

# Single-Sided AC Magnetic Fields For Induction Heating

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**Abstract**—We present simulations and demonstrate experimentally a new concept in winding a planar induction heater. The winding results in minimal ac magnetic field below the plane of the heater, while concentrating the flux above. Ferrites and other types of magnetic shielding are typically not required. The concept of a one-sided ac field can be generalized to other geometries as well.

**Keywords**—induction heating; Halbach; one-sided flux; ac Halbach; single-sided field; induction cooker

## I. INTRODUCTION

Induction heating is used in industrial [2], medical [3, 4], and home consumer [5, 6] applications. One of the key concerns in induction heating is containing the stray magnetic fields; solutions include both active and passive shielding, which are extrinsic to the induction coil design [7-11].

We demonstrate a new winding arrangement based on a Halbach array, which in an ideal form results in a field on only one side of a geometric surface [12, 13]. These surfaces can be general and along with planar designs, cylindrical and spherical surfaces, among others, are possible [14, 15]. Traditionally, these Halbach configurations have been used to generate dc magnetic fields, but we show that ac fields can also be generated with one-sided characteristics.

In this paper, we present both finite element simulation and experimental results for a prototype winding arrangement of a planar induction heater based on a two-dimensional Halbach configuration. By using a Halbach winding configuration, the flux cancelation is achieved implicitly without the use of passive shields such as ferrite plates, conductor plates, or active shielding. In doing so, cost, weight, and size are reduced, along with an improvement in mechanical robustness by not using ferrites.

## II. HALBACH WINDING

Both Halbach [12] and Mallinson [13] independently posited magnetization configurations that elicit one-sided magnetic fluxes. Some of the theory for the ideal cases is derived in [15]; in the ideal case, the field has a sinusoidal variation on the plane of the array, falls off exponentially from the top surface, and is zero below. We can derive the magnetic flux density at a point  $z$  above and  $x$  along the Halbach surface with thickness  $d$  as

$$B = \mu_0 M_0 (1 - e^{-kd}) e^{-kz} \cos kx. \quad (1)$$

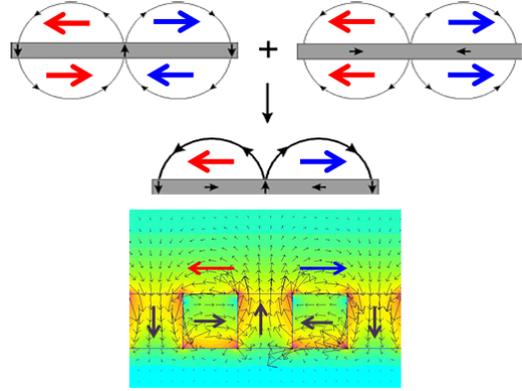


Fig. 1. DC Halbach Array [1]

$k = 2\pi / \lambda$  is the radian reciprocal of the array wavelength and for a wound Halbach array  $M_0 = \alpha k NI$ , where  $NI$  are the amp-turns and  $\alpha$  is a geometric factor.

The faster fall-off in field resulting from a Halbach surface can be advantageous in induction cooking appliances, including wide area, flexible cooking zones [16] because the bottom of the pans are close to the surface so power transfer can be achieved while still minimizing stray fields.

Fig. 1 illustrates the construction of a one-sided dc field using magnetizations from a permanent magnet. It shows how the superposition of an alternating pattern of vertical and

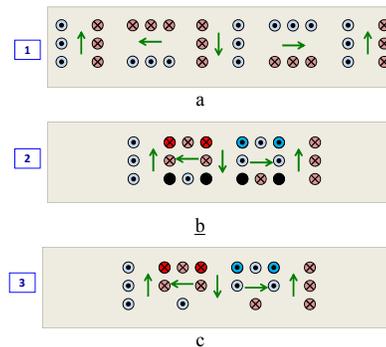


Fig. 2. Compression of a Unit Cell for a Wound Halbach Array

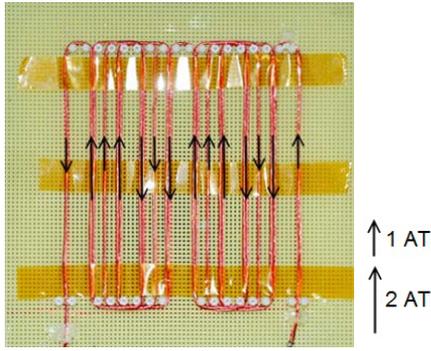


Fig. 3. Two-Dimensional Winding Halbach Approximation. Arrows indicate per unit ampere-turns on the top layer of the winding structure.

horizontal magnetizations combine to produce twice the field on top and none on the bottom. In this case, (1) then refers to the fundamental spatial harmonic of the magnetization pattern.

An example of a wound dc Halbach array can be found in [17]. In Fig. 2a, we approximate each magnetization with a three turn winding. If we compress the windings together as in Fig. 2c, there is a doubling of amp-turns in some of the turns in the top layer, and cancellations on the bottom layer. This arrangement reduces the winding complexity with a decreasing winding density with each layer. Fig. 3 shows how a two-dimensional implementation of the array is wound. A two-dimensional approach means that each layer can be wound independently, which results in a reduction in winding and hence manufacturing complexity.

### III. FINITE ELEMENT SIMULATIONS

We performed finite element simulations for frequency-dependent magnetic induction. In addition, we performed a simulation using a multiphysics model that included heat

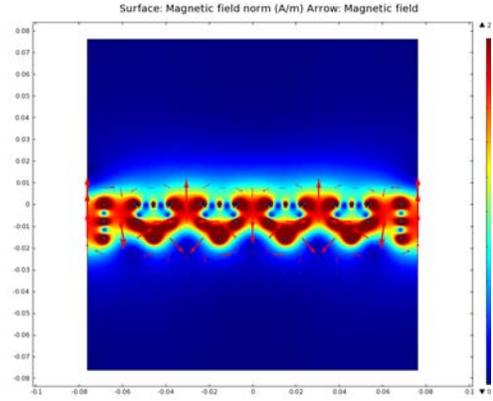


Fig. 5. Field distortion of the Halbach winding array occurs at 500 kHz because of current density distortion from the proximity effect. Litz wire can minimize the effect.

conduction, convection, and radiation.

#### A. Magnetic Field Modeling

We performed simulations at the nominal operating frequency of 500 kHz. By using a thin-wire approximation, skin and proximity effects in the winding can be neglected; this is a valid model for an experiment if the appropriate Litz wire is used. Fig. 4 shows that the additional field from adding a steel target on top of a Halbach winding is negligible. In addition, one observes that in comparison to a quadrupole winding (top layer only), a complete Halbach winding has a significantly higher concentration of magnetic flux above and a field that does not extend as far below.

If we use a solid conductor winding and increase the diameter, frequency, and current, proximity effects begin to dominate and distortion in the magnetic field occurs, resulting in decreased flux above and increased field below; this is

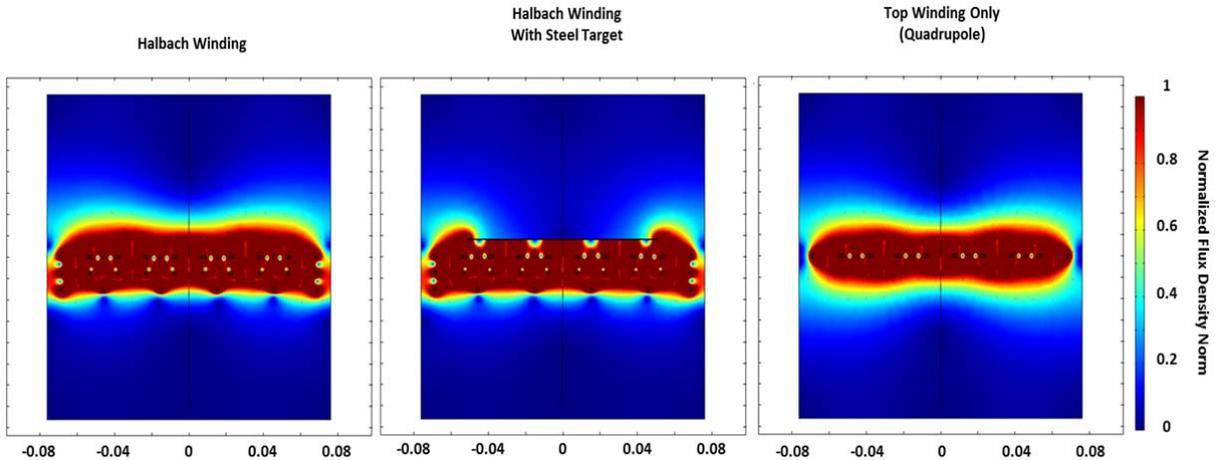


Fig.4. Finite Element Simulations of Magnetic Flux Density

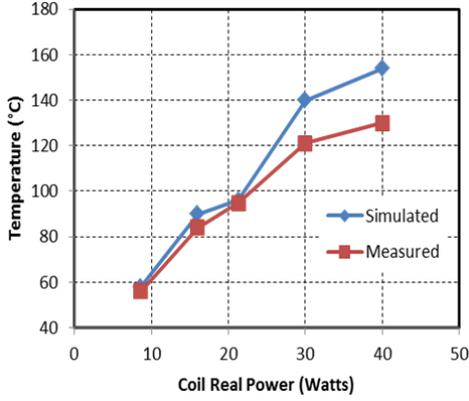


Fig. 6. Multiphysics finite element model includes heat convection, conduction, and radiation, along with magnetic induction.

illustrated in Fig. 5.

### B. Multiphysics Modeling

We performed a multiphysics simulation in Fig. 6 that includes models for heat conduction, convection, and radiation. The effect of resistive heating from the winding was discounted by enforcing a thermally insulating boundary at the surface of the wire. Temperature dependent target resistivity is included as well. The results are given for steady-state temperature and power level. The simulation deviates from measurements at higher temperatures presumably because of regime changes in the convection model.

## IV. EXPERIMENTAL RESULTS AND DISCUSSION

We constructed a prototype Halbach winding array on an FR4 perforated board, which is illustrated in Fig. 7. It consists of three layers, as in Fig. 2. By lap winding the end turns, a significant number of the current segments cancel, hence reducing stray fields at the ends. Thin magnetic steel was used as a target to increase the in-plane thermal time constant, so that transient thermal effects could be observed using an infrared camera. Transient thermal behavior, i.e. step response to power, is useful in determining heating distribution and

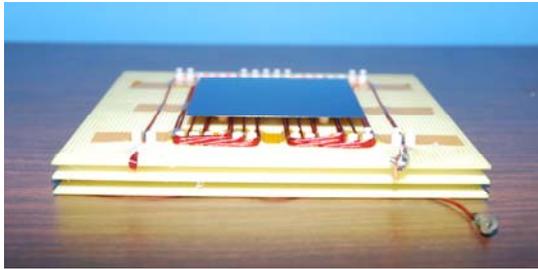


Fig. 7. Induction coil with steel target showing lap winding structure to minimize end-turn fringing field.

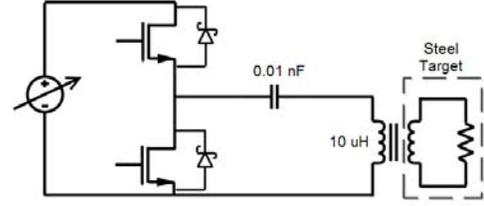


Fig. 8. Half-bridge inverter is used to drive a series resonant circuit.

uniformity. The heating distribution is an indicator of the induced currents and hence magnetic flux distribution at the target. The top surface of the target was coated with high temperature black paint and calibrated to a thermocouple to calculate an emissivity of 0.97, which is needed for infrared temperature measurements.

Table I delineates the parameters relevant to the experiments. The nominal operating frequency was chosen to maximize the ratio of the unloaded to the loaded Q for the particular target. This maximizes the target heating relative to the coil resistive loss.

The induction coil was connected as part of a series

TABLE I. INDUCTION HEATING PARAMETERS

Coil Parameters	
Nominal Operating Frequency	500 kHz
Unloaded Q	78
Front Loaded Q	26
Rear Loaded Q	73
Inductance	8.2 $\mu$ H
Winding Pitch (inches/mm)	0.3/7.6
Layer Spacing	0.3/7.6
Copper Litz Wire	175 strands x 40 ga
Target Parameters	
Material	AISI 1008 Steel
Thickness	10 mil/0.25mm
Dimensions (inches/cm)	4 x 4/10.2 x 10.2
Nominal Relative Permeability	1500
Nominal Resistivity	130 x 10 <sup>-9</sup> $\Omega$ ·m
Skin Depth at 500 kHz	6.6 $\mu$ m
Thermal Conductivity	59.5 W/m·K
Specific Heat	481 J/kg·K
Density	7.87 x 10 <sup>3</sup> kg/m <sup>3</sup>
Coating Emissivity	0.97
Gap to Coil (inches/mm)	3/8" / 9.5

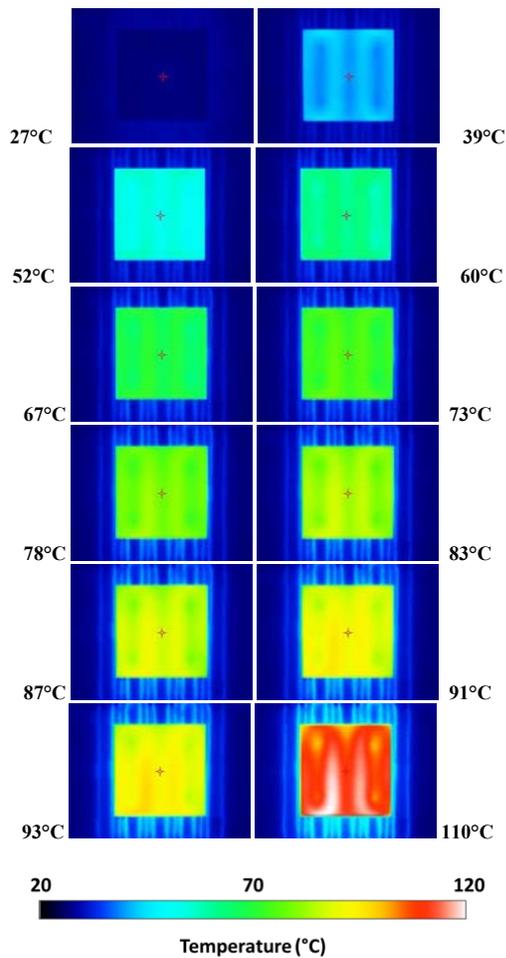


Fig. 9. Time/Temperature Evolution of Target Heating

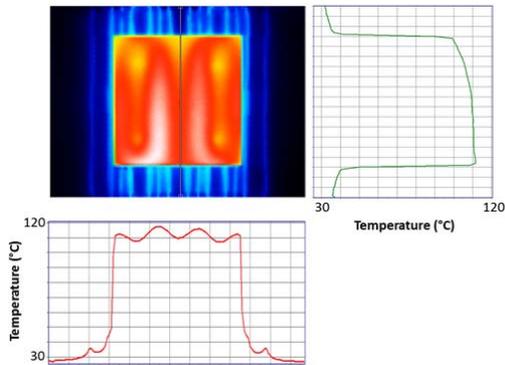


Fig. 10. Temperature profile of target on top of Halbach winding along the lines bisecting the target.

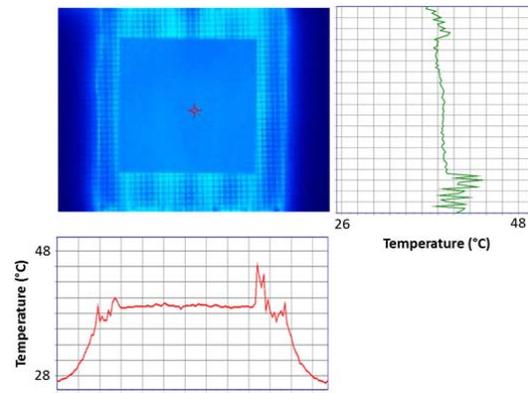


Fig. 11. Temperature profile of steel target on the bottom side of the Halbach induction winding shows negligible inductive heating. Temperature rise is due to the resistive heating in the winding.

The series capacitor is a parallel combination of ceramic capacitors for high current capability.

We used a Fluke TI 20 to image the target heating in the infrared. Fig 9 shows the evolution of heating with a step input in sinusoidal coil current amplitude. This only approximates a step in power because target resistance is a strong function of temperature. There appears to be a small air current from the air conditioning along the top of the target appearing vertically in the figures, which becomes more pronounced at higher temperatures.

From the images, we also extracted the temperature profiles

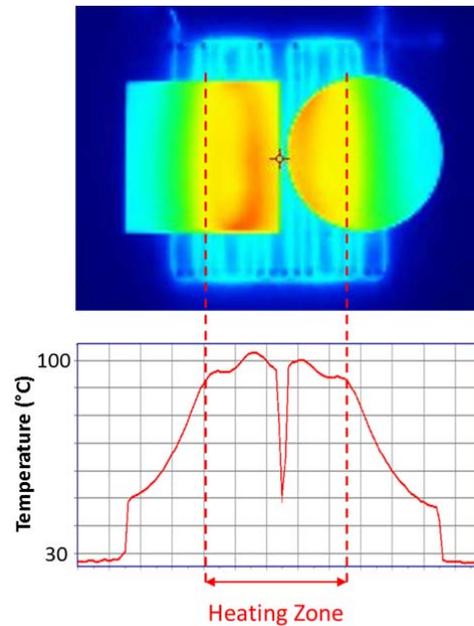


Fig. 12. Heating Zone

resonant circuit to a half-bridge MOSFET inverter in Fig. 8.

along the two bisecting axes of the target. In Fig. 10, the temperature profiles along each direction appear relatively uniform. The temperature profile within the heating zone in the horizontal axis shows a sinusoidal variation, which is what is expected from a thermal low-pass of the intensity of the inductively coupled magnetic flux from a Halbach array.

Fig. 11 is a salient illustration of a single-sided flux. The target is only heated by the resistive losses from the hotter winding. The thermal radiation from the bottom winding is apparent through the perforated FR-4 substrate. No inductive heating pattern is apparent in the temperature profile of the target.

The inductive heating element has a relatively well-defined heating zone, which is illustrated in Fig. 12. This is consistent with the magnetic flux distribution on the target in Fig. 4. Beyond the heating zone, the expected exponential drop-off from heat diffusion is apparent. This shows that edge effects are not that significant in that a relatively sharp boundary is formed for the heating zone, which is also consistent with the simulations shown in Fig. 4. Fig. 12 also serves as a partial illustration and comparison of the heating effects on circular and rectangular targets.

#### V. CONCLUSION

We presented and demonstrated a new concept in winding an induction heater. The winding results in minimal ac magnetic field below the plane of the heater, while concentrating the flux above. Ferrites and other types of magnetic shielding are not required, but may be used if better fringe field containment is desired. The concept of a one-sided field can be generalized to other geometries, some of which have already been developed for applications involving only a dc field. Future work includes more detailed study of the proximity effects on field distortion for lower cost windings materials, edge effects, and the effects of the end windings, as well as scaling up the design to multi-kilowatt levels for induction cooking applications.

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