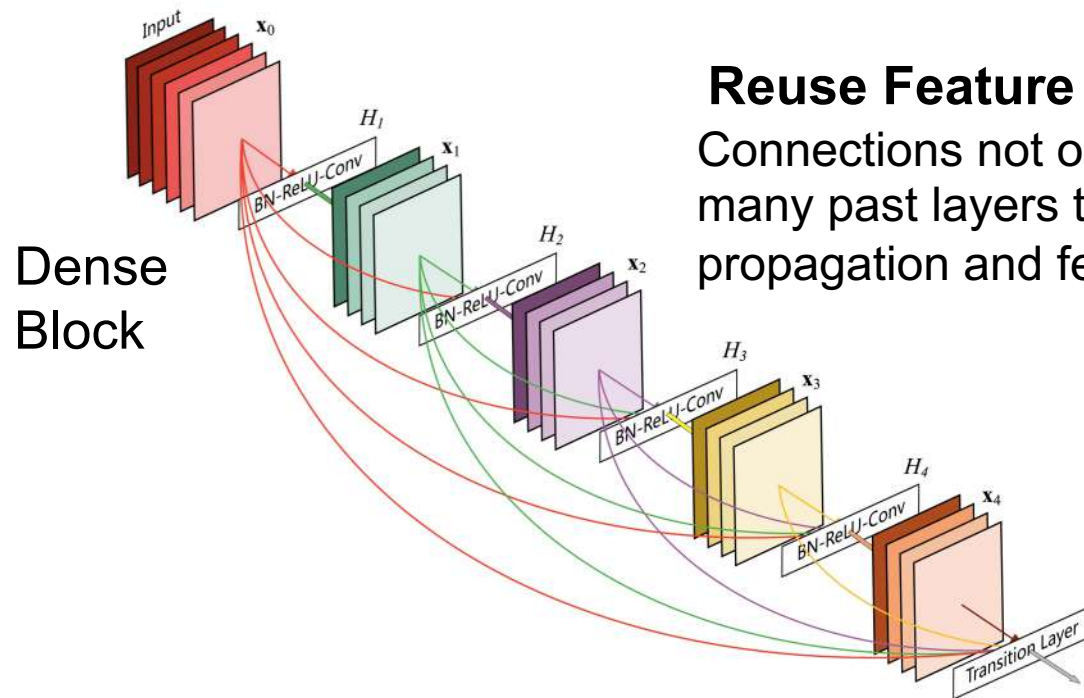


output fmap with M channels



Reuse (M-K) channels in feature maps from previously processed layers

# Feature Map Reuse

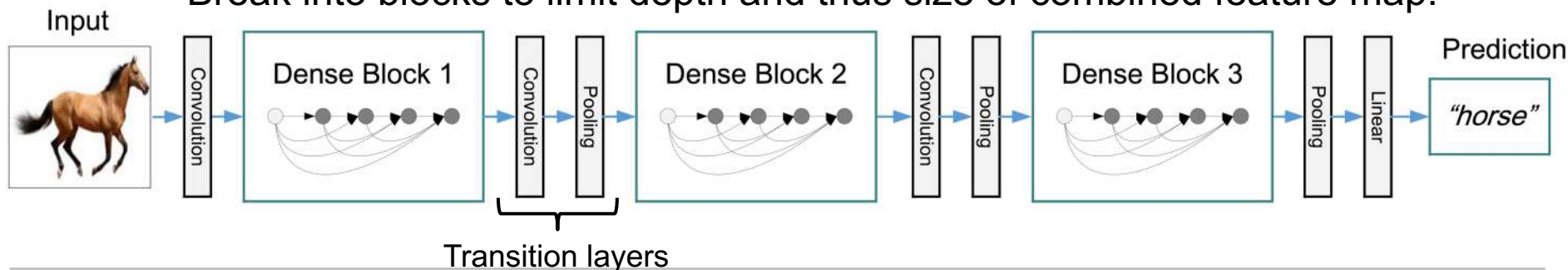


**Reuse Feature Maps from Multi. Layers!**

Connections not only from previous layer, but many past layers to strengthen feature map propagation and feature reuse.

Feature maps are concatenated rather than added.

Break into blocks to limit depth and thus size of combined feature map.

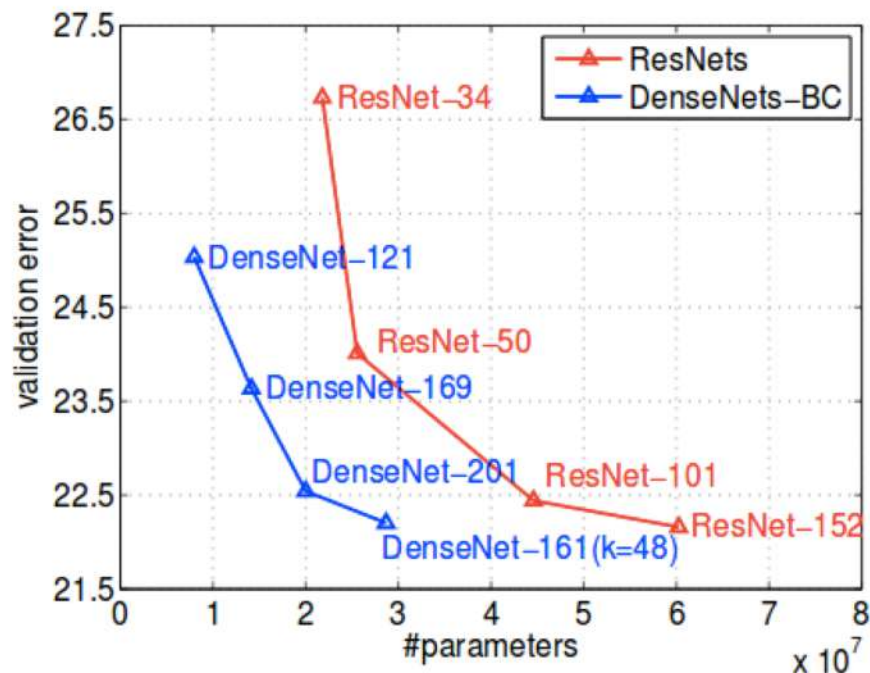




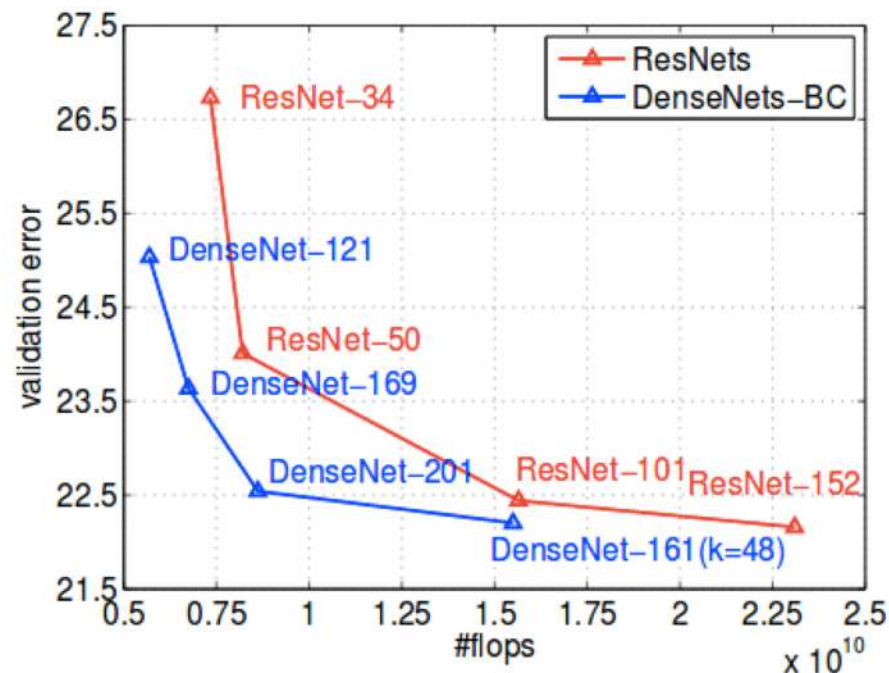
# DenseNet

Higher accuracy than ResNet with fewer weights and multiplications

Top-1 error



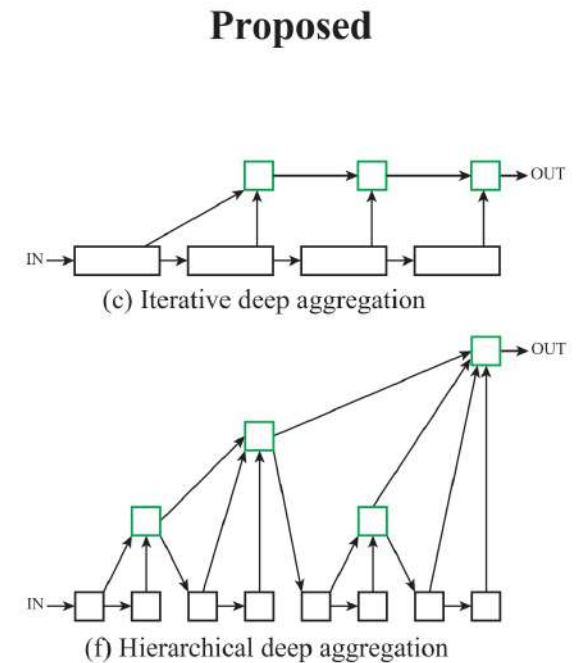
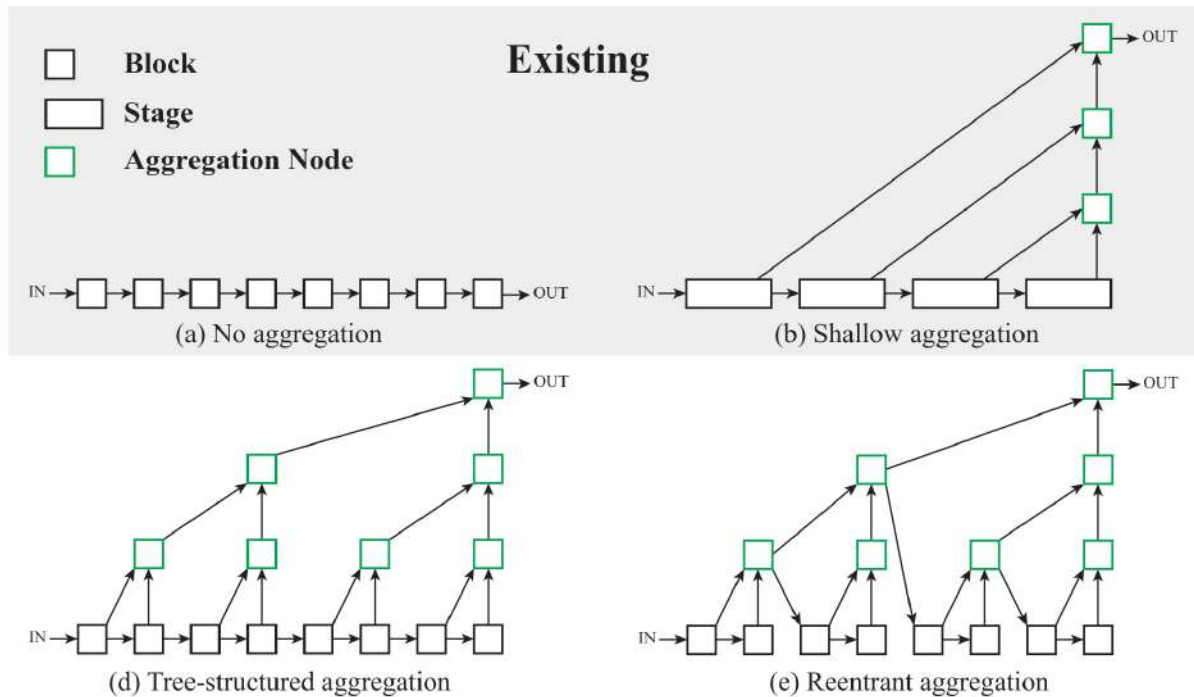
Top-1 error



Note: 1 MAC = 2 FLOPS

# Feature Map Reuse

- More complicated layer aggregation



# Simplify FC Layers

CONV Layers: 5

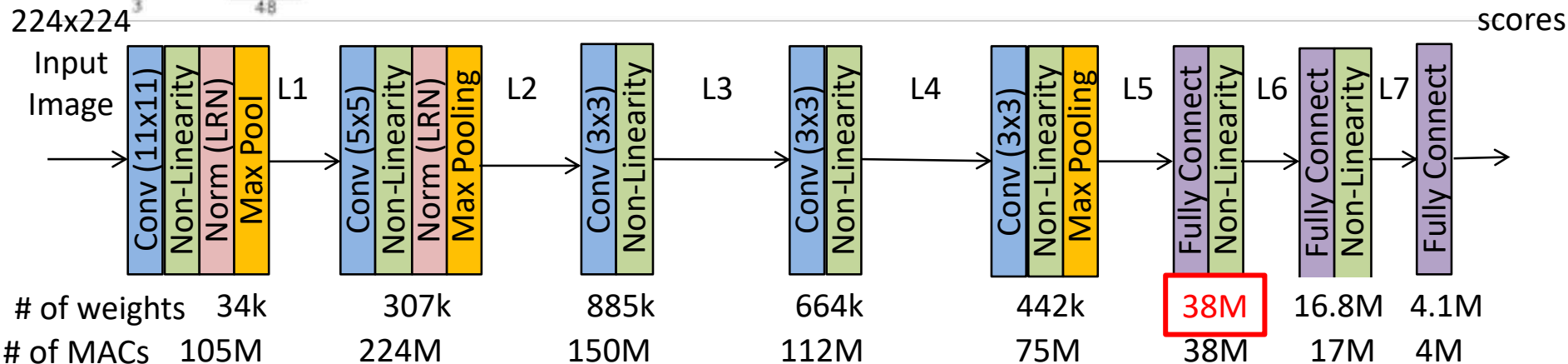
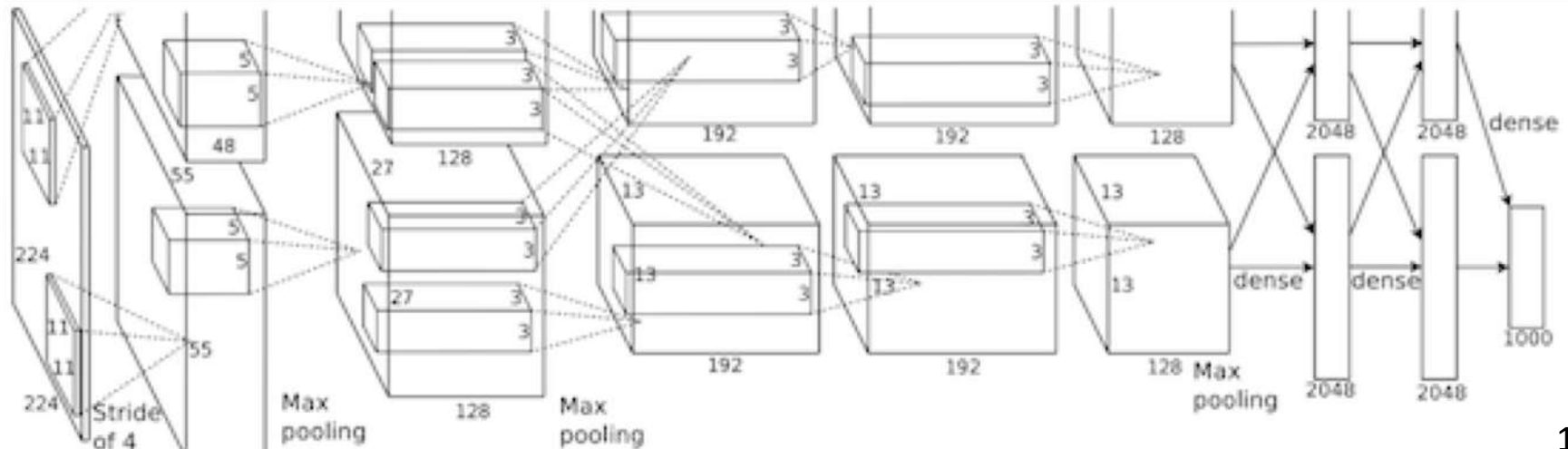
Fully Connected Layers: 3

Weights: 61M

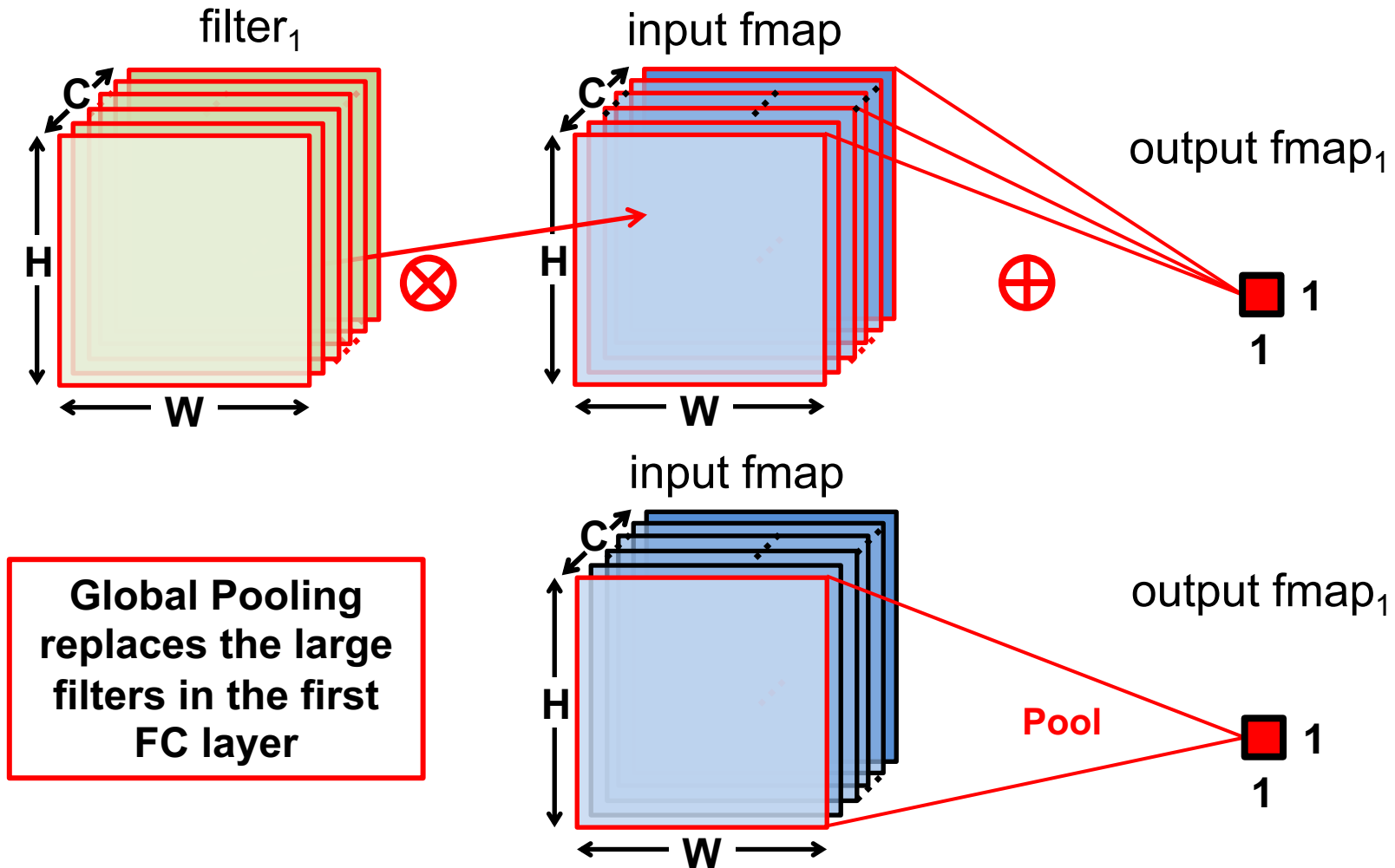
MACs: 724M

ILSCVR12 Winner

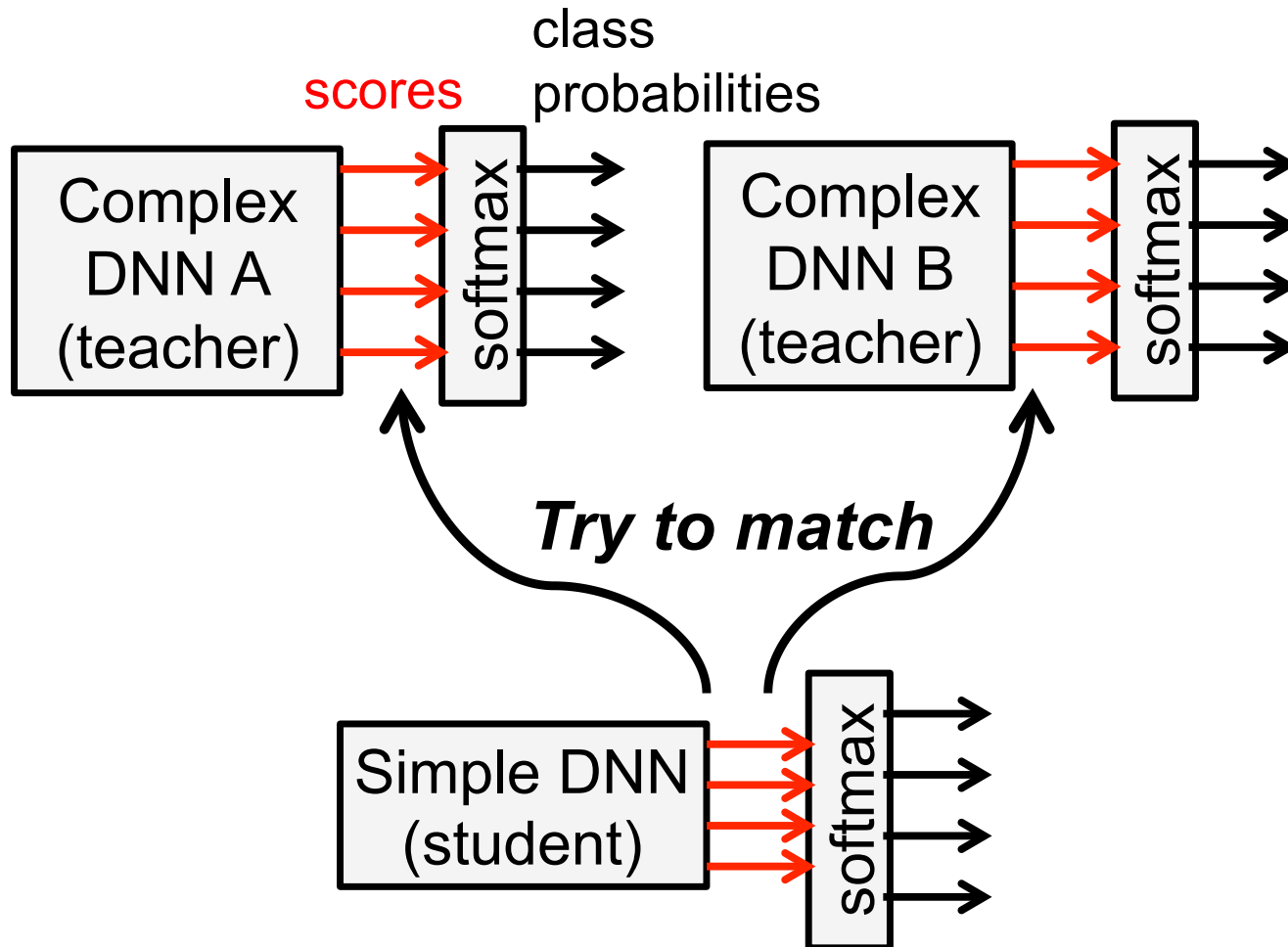
[Krizhevsky et al., NIPS 2012]



# Simplify FC Layers



# Knowledge Distillation

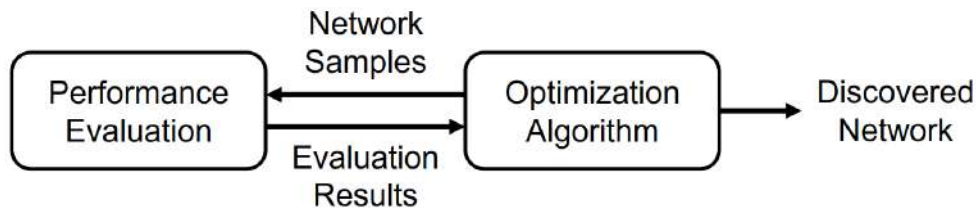


[Bucilu et al., KDD 2006],[Hinton et al., arXiv 2015]

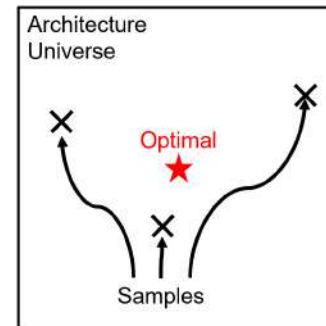
# Network Architecture Search (NAS)

# Learn Network Architecture

Rather than handcrafting the architecture, automatically search for it



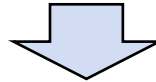
**Three main components:**  
(1) search space, (2) optimization algorithm,  
and (3) performance evaluation.



# Evaluate NAS Performance

- Key Metrics
  - Achievable DNN accuracy
  - Required search time

$$time_{nas} = num_{samples} \times time_{per\_sample}$$



$$time_{nas} \propto \left( \frac{num_{nas\_tuning} \times size_{search\_space}}{efficiency_{alg}} \right) \times (time_{train} + time_{eval})$$

(2) Improve the optimization algorithm

(1) Shrink the search space

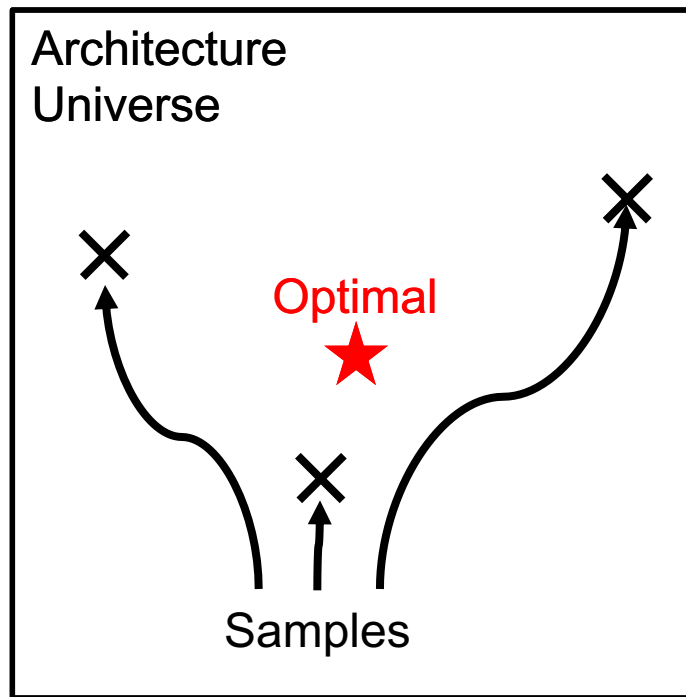
(3) Simplify the performance evaluation

Researchers improve the efficiency of NAS in 3 main components



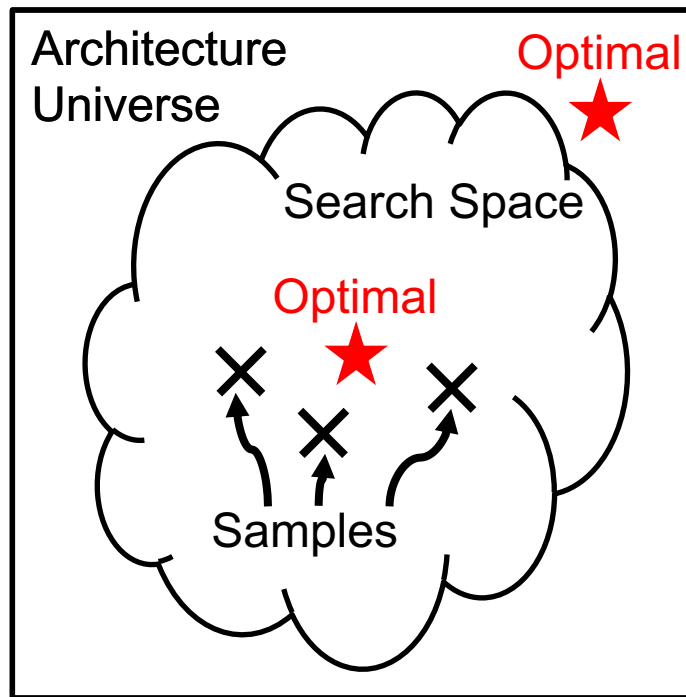
# (1) Shrink the Search Space

- Trade the discoverable architectures for search speed



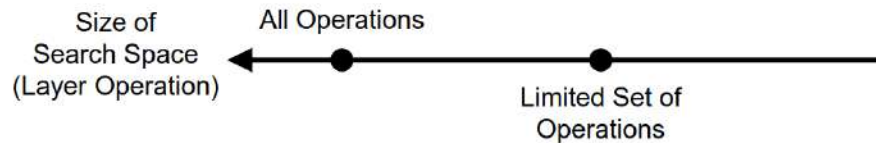
# (1) Shrink the Search Space

- Trade the discoverable architectures for search speed
- May irrecoverably limit the achievable network performance
  - Domain knowledge learned in manual network design provides guidance



# (1) Shrink the Search Space

- Search space = layer operations + connections between layers

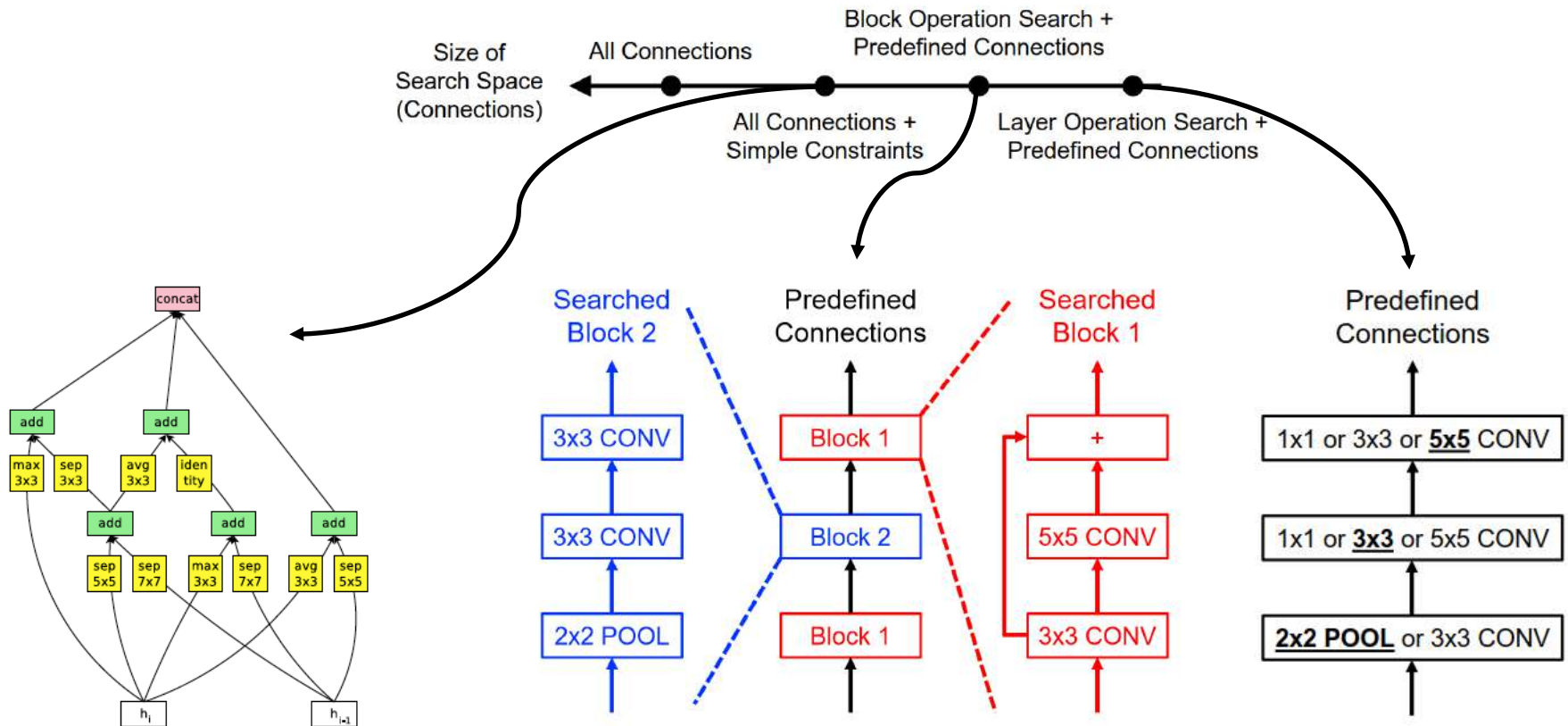


## Common layer operations:

- Identity
- 1x3 then 3x1 convolution
- 1x7 then 7x1 convolution
- 3x3 dilated convolution
- 1x1 convolution
- 3x3 convolution
- 3x3 separable convolution
- 5x5 separable convolution
- 3x3 average pooling
- 3x3 max pooling
- 5x5 max pooling
- 7x7 max pooling

# (1) Shrink the Search Space

- Search space = layer operations + connections between layers

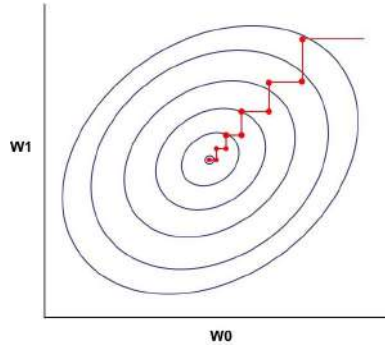


# (2) Improve Optimization Algorithm

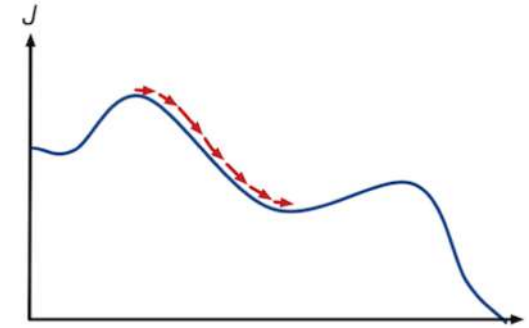
Random



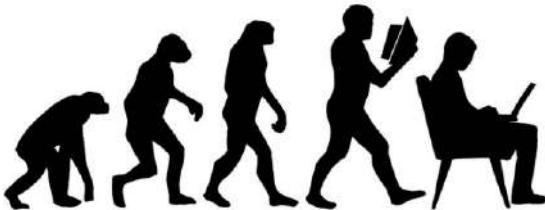
Coordinate Descent



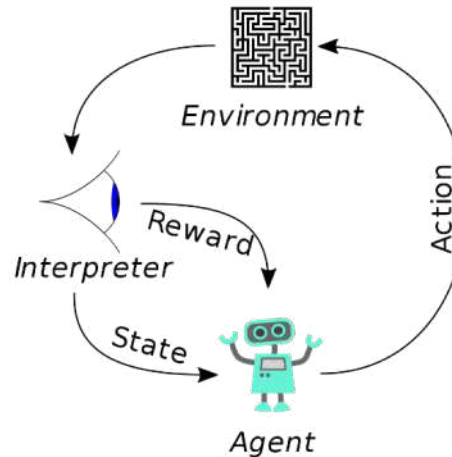
Gradient Descent



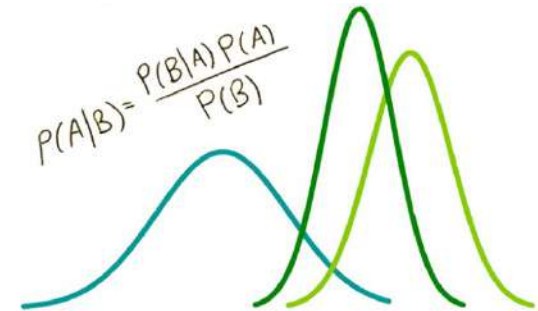
Evolutionary



Reinforcement Learning



Bayesian



## (2) Improve Optimization Algorithm

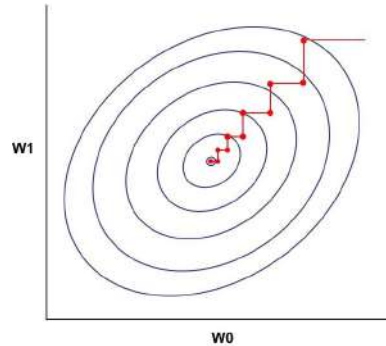
### Random



Randomly samples the entire space

- Simple
- Does not use previous results

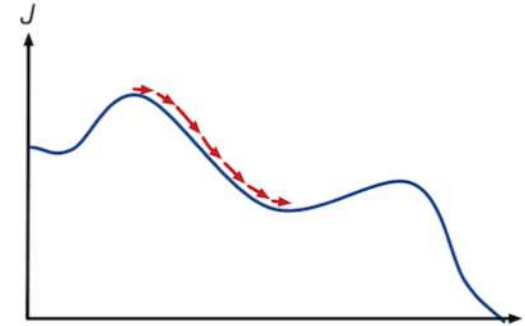
### Coordinate Descent



Starts from the previous best sample and greedily finds the best direction to move

- Uses previous results
- Simple
- Limited number of directions

### Gradient Descent



Starts from the previous best sample and goes in the direction that has the largest gradient

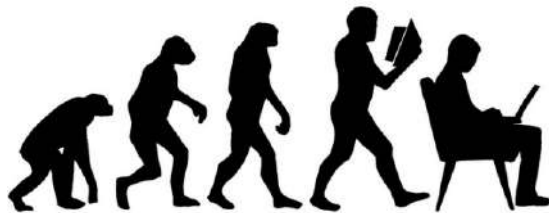
- Explores more directions
- The metric should be differentiable

## (2) Improve Optimization Algorithm

Starts from the previous best sample and goes in the best randomly-sampled direction

- The metric does not need to be differentiable
- More complicated

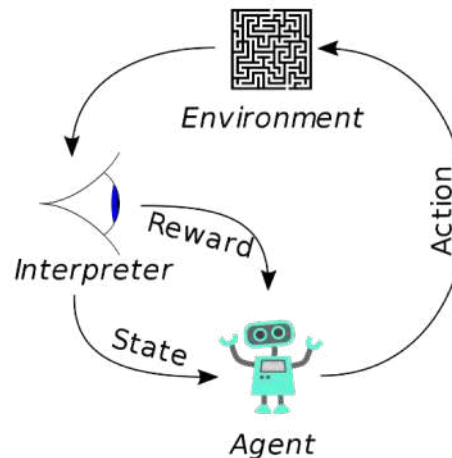
### Evolutionary



Learns from the previous samples and infers the best sample

- Better uses the previous samples
- Needs to design and train the agent

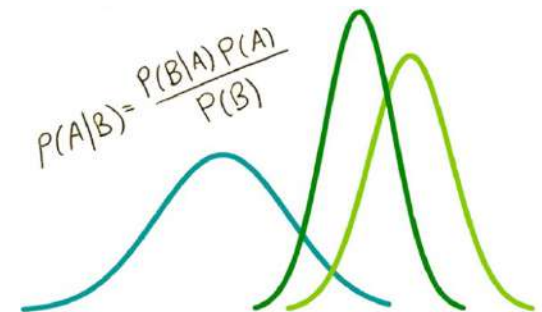
### Reinforcement Learning



Models the entire surface of the search space and picks the best sample

- Gets rid of the iterative process
- Hard to model a large search space

### Bayesian



## (3) Simplify the Performance Evaluation

- NAS needs only the rank of the performance values
- Method 1: approximate accuracy
- Method 2: approximate weights
- Method 3: approximate metrics (e.g., latency, energy)



# (3) Simplify the Performance Evaluation

- NAS needs only the rank of the performance values
- Method 1: approximate accuracy

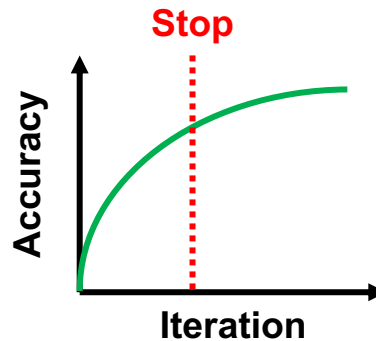
## Proxy Task

E.g., Smaller resolution,  
simpler tasks



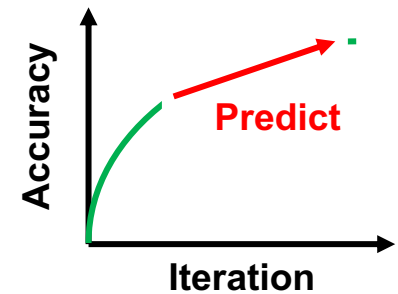
## Early Termination

Stop training earlier



## Accuracy Prediction

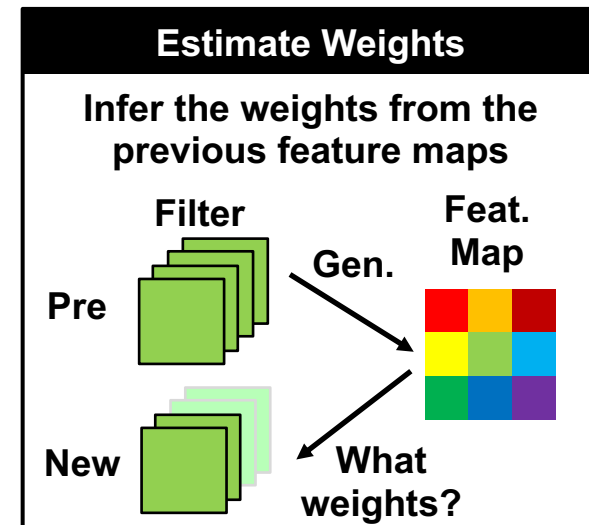
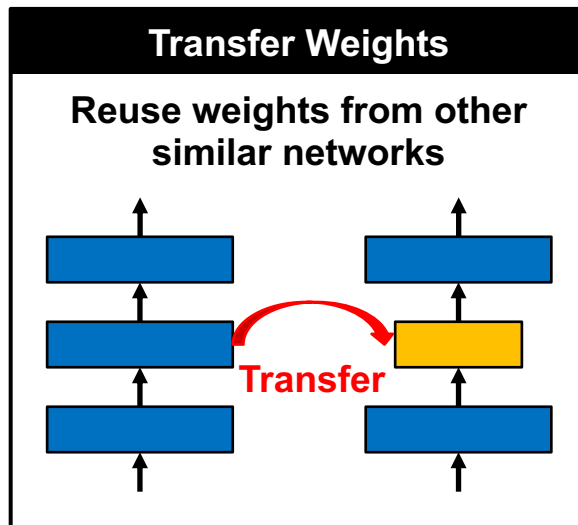
Extrapolate accuracy



- Method 2: approximate weights
- Method 3: approximate metrics

# (3) Simplify the Performance Evaluation

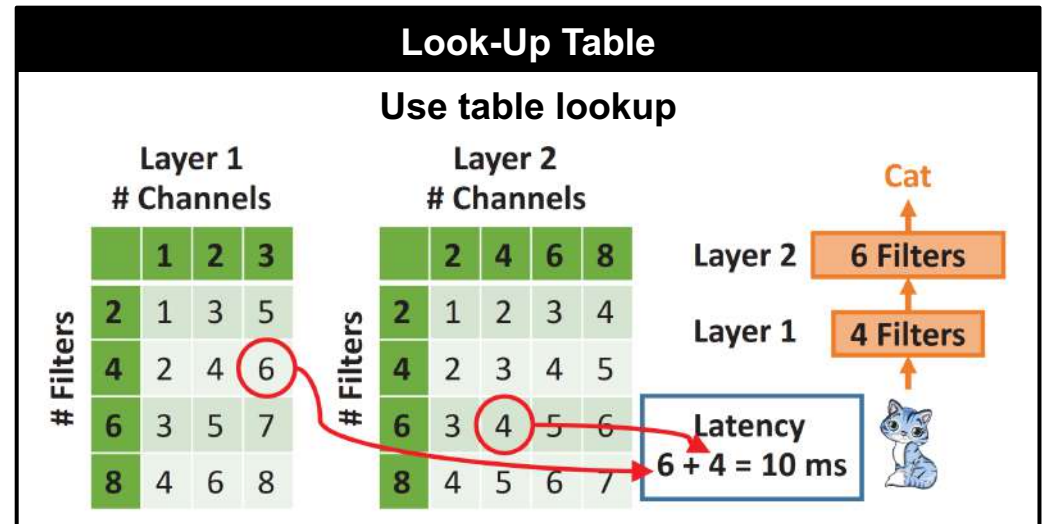
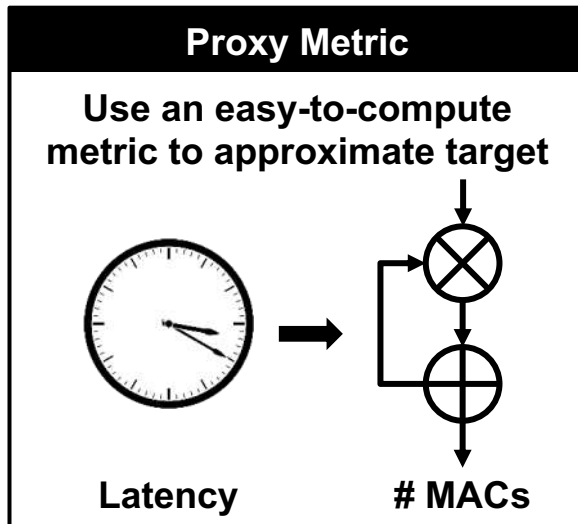
- NAS needs only the rank of the performance values
- Method 1: approximate accuracy
- Method 2: approximate weights



- Method 3: approximate metrics

# (3) Simplify the Performance Evaluation

- NAS needs only the rank of the performance values
- Method 1: approximate accuracy
- Method 2: approximate weights
- Method 3: approximate metrics (e.g., latency, energy)

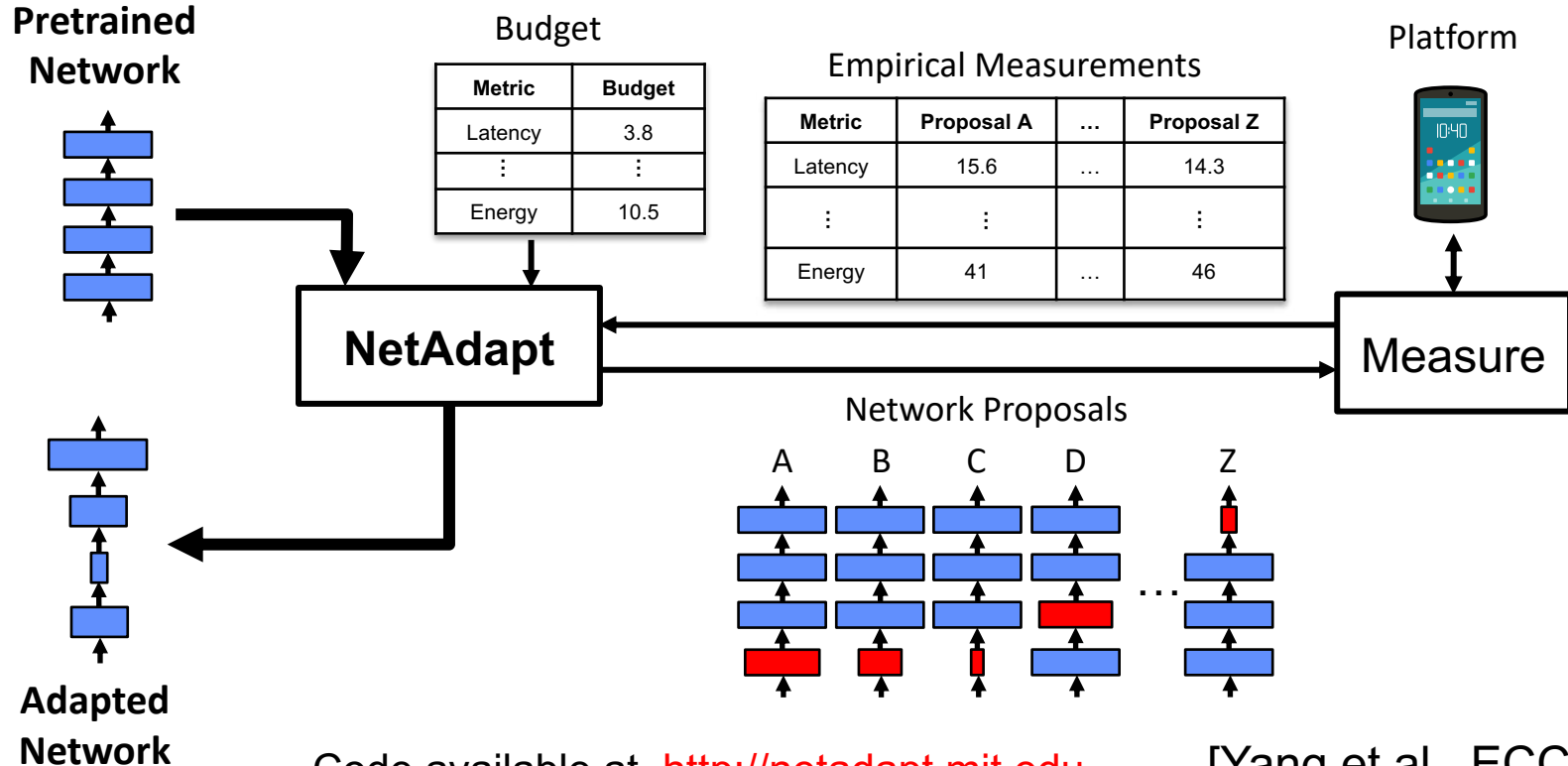


# Other Things to Know

- **The components may not be chosen individually**
  - Some optimization algorithms limit the search space
  - Using direct hardware metrics may limit the selection of the optimization algorithms
- **Commonly overlooked properties**
  - The complexity of implementation and usage
  - The ease of tuning
  - The probability of convergence to a good architecture

# NetAdapt: Platform-Aware DNN Adaptation

- **Automatically adapt DNN** to a mobile platform to reach a target latency or energy budget
- An example of **coordinate descent NAS**



Code available at <http://netadapt.mit.edu>

[Yang et al., ECCV 2018]

# Problem Formulation

$$\max_{Net} Acc(Net) \text{ subject to } Res_j(Net) \leq Bud_j, j = 1, \dots, m$$



Break into a set of simpler problems and solve iteratively

$$\max_{Net_i} Acc(Net_i) \text{ subject to } Res_j(Net_i) \leq Res_j(Net_{i-1}) - \Delta R_{i,j}, j = 1, \dots, m$$

\**Acc*: accuracy function, *Res*: resource evaluation function,  
 **$\Delta R$** : resource reduction, *Bud*: given budget

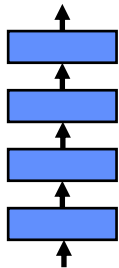
## • Advantages

- Supports multiple resource budgets at the same time
- Guarantees that the budgets will be satisfied because the resource consumption decreases monotonically
- Generates a family of networks (from each iteration) with different resource versus accuracy trade-offs

# Simplified Example of One Iteration

## 1. Input

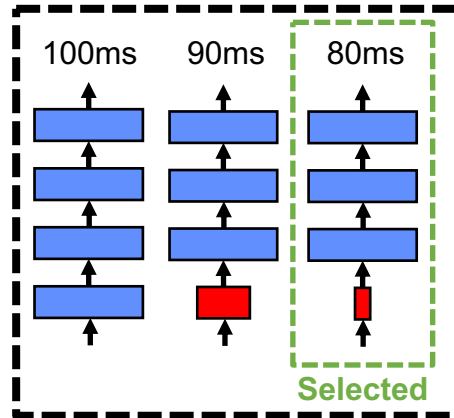
Network from  
Previous Iteration



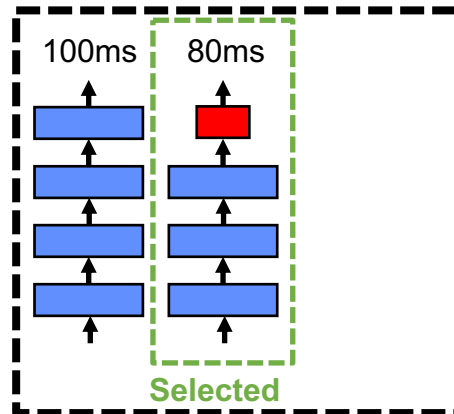
Latency: 100ms  
Budget: 80ms

## 2. Meet Budget

Layer 1

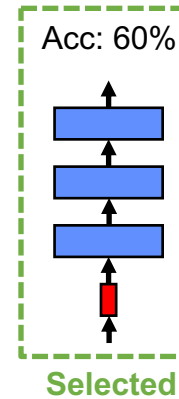


Layer 4

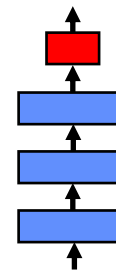


## 3. Maximize Accuracy

Acc: 60%

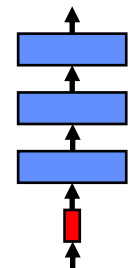


Acc: 40%



## 4. Output

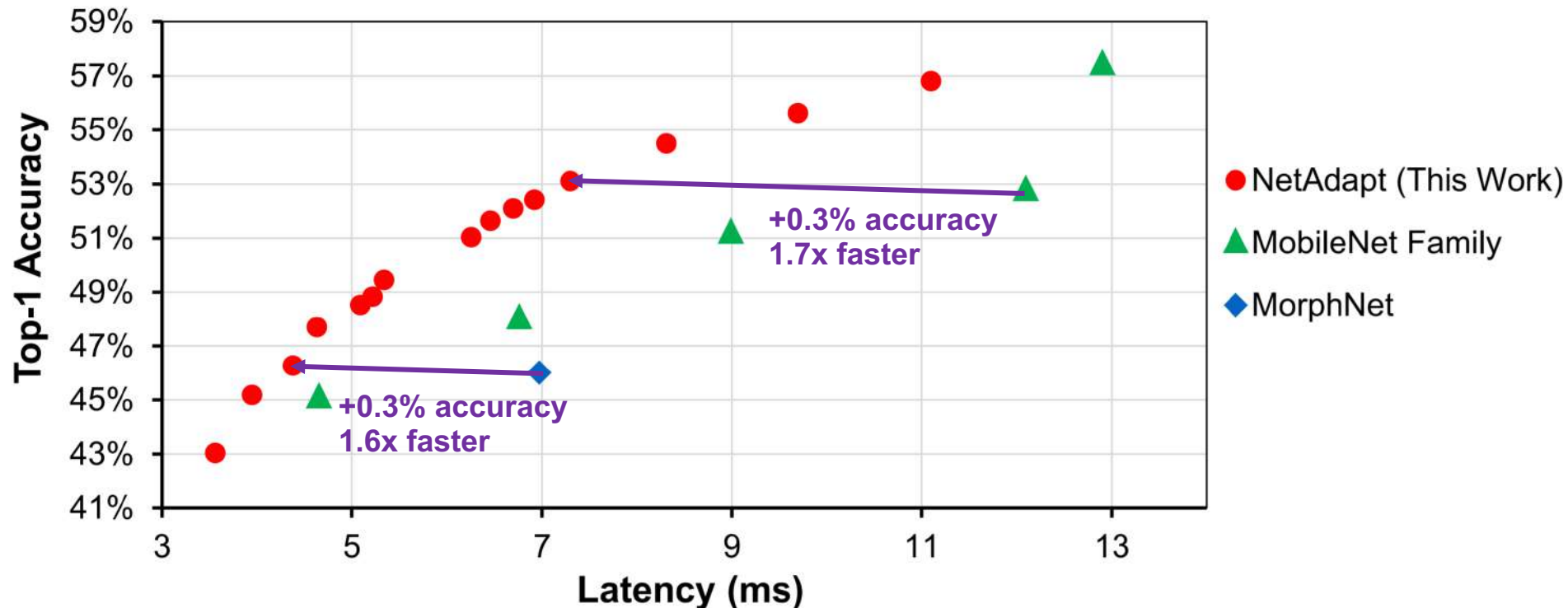
Network for  
Next Iteration



Latency: 80ms  
Budget: 60ms

# Improved Latency vs. Accuracy Tradeoff

- NetAdapt boosts **the real inference speed** of MobileNet by up to 1.7x with higher accuracy



\*Tested on the ImageNet dataset and a Google Pixel 1 CPU

Reference:

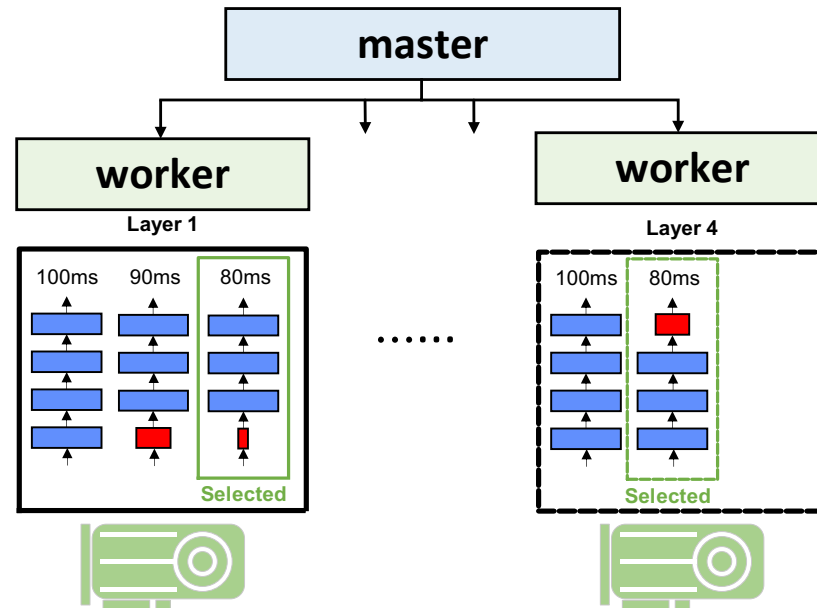
**MobileNet:** Howard et al, "Mobilenets: Efficient convolutional neural networks for mobile vision applications", arXiv 2017

**MorphNet:** Gordon et al., "Morphnet: Fast & simple resource-constrained structure learning of deep networks", CVPR 2018



# Code of NetAdapt

- Reimplemented framework on PyTorch
- **Flexible:** can support **different networks and tasks**
- **Scalable:** spawn multiple workers to simplify networks in parallel



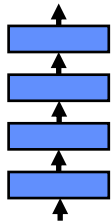
- **Easy-to-use:** require implementing only **one file (8 functions)**

Code available at <https://github.com/denru01/netadapt>

# Code of NetAdapt

## 1. Input

Network from  
Previous Iteration



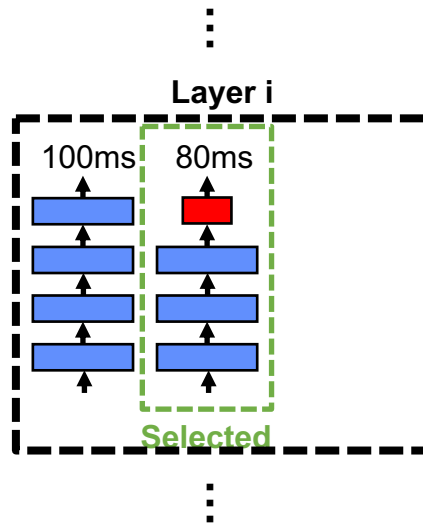
Latency: 100ms  
Budget: 80ms

```
get_num_simplifiable_blocks()
```

```
get_network_def_from_model()
```

Layer 1: ( 3, 16)  
Layer 2: (16, 32)  
Layer 3: (32, 64)  
Layer 4: (64, 10)

## 2. Meet Budget

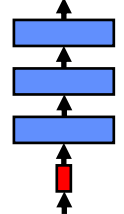


## 3. Maximize Accuracy



## 4. Output

Network for Next  
Iteration

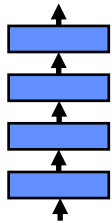


Latency: 80ms  
Budget: 60ms

# Code of NetAdapt

## 1. Input

Network from  
Previous Iteration



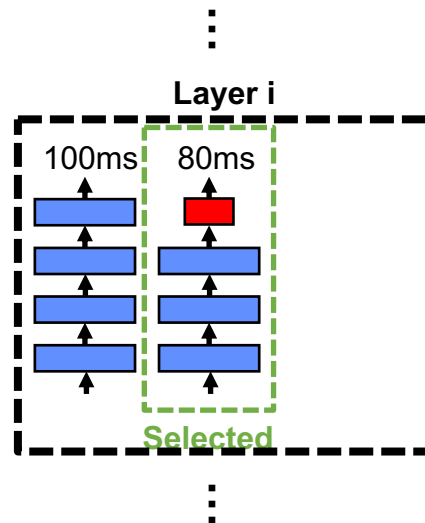
Latency: 100ms  
Budget: 80ms

```
get_num_simplifiable_blocks()
```

```
get_network_def_from_model()
```

Layer 1: ( 3, 16)  
Layer 2: (16, 32)  
Layer 3: (32, 64)  
Layer 4: (64, 10)

## 2. Meet Budget



```
compute_resource()
```

```
simplify_network_def_based_on_constraint()
```

```
simplify_model_based_on_network_def()
```

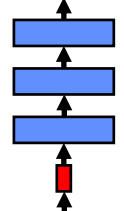
```
finetune()
```

## 3. Maximize Accuracy



## 4. Output

Network for Next  
Iteration

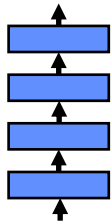


Latency: 80ms  
Budget: 60ms

# Code of NetAdapt

## 1. Input

Network from  
Previous Iteration



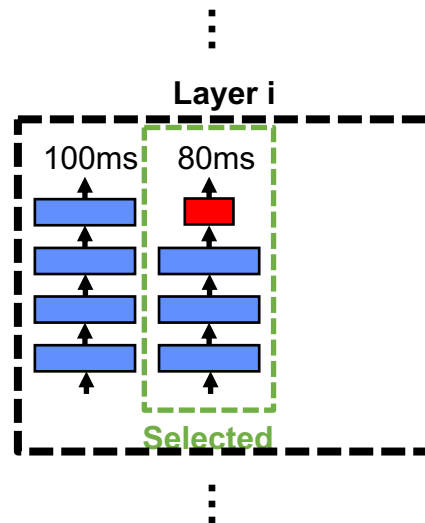
Latency: 100ms  
Budget: 80ms

```
get_num_simplifiable_blocks()
```

```
get_network_def_from_model()
```

Layer 1: ( 3, 16)  
Layer 2: (16, 32)  
Layer 3: (32, 64)  
Layer 4: (64, 10)

## 2. Meet Budget



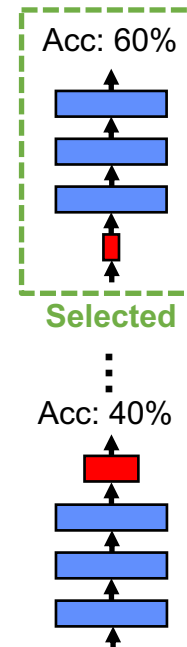
```
compute_resource()
```

```
simplify_network_def_based_on_constraint()
```

```
simplify_model_based_on_network_def()
```

```
finetune()
```

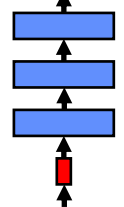
## 3. Maximize Accuracy



```
evaluate()
```

## 4. Output

Network for Next  
Iteration

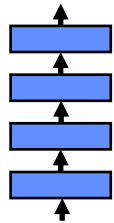


Latency: 80ms  
Budget: 60ms

# Code of NetAdapt

## 1. Input

Network from  
Previous Iteration



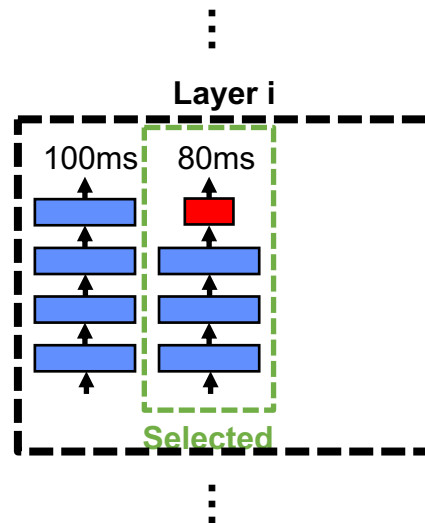
Latency: 100ms  
Budget: 80ms

```
get_num_simplifiable_blocks()
```

```
get_network_def_from_model()
```

Layer 1: ( 3, 16)  
Layer 2: (16, 32)  
Layer 3: (32, 64)  
Layer 4: (64, 10)

## 2. Meet Budget



```
compute_resource()
```

```
simplify_network_def_based_on_constraint()
```

```
simplify_model_based_on_network_def()
```

```
finetune()
```

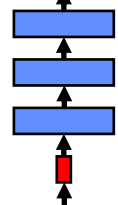
## 3. Maximize Accuracy



```
evaluate()
```

## 4. Output

Network for Next  
Iteration



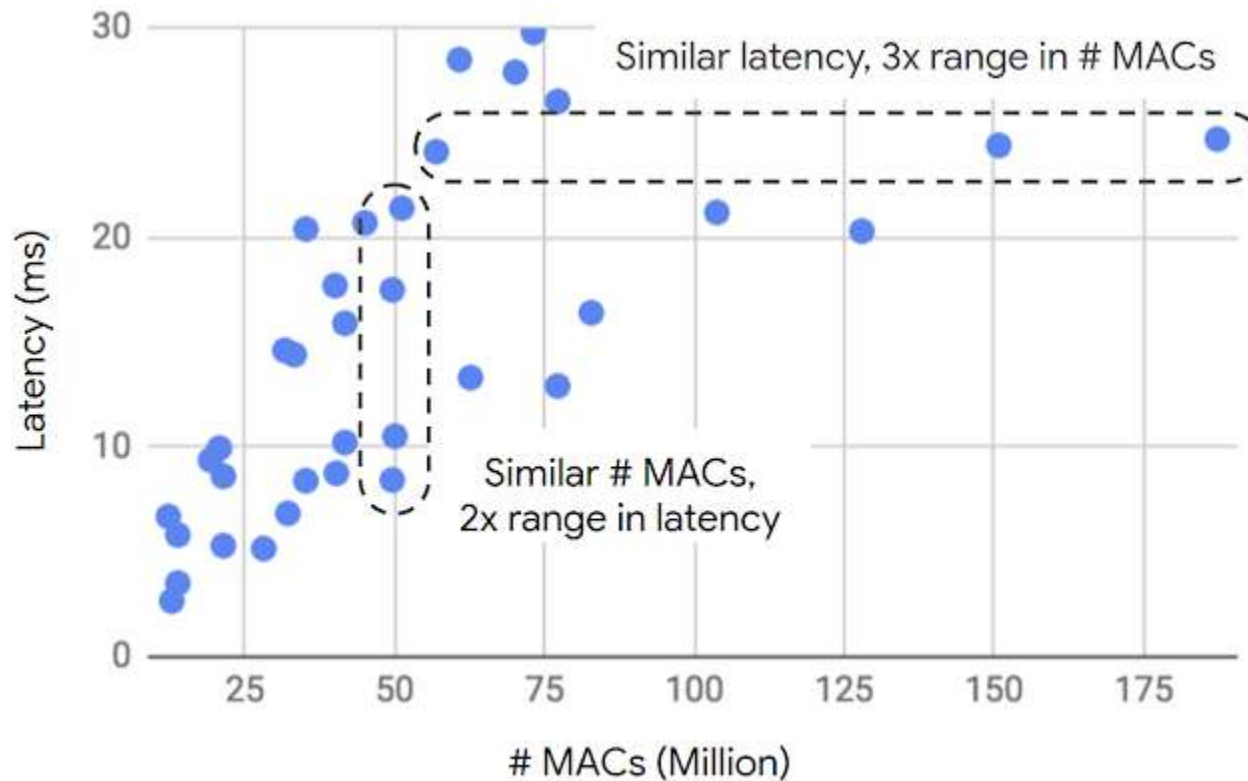
Latency: 80ms  
Budget: 60ms

Some ready-to-use utilities  
have been provided to  
facilitate implementation.

# Hardware In the Loop

# # of Operations vs. Latency

- # of operations (MACs) does not approximate latency well

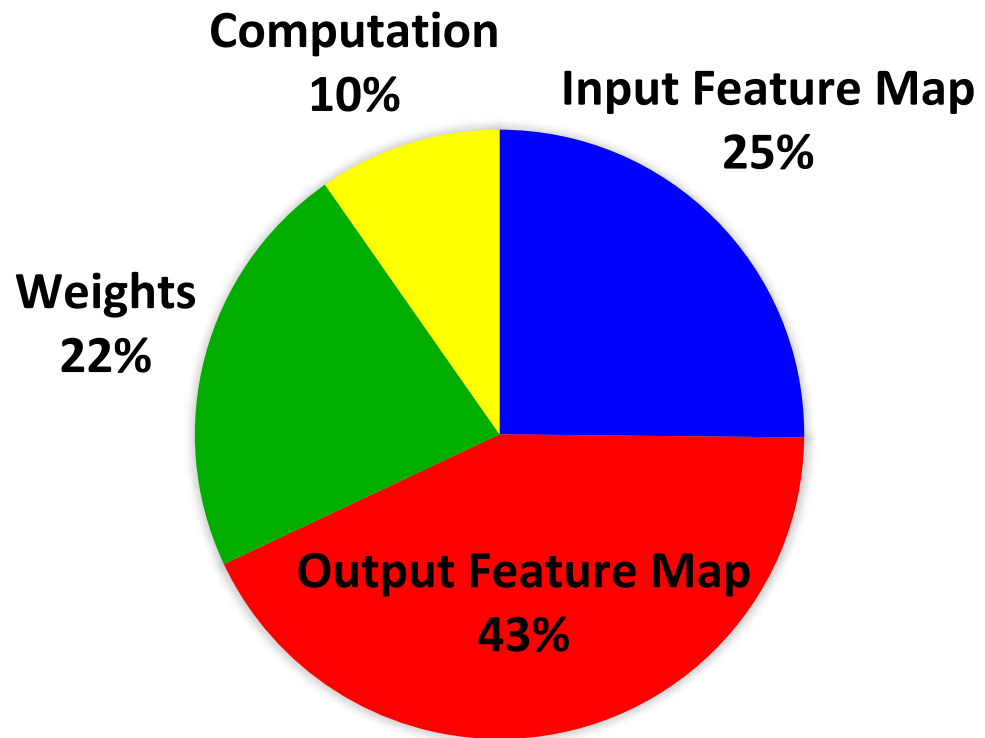


Source: Google (<https://ai.googleblog.com/2018/04/introducing-cvpr-2018-on-device-visual.html>)

# # of Weights vs. Energy

- Number of weights ***alone*** is not a good metric for energy
- **All data types** should be considered

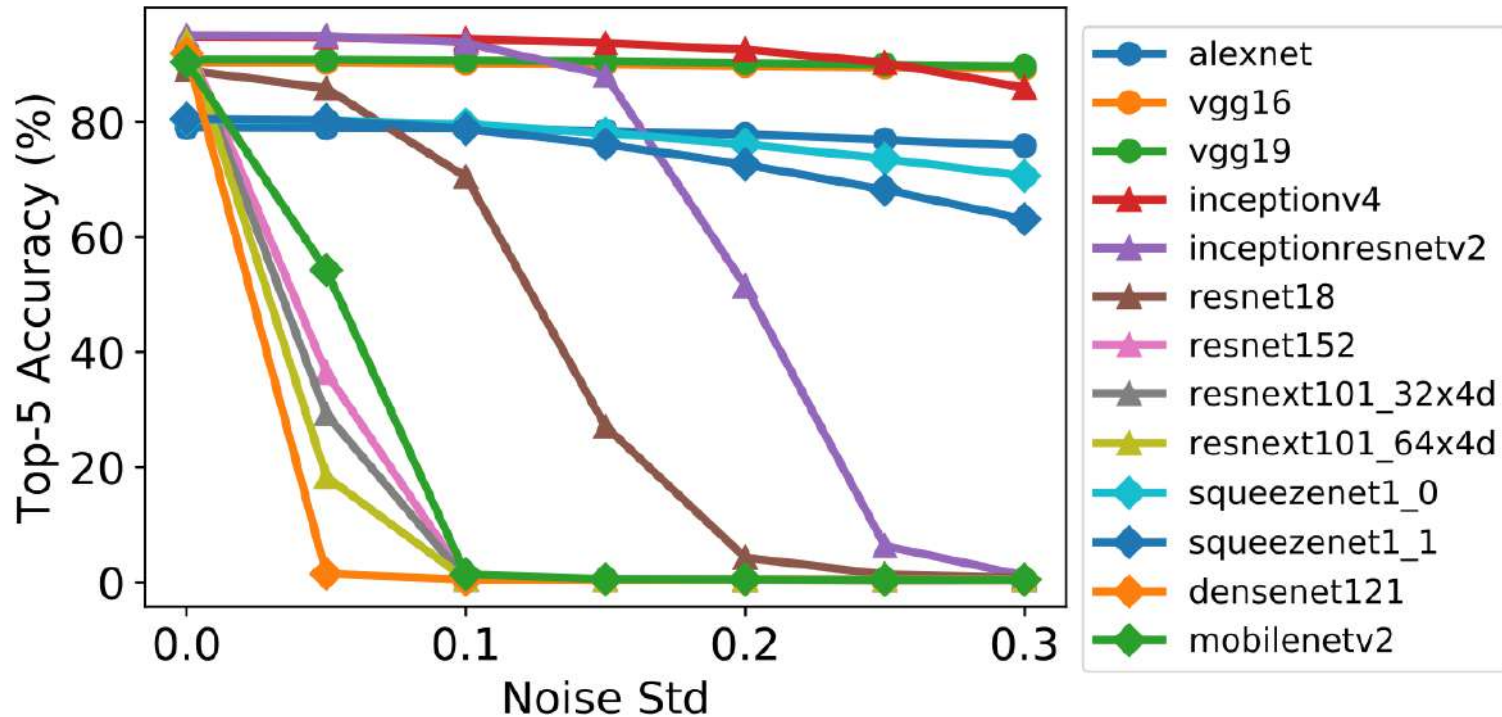
## Energy Consumption of GoogLeNet





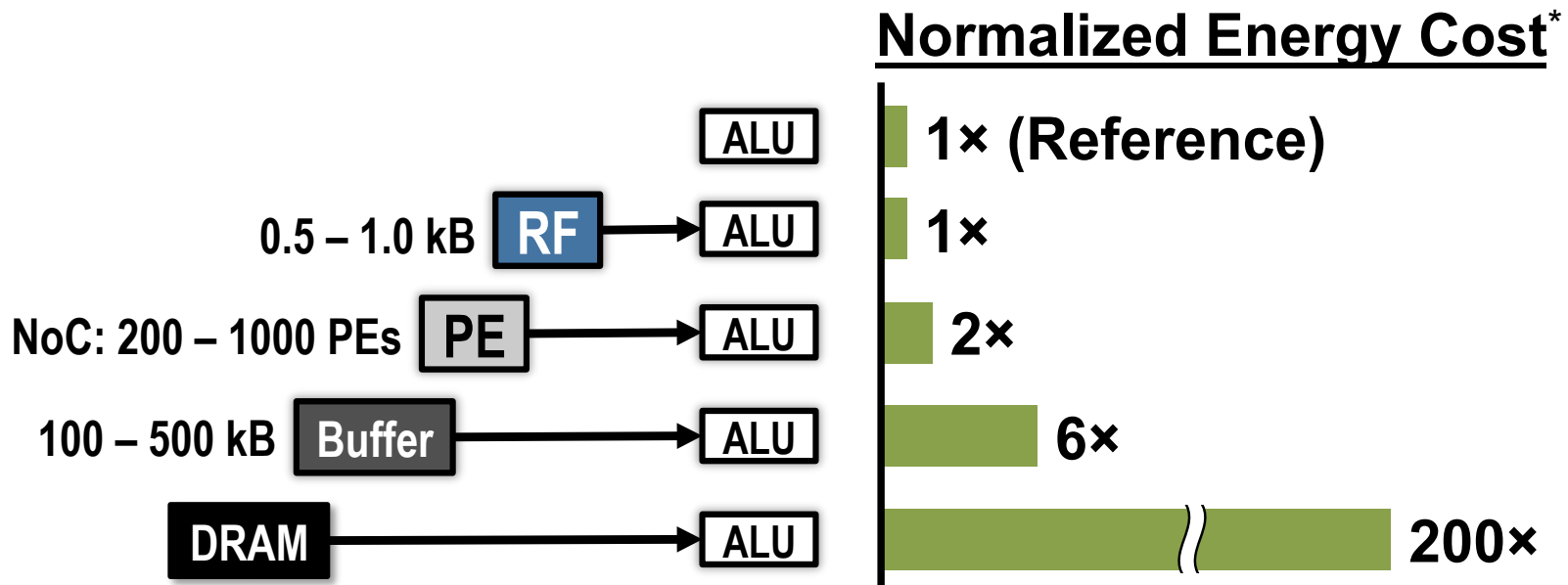
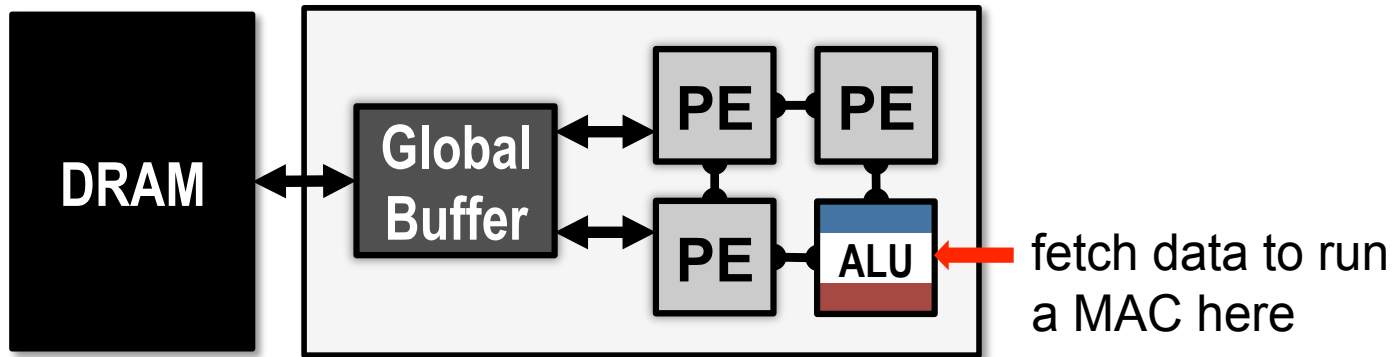
# Other Hardware Metrics

- E.g., noise resilience in analog accelerators



**DNN model that gives highest accuracy on a digital processor may not be the best for an analog processor**

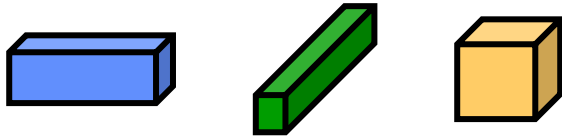
# Data Movement is Expensive



\* measured from a commercial 65nm process

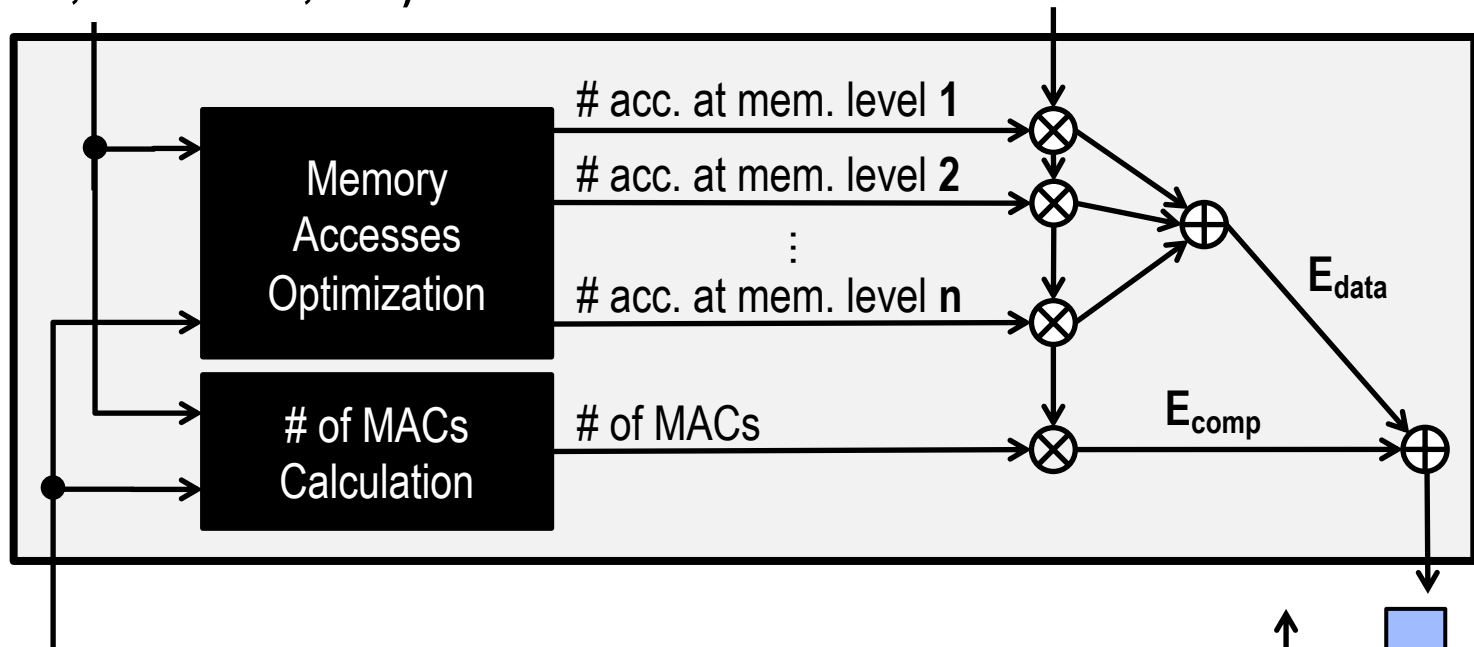
Energy of weight depends on **memory hierarchy** and **dataflow**

# Energy Estimation Methodology

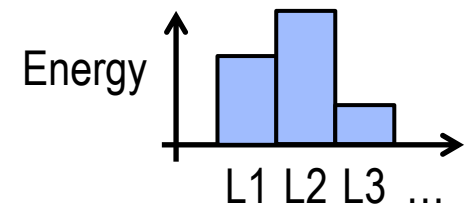


**DNN Shape Configuration**  
(# of channels, # of filters, etc.)

**Hardware Energy Costs of each  
MAC and Memory Access**



**DNN Weights and Input Data**  
[0.3, 0, -0.4, 0.7, 0, 0, 0.1, ...]



**DNN Energy Consumption**

# Energy Estimation Tool V1

Website: <https://energyestimation.mit.edu/>

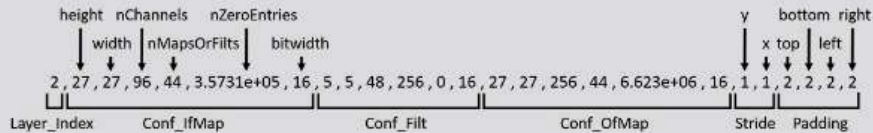
## Deep Neural Network Energy Estimation Tool

### Overview

This Deep Neural Network Energy Estimation Tool is used for evaluating and designing energy-efficient deep neural networks that are critical for embedded deep learning processing. Energy estimation was used in the development of the energy-aware pruning method (Yang et al., CVPR 2017), which reduced the energy consumption of AlexNet and GoogLeNet by 3.7x and 1.6x, respectively, with less than 1% top-5 accuracy loss. This website provides a simplified version of the energy estimation tool for shorter runtime (around 10 seconds).

### Input

To support the variety of toolboxes, this tool takes a single network configuration file. The network configuration file is a txt file, where each line denotes the configuration of a CONV/FC layer. The format of each line is:



- Layer\_Index:** the index of the layer, from 1 to the number of layers. It should be the same as the line number.
- Conf\_IfMap, Conf\_Filt, Conf\_OfMap:** the configuration of the input feature maps, the filters and the output feature maps. The configuration of each of the three data types is in the format of "height width number\_of\_channels number\_of\_maps\_or\_filt number\_of\_zero\_entries bitwidth\_in\_bits".
- Stride:** the stride of this layer. It is in the format of "stride\_y stride\_x".
- Pad:** the amount of input padding. It is in the format of "pad\_top pad\_bottom pad\_left pad\_right".

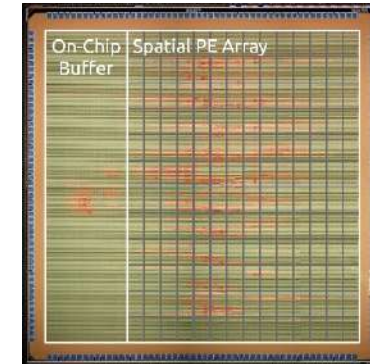
Therefore, there will be 25 entries separated by commas in each line.

### Running the Estimation Model

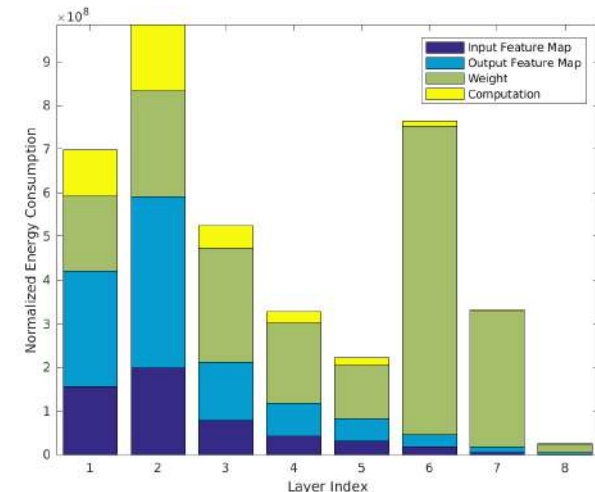
After creating your text file, follow these steps to upload your text file and run the estimation model:

1. Check the "I am not a robot" checkbox and complete the Google reCAPTCHA challenge. Help us prevent spam.
2. Click the "Choose File" button below to choose your text file from your computer.
3. Click the "Run Estimation Model" button below to upload your text file and run the estimation model.

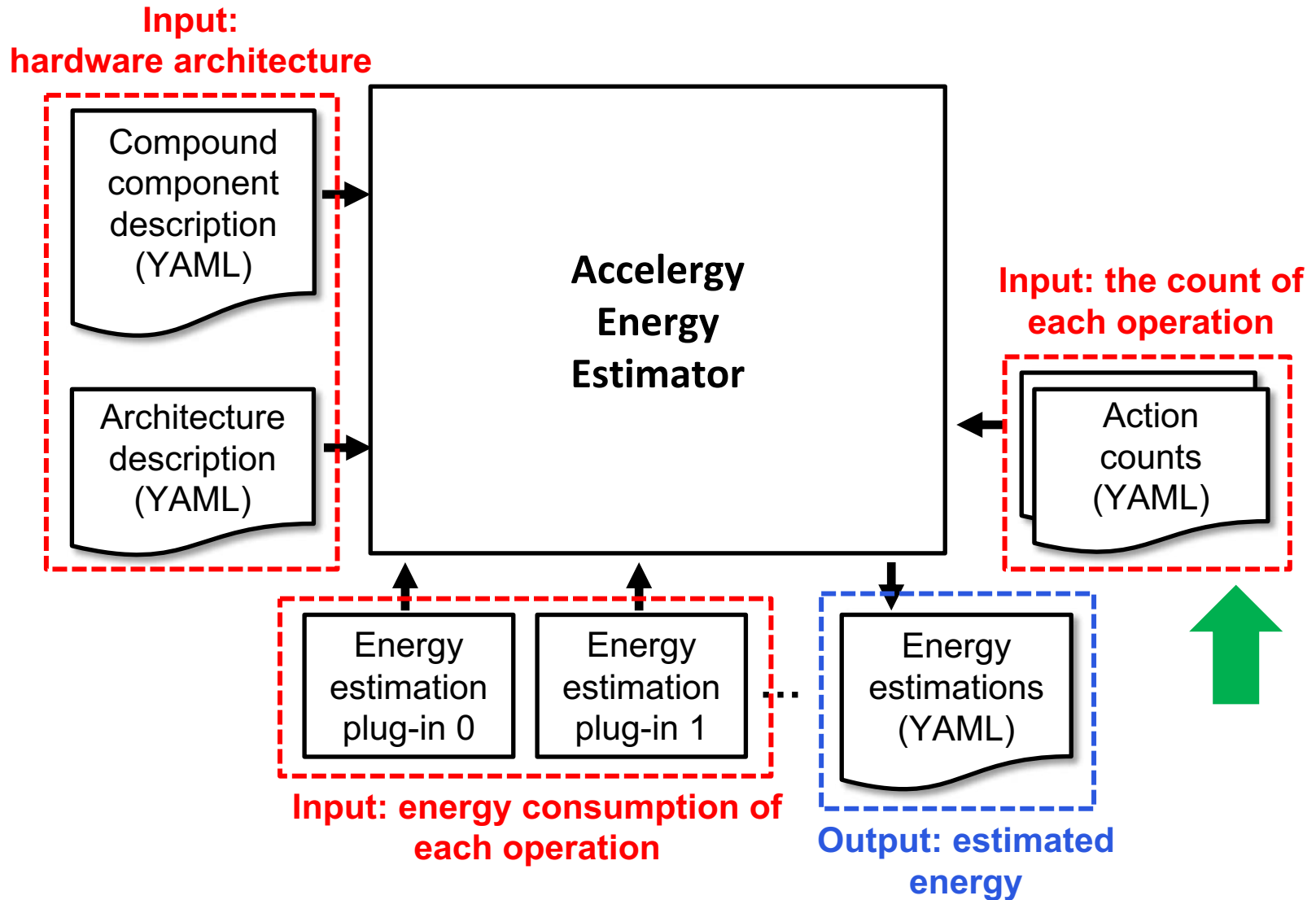
## Eyeriss V1



## Output DNN energy breakdown across layers

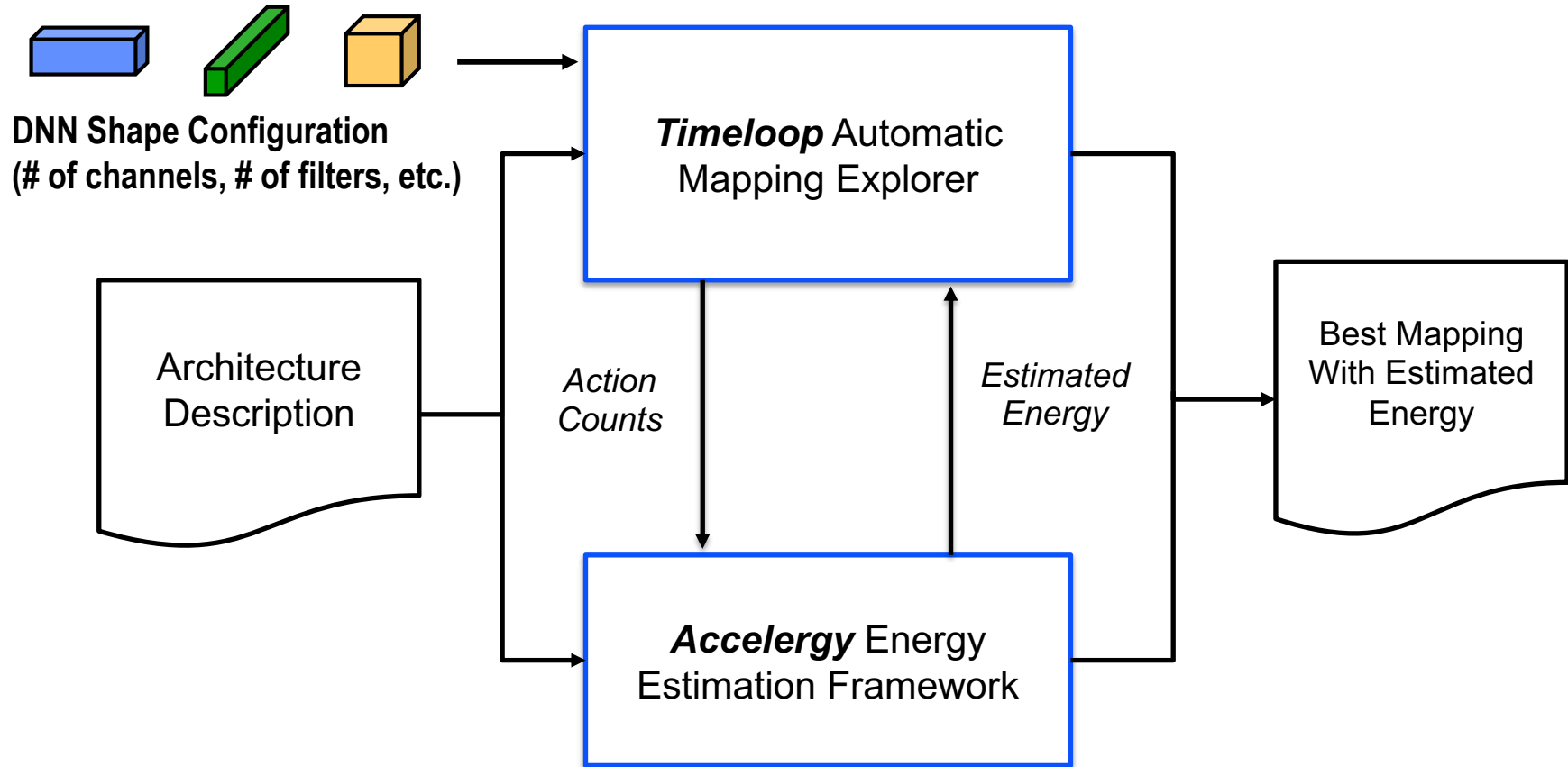


# Energy Estimation Tool V2 - Accelergy



# Energy Estimation Tool V2 - Accelergy

Integrate 3<sup>rd</sup>-party tools to generate the count of each operation



Tutorial at MICRO 2019: <http://accelergy.mit.edu/tutorial.html>

# Energy Estimation Tool V2 - Accelergy

Website: <https://accelergy.mit.edu/>

nelliewu95 / accelergy

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Code Issues 0 Pull requests 0 Projects 0 Wiki Security Insights

No description, website, or topics provided.

22 commits 1 branch 1 release 2 contributors MIT

Branch: master New pull request Create new file Upload files Find File Clone or download

File	Commit Message	Time Ago
accelergy	Delete ERT_generator_old.py	2 days ago
examples	v0.2 initial milestone	2 days ago
share	compound class v0.2 parsing	3 days ago
.gitignore	v0.2 initial milestone	2 days ago
COPYRIGHT	initial commit	3 months ago
README.md	v0.2 initial milestone	2 days ago
setup.py	separation of v0.1 and v0.2	3 days ago

README.md

## Accelergy infrastructure (version 0.2)

An infrastructure for architecture-level energy estimations of accelerator designs. Project website: <http://accelergy.mit.edu>

### Get started

- Infrastructure tested on RedHat Linux6 WLS

## Output DNN energy breakdown across components

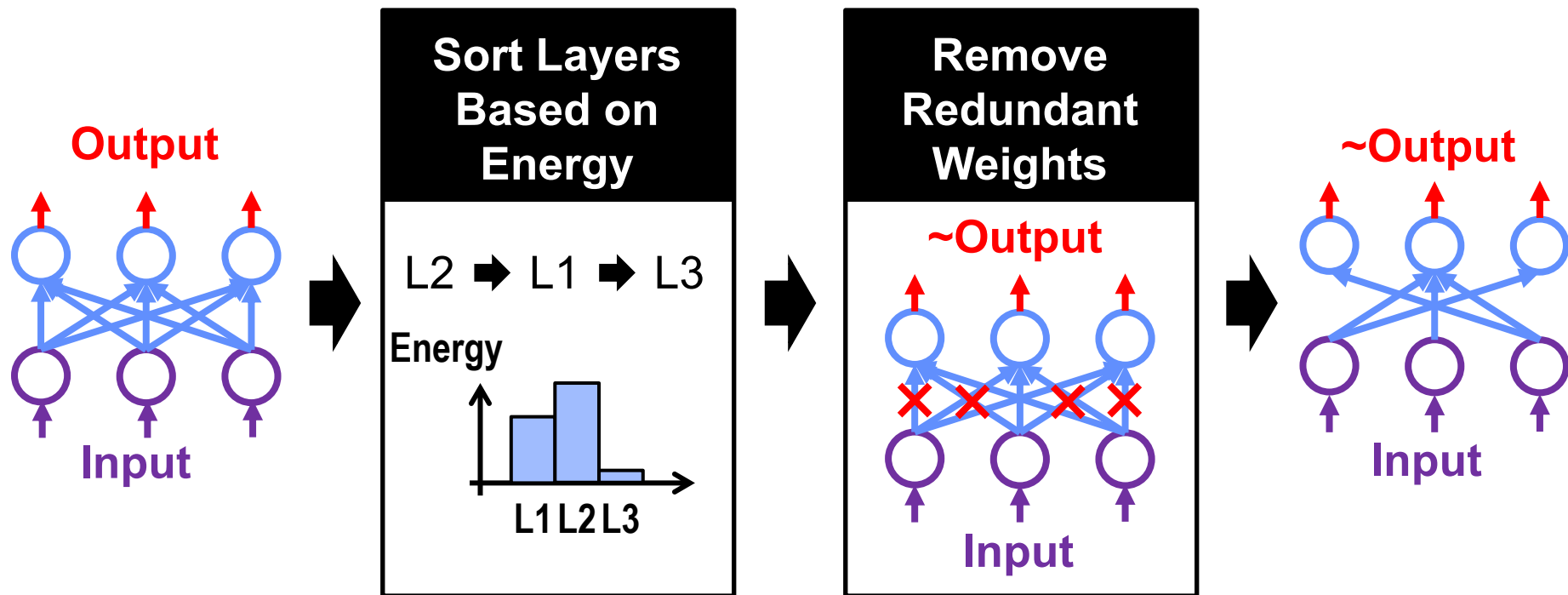
```

hierarchy.PE[0].ifmap_sp: 140.0
hierarchy.PE[0].mac[0]: 70.0
hierarchy.PE[0].mac[1]: 70.0
hierarchy.PE[1].ifmap_sp: 180.0
hierarchy.PE[1].mac[0]: 70.0
hierarchy.PE[1].mac[1]: 70.0
hierarchy.weights_glb: 5400.0
  
```



# Energy-Aware Pruning

- Problem formulation:  $\min_{Net} Erg(Net)$  subject to  $Acc(Net) \geq Th$
- Reduces energy by **removing redundant weights**
- Uses **estimated energy** to guide the layer-by-layer pruning
  - Prunes the layer that consume the most energy first

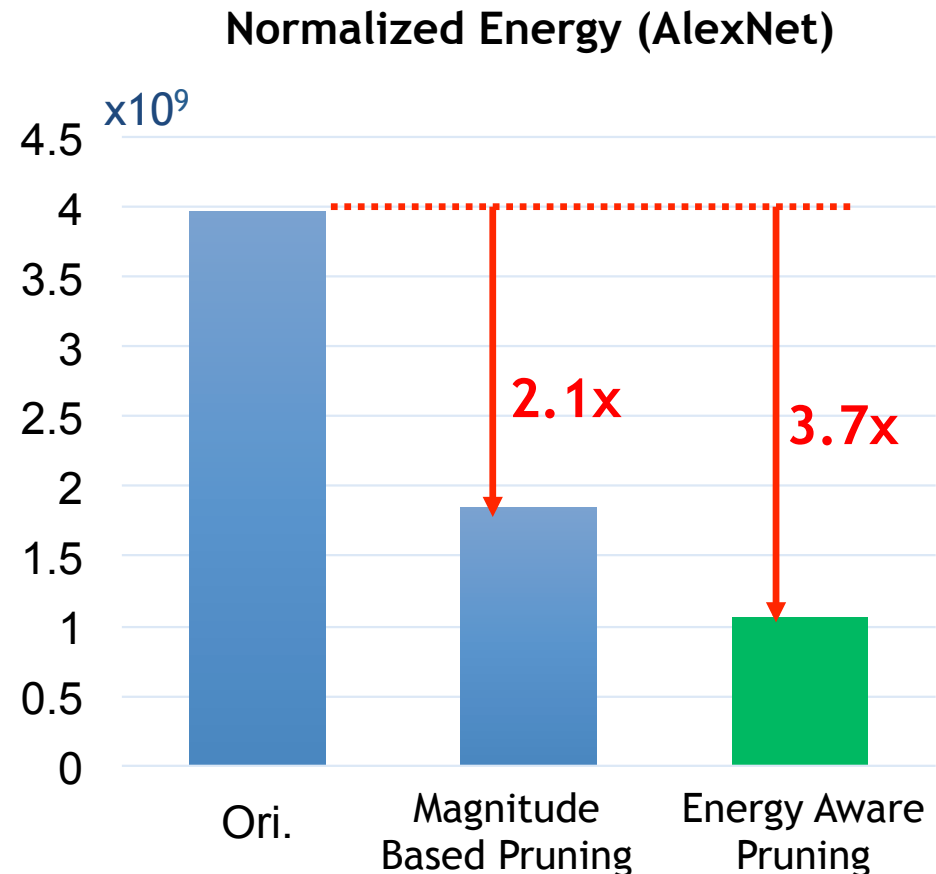




# Energy-Aware Pruning

Directly target energy and incorporate it into the optimization of DNNs to provide greater energy savings

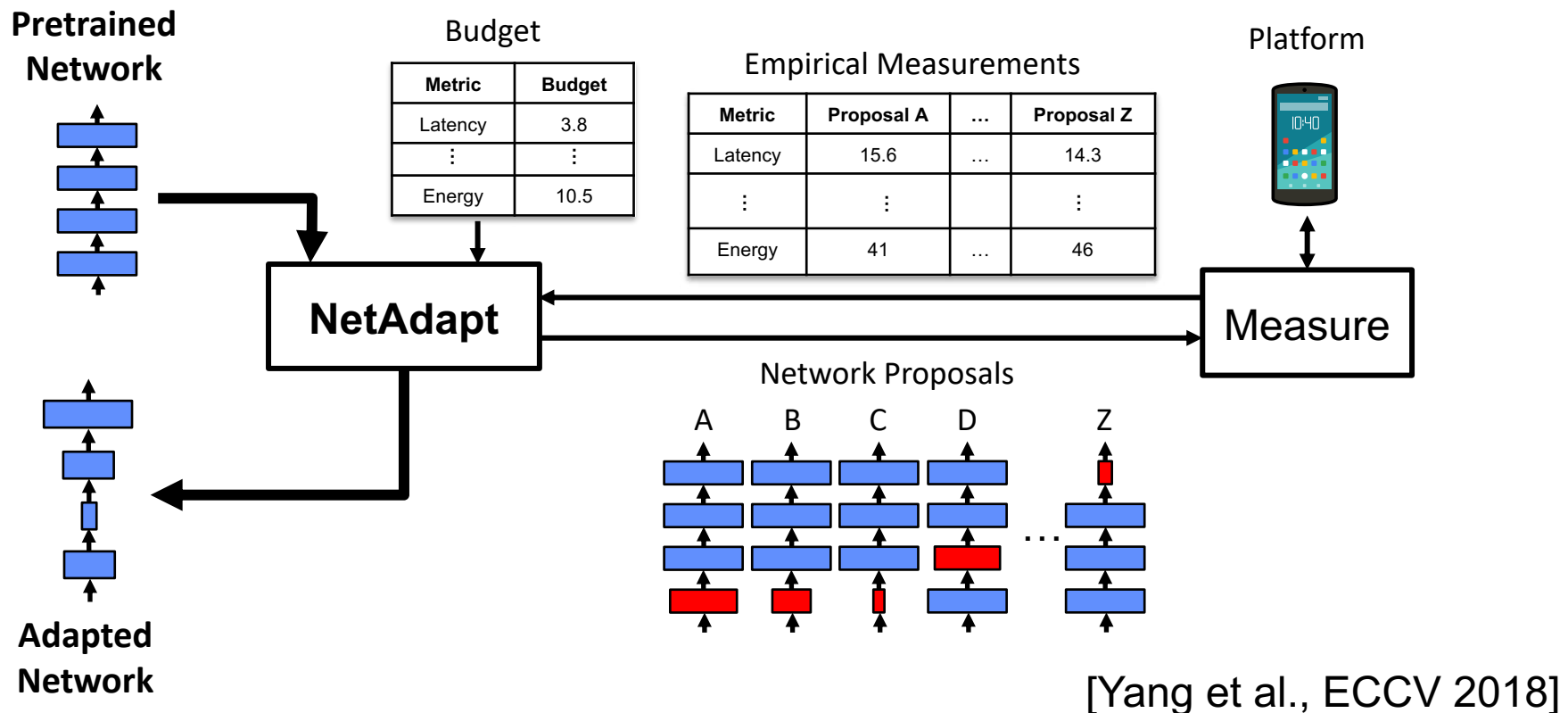
- Sort layers based on energy and prune layers that consume most energy first
- EAP reduces AlexNet energy by **3.7x** and outperforms the previous work that uses magnitude-based pruning by **1.7x**



Pruned models available at  
<http://eyeriss.mit.edu/energy.html>

# NetAdapt: Platform-Aware DNN Adaptation

- **Automatically adapt DNN** to a mobile platform to reach a target latency or energy budget
- Use **empirical measurements** to guide optimization (avoid modeling of tool chain or platform architecture)



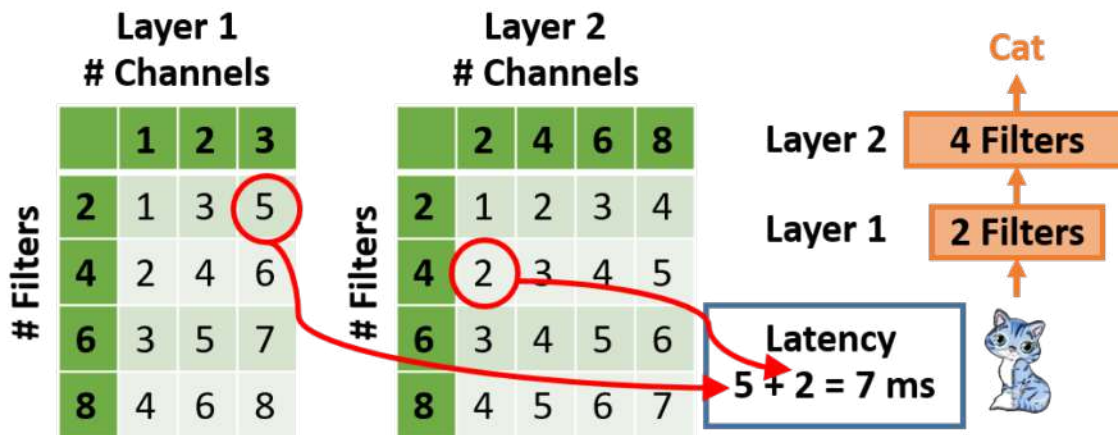
# NetAdapt: Using Direct Metrics is Important

- If NetAdapt was guided by the number of MACs, it would also achieve a better accuracy-MAC trade-off
- However, it does not mean lower latency
- It is important to incorporate direct metrics rather than indirect metrics into the design of DNNs

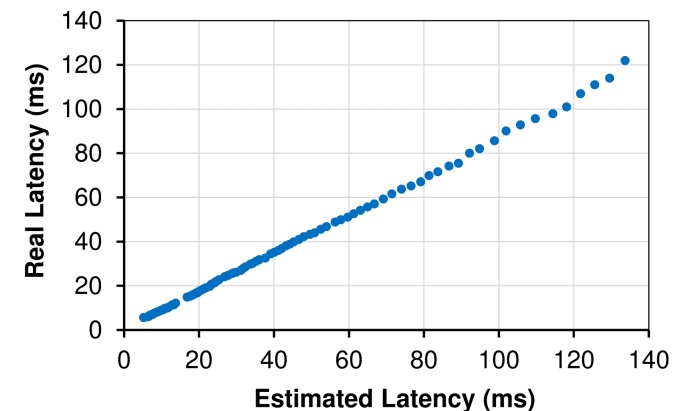
Network	Top-1 Accuracy	# of MACs (M)	Latency (ms)
Small MobileNet V1	45.1 (+0)	13.6 (100%)	4.65 (100%)
NetAdapt	46.3 (+1.2)	11.0 (81%)	6.01 (129%)
Large MobileNet V1	68.8 (+0)	325.4 (100%)	69.3 (100%)
NetAdapt	69.1 (+0.3)	284.3 (87%)	74.9 (108%)

# NetAdapt: Fast Resource Consumption Estimation

- Taking measurements can be slow due to the long turn-around time and the limited number of platforms
- Solution: use per-layer lookup tables
  - The network latency can be estimated by the sum of the latency of each layer
  - The layers with the same configuration only need to be measured once
  - The network-wide lookup table grows exponentially with the number of layers



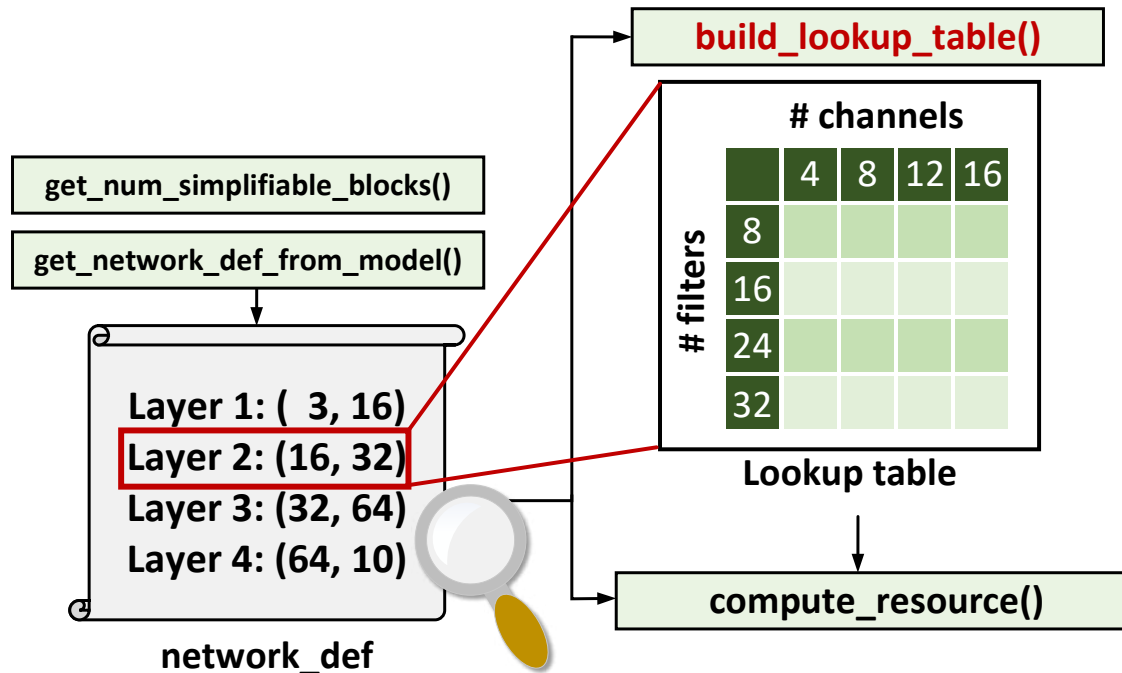
Fast Resource Consumption Estimation



Real Latency vs. Estimated Latency

# NetAdapt: Code

- Support building and using lookup tables



Code available at <https://github.com/denru01/netadapt>

# Part 3: Applications (Beyond Image Classification)

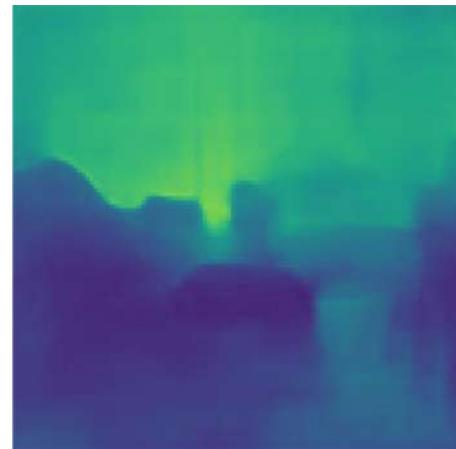
# FastDepth: Fast Monocular Depth Estimation

- Real-time low-power depth sensing is critical for navigation of small robotic vehicles.
- Depth estimation from a single RGB image desirable, due to the relatively low cost and size of monocular cameras.

RGB

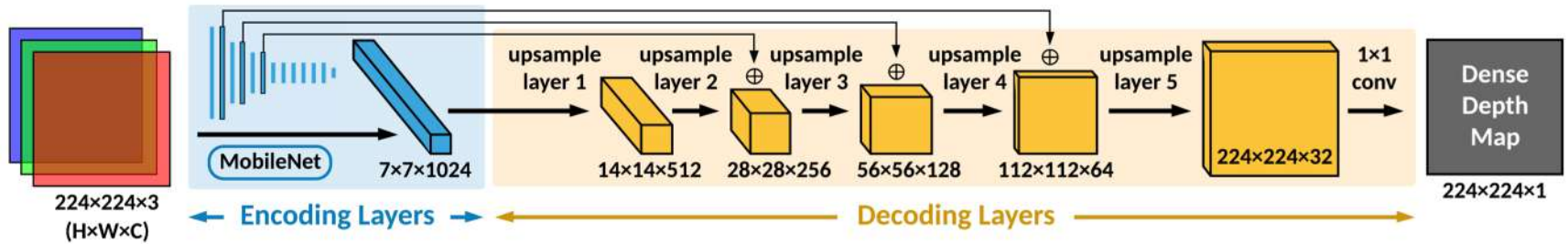


Prediction



Our goal is to enable **high accuracy, low latency, high throughput monocular depth estimation** on a **deployable embedded system**.

# Efficient Network Design for FastDepth



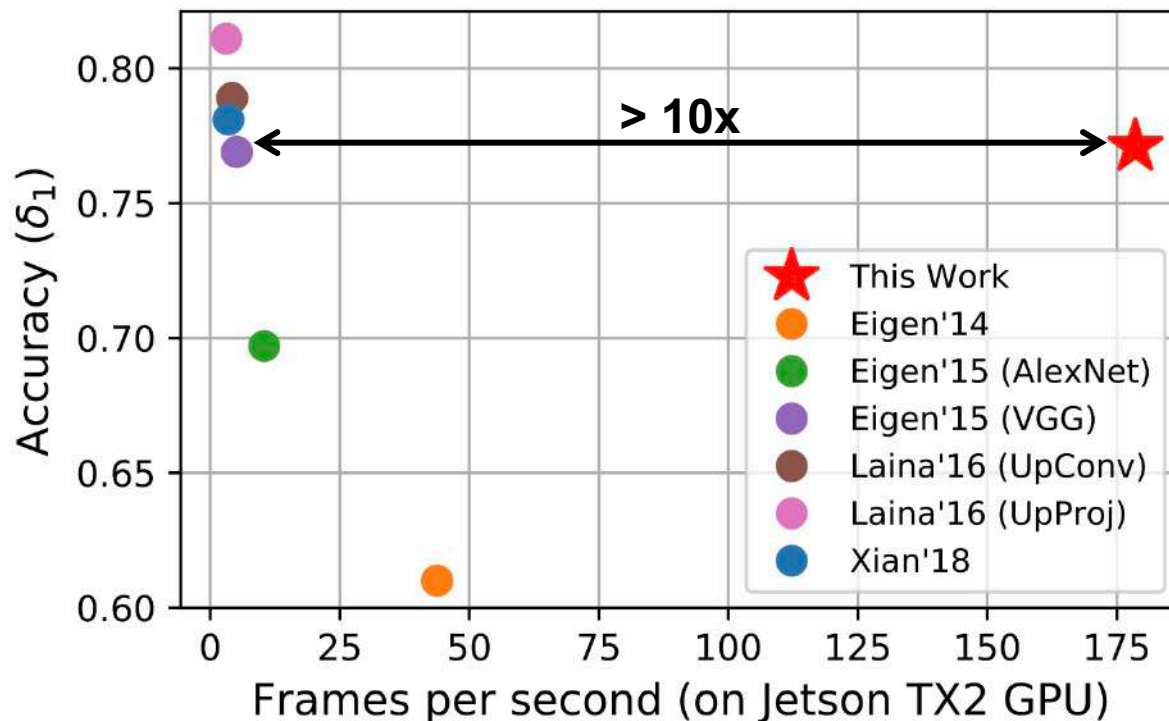
FastDepth achieves high frame rates through

- An efficient and lightweight encoder-decoder network architecture with a low-latency decoder design incorporating depthwise separable layers and additive skip connections
- Network pruning (NetAdapt) applied to whole encoder-decoder network
- Platform-specific compilation (TVM) targeting embedded systems



# FastDepth: Fast Monocular Depth Estimation

Depth estimation at **high frame rates on an embedded platform**  
(an order of magnitude faster than previous approaches) while  
still maintaining accuracy



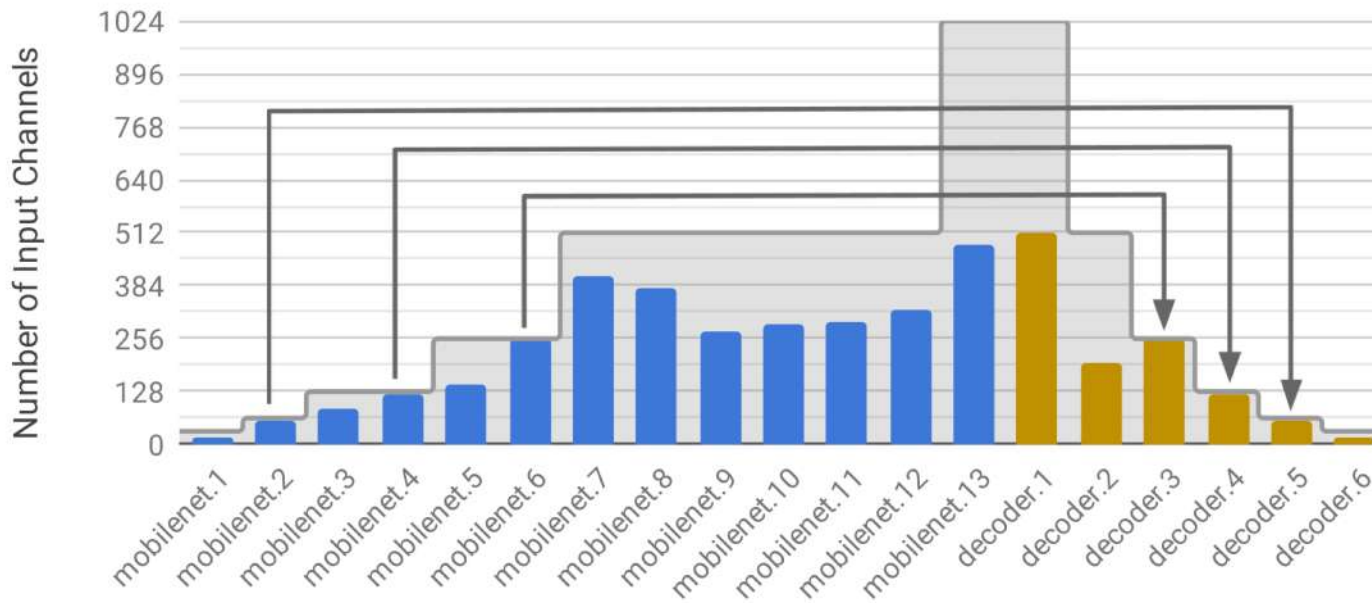
*Configuration: Batch size of one (32-bit float)*



~40fps on  
an iPhone

# Simplify Network by NetAdapt

	Before Pruning	After Pruning	Reduction
Weights	3.93M	1.34M	2.9×
MACs	0.74G	0.37G	2.0×
RMSE	0.599	0.604	-
$\delta_1$	0.775	0.771	-
CPU [ms]	66	37	1.8×
GPU [ms]	8.2	5.6	1.5×



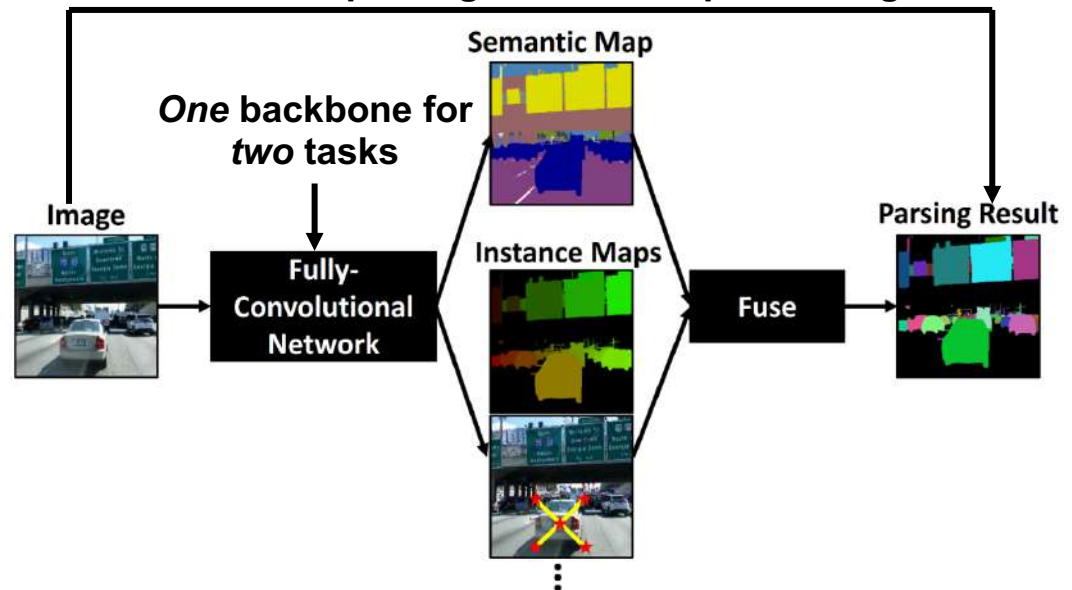
# DeeperLab: Single-Shot Image Parser

Joint Semantic and  
Instance Segmentation  
(high resolution  
input image)



**Fully convolutional,  
one-shot parsing  
(bottom-up approach)**

One-shot parsing for efficient processing



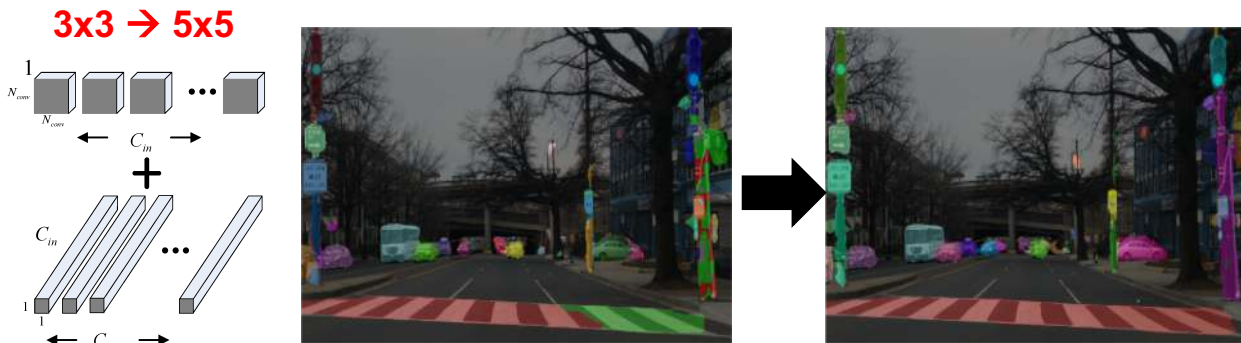
<http://deeperlab.mit.edu/>

[Yang et al., arXiv 2019]

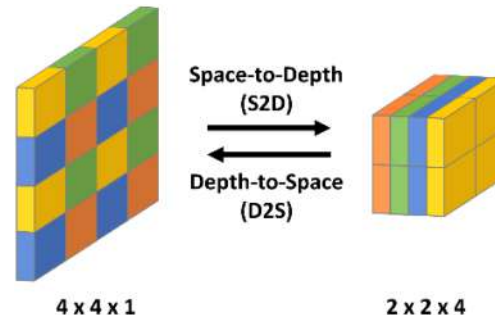
# DeeperLab: Efficient Image Parsing

## *Address memory requirement for large feature map*

- 1 Wide MobileNet: Increase kernel size rather than depth



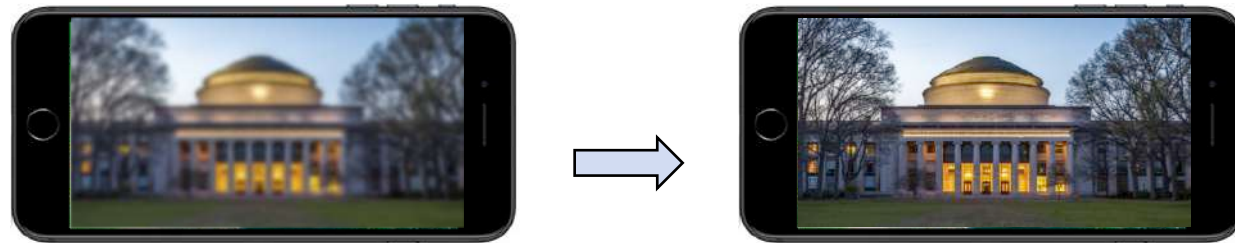
- 2 Space-to-depth/depth-to-space: Avoid upsampling



**Achieves near real-time 6.19  
fps on GPU (V100) with  
25.2% PQ and 49.8% PC on  
Mapillary Vistas dataset**

# Applications (Beyond DNN Acceleration)

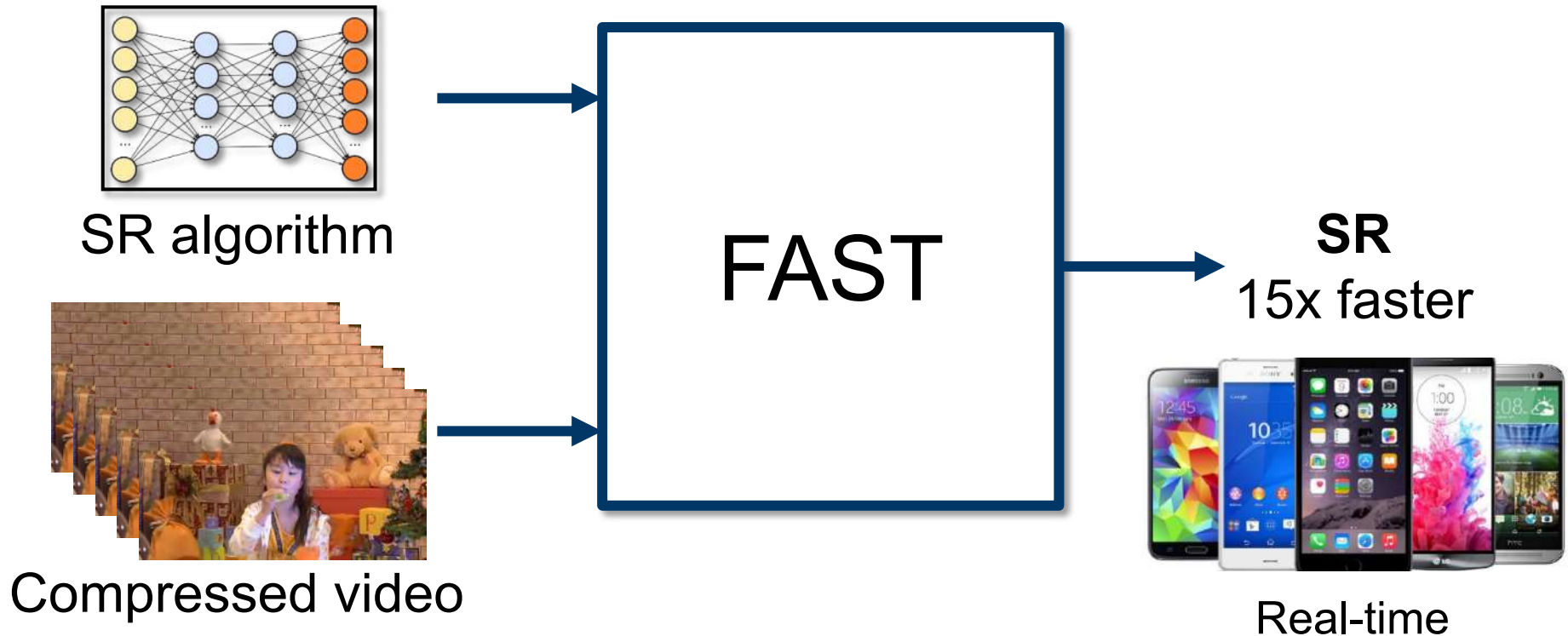
# Super-Resolution on Mobile Devices



Use **super-resolution** to improve the viewing experience of lower-resolution content (*reduce communication bandwidth*)

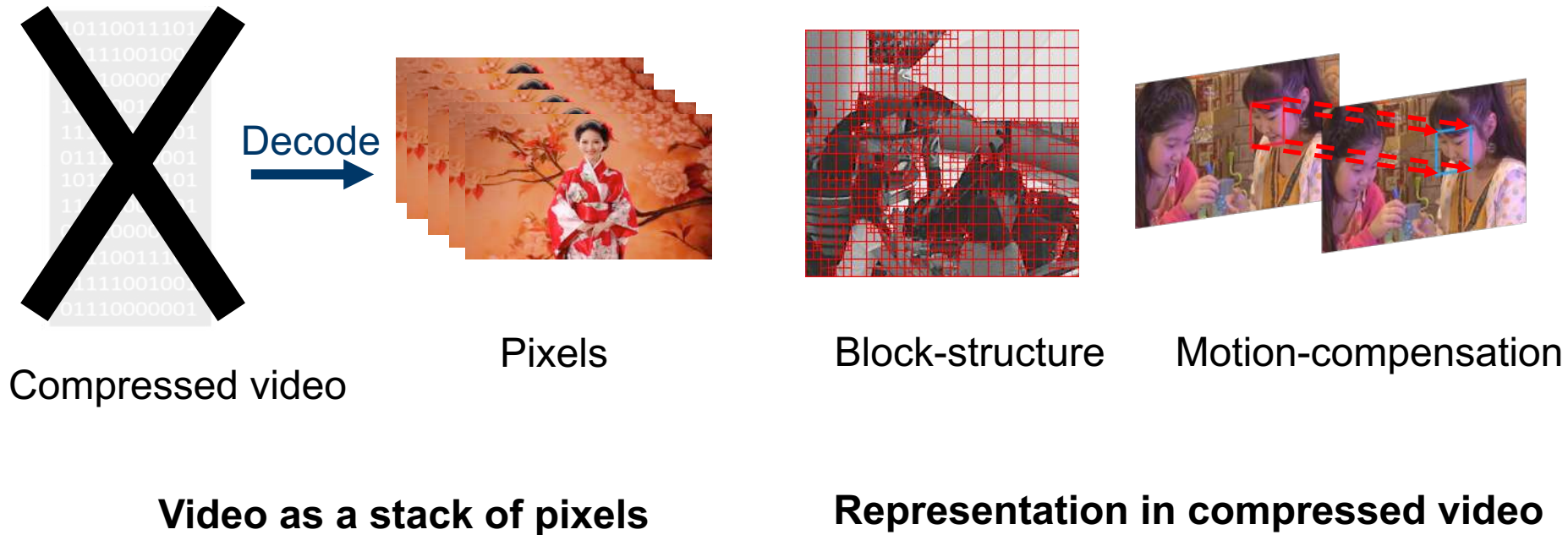


# FAST: A Framework to Accelerate SuperRes



A framework that accelerates **any SR** algorithm by up to **15x** when running on compressed videos

# Free Information in Compressed Videos



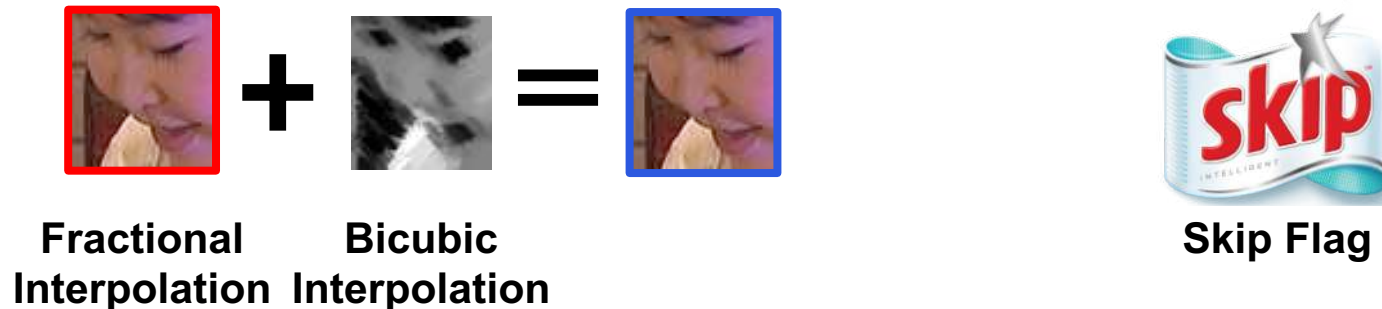
This representation can help **accelerate** super-resolution



# Transfer is Lightweight



Transfer allows SR to run on only **a subset of frames**



The complexity of the transfer is comparable to bicubic interpolation.  
Transfer **N** frames, accelerate by **N**

# Evaluation: Accelerating SRCNN



PartyScene

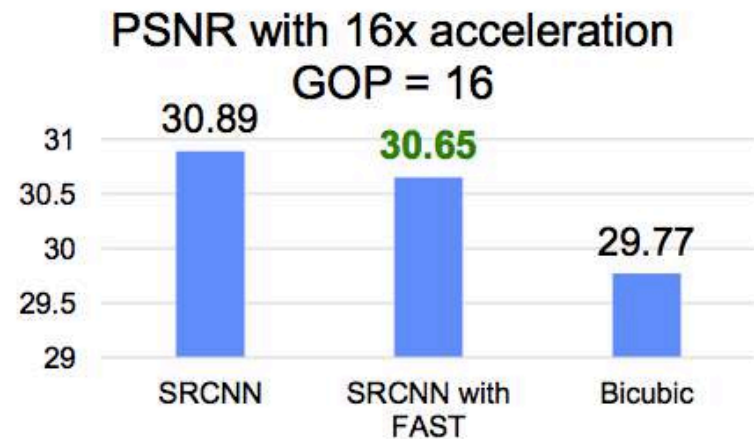
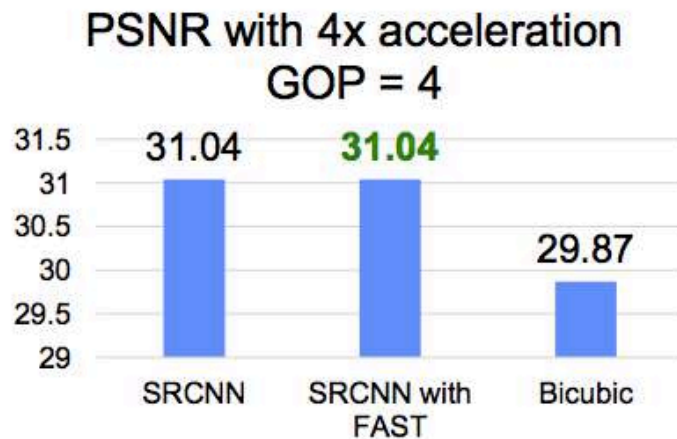


RaceHorse



BasketballPass

**Examples of videos in the test set (20 videos for HEVC development)**



**4 × acceleration with NO PSNR LOSS. 16 × acceleration with 0.2 dB loss of PSNR**

# Visual Evaluation



SRCNN

FAST +  
SRCNN

Bicubic

Look ***beyond*** the DNN accelerator for opportunities to accelerate DNN processing (e.g., structure of data and temporal correlation)

Code released at [www.rle.mit.edu/eems/fast](http://www.rle.mit.edu/eems/fast)

# Summary

- **DNNs are a critical component in the AI revolution**, delivering record breaking accuracy on many important AI tasks for a wide range of applications; however, it comes at the cost of **high computational complexity**
- **Efficient processing of DNNs** is an important area of research with many promising opportunities for innovation at **various levels of hardware design, including algorithm co-design**
- When considering different DNN solutions it is important to **evaluate with the appropriate workload** in term of both input and model, and recognize that they are **evolving rapidly**.
- It's important to consider a **comprehensive set of metrics** when evaluating different DNN solutions: **accuracy, speed, energy, and cost**



# Additional Resources

## Overview Paper

V. Sze, Y.-H. Chen, T.-J. Yang, J. Emer, “*Efficient Processing of Deep Neural Networks: A Tutorial and Survey*,” **Proceedings of the IEEE**, Dec. 2017

***Book Coming Soon!***

More info about **Tutorial on DNN Architectures**

<http://eyeriss.mit.edu/tutorial.html>

MIT Professional Education Course on

**“Designing Efficient Deep Learning Systems”**

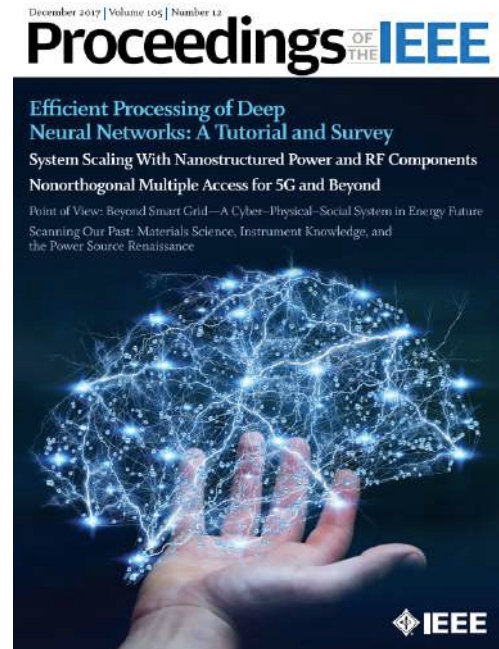
<http://professional-education.mit.edu/deeplearning>

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