Introduction

Tools for Practical Source Coding
The primary focus of our work is the analysis and design of building blocks for practical compression systems. We tend to work at a level of abstraction where our parts fit in many applications, but we also sometimes follow through to final applications. To be able to influence practice, we emphasize structured signal transformations and scalar and lattice quantization. Beyond just compression, we are interested in whole communication systems, including channel coding, networking, and congestion control.

Oversampling
Though it is not obvious on the surface, the power of oversampled representations is central to the digitization that surrounds us in this digital age. For scientific processing but also for most communication and storage, acquired signals are quantized to discrete values in the process of analog-to-digital conversion (ADC). ADC is made orders of magnitude cheaper by having very coarse (e.g., one bit) discretization of a highly oversampled version of a signal; it is much cheaper to run fast than to be accurate in analog electronics. The ubiquity of these techniques in audio processing is evidenced by the obscure "1-bit DAC" imprint on CD players, yet the full power of oversampled representations for higher-dimensional signals remains to be exploited.

Nonlinearities
For reasons of both computational complexity and mathematical elegance, linear transformations are central to the theory and practice of signal processing. But there are many nonlinear operations that are not too difficult to analyze or implement that provide very valuable properties. Examples include sorting, as in the Burrows-Wheeler Transform or permutation coding; thresholding, which is prominent in denoising; and pseudolinear integer-to-integer transforms, which are promising for conventional lossy source coding and multiple description coding. We are interested in developing tools based on tractable nonlinearities.

Technology and Pedagogy
The goal in any engineering research should be to aid good engineering, specifically the design of objects and processes for the betterment of the human condition. While we strive to advance technology, at the same time we embrace the additional opportunities that come from being at an educational institution. We make some of our contribution by illuminating topics we find important to non-specialists. And we take the time to work beyond the point of having mathematical proof to also have clear, intuitive, and visual demonstrations.

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Chapter 2. Signal Transformation and Information Representation

1. Generalized Permutation Codes

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Permutation codes are a class of structured vector quantizers with a computationally-simple encoding procedure. We provide an extension that preserves the computational simplicity but yields improved operational rate–distortion performance. The new class of vector quantizers has a codebook comprising several permutation codes as subcodes. Methods for designing good code parameters are given. One method depends on optimizing the rate allocation in a shape–gain vector quantizer with gain-dependent wrapped spherical shape codebook.

Quantized frame expansions are overcomplete representations of signals approximated by some quantizer. This scheme proved to be a very useful tool to combat quantization noise and erasures. Normally, a scalar quantizer is used in the quantization phase. We investigate the use of permutation codes, as a quantizer. We explore consistent reconstructions for the new scheme and provide an algorithm to achieve this type of reconstruction. A variety of necessary and sufficient conditions on the frame for the linear reconstruction to be also consistent are derived. The improvement in end-to-end rate–distortion performance is demonstrated using Matlab.

2. Optimal Quantizer Design for Compressed Sensing Reconstruction

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As compressed sensing (CS) principles gain relevance in real-world applications, it becomes imperative to understand how quantization of measurements affects signal reconstruction. We consider the metric of signal reconstruction fidelity and apply concepts from distributed functional quantization to design optimal scalar quantizers for CS measurements. Optimal in this setting means minimum quantization distortion. We find the best design is the Lloyd-Max quantizers with the point density reweighted by a sensitivity function. Although its exact form is analytically intractable for the problem model specified, the sensitivity can be found easily through Monte Carlo simulation, and importance sampling leads to faster convergence. In the fixed-rate scalar quantizer case, a constant factor improvement in distortion is noted compared to other practical designs. We expect similar or better improvement in the variable-rate case. Interesting extensions via the replica method are being studied.

3. Estimation Bounds in Compressed Sensing

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Multi-sensor receivers are often used for geolocation via time-difference or angle of arrival estimation. We consider compressive sensing networks which use random projections to
undersample sparse data. A novel block-OMP reconstruction algorithm is used to recover the parameters of interest. We also derive Cramer-Rao bounds for both time-difference of arrival (TDOA) and angle of arrival (AoA) cases. The bounds are loose compared to algorithmic results at interesting SNR levels, which is a well-known effect the CRB of nonlinear estimation.

For TDOA, we also consider the case when the delay is discrete. Using a maximum empirical mutual information (MMI) estimator, we show that only partial support recovery is necessary for delay estimation to be successful with overwhelming probability. We provide necessary and sufficient conditions on the scaling of the signal and sparsity dimensions for delay recovery.

### 4. Structural Properties of the Caenorhabditis elegans Neuronal Network

**Sponsor**
National Science Foundation Graduate Research Fellowship Program (NSF GRFP)

**Project Staff**
Lav R. Varshney, Dr. Dmitri B. Chklovskii (Janelia Farm Research Campus, Howard Hughes Medical Institute), Professor Sanjoy K. Mitter, Professor Vivek K Goyal

Neuronal wiring diagrams and analysis of their structural properties can provide insights into the function of nervous systems. Using materials from White et al. and new electron micrographs, we assemble a whole neuronal wiring diagram of hermaphrodite Caenorhabditis elegans. We catalog various statistical and topological properties of the neuronal network and also propose a convenient method for visualization. The C. elegans neuronal network is far from random yet is statistically similar in many respects to other natural networks. We apply spectral analysis to network dynamics and provide a theoretical framework for predicting the propagation of signals in the network in response to sensory or artificial stimulation. These results should help plan experimental investigations of the network and facilitate discovery of principles governing network structure and function.

### 5. A Channel that Dies

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Physical communication systems have a tendency to incur catastrophic failure at random times. The system may run out of energy, terminal equipment might fail, or the physical communication channel might be destroyed. All such cases may be modeled as failure of the communication channel. As such, it is of interest to study information theoretic limits on communicating over channels that die at random times. This work studies one such channel model and provides some positive and negative results.

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Previous work established the ability of digital post-processing algorithms to effectively mitigate the effect of timing noise, or “jitter,” on samples generated by analog-to-digital converters (ADCs). Towards the practical application of this idea, a nonlinear Polynomial Least Squares estimator was developed that could process samples in real time, with minimal additional computational overhead compared to a linear post-processor. Several variations on this estimator were developed and evaluated against both linear and approximate Bayes Least Squares estimators to determine their efficacy. The correlation between different higher-order terms of the estimator and the data was investigated and used to improve the scalability of the estimator. These algorithms were simulated extensively using MATLAB.

7. Augmenting Accelerated Parallel MR Image Reconstruction using a Sparsity Prior

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Accelerated k-space acquisitions taken in parallel using multiple coils can be combined to form a full-FOV k-space reconstruction using GRAPPA, a technique that uses additional calibration lines acquired near the center of the image to guide reconstruction of the missing k-space lines across all the coil images. This technique is limited by the effective SNR reduction caused by the coil geometry and the reduced scan time. A sparsity prior is a reasonable assumption for natural images, including those generated by MRI, and common techniques like Compressed Sensing (CS) can be used to reconcile observations with this prior information. This work aims to incorporate the sparsity prior into the GRAPPA algorithm, or reformulate accelerated parallel MRI reconstruction to account for sparsity. Recent efforts, such as L1 SPIR-iT, have been evaluated to support the promise of CS-augmented reconstruction, and another approach to combine the objectives into a single CS-type optimization problem has been devised.

**Publications**

**Journal Articles, Published**


**Journal Articles, Accepted**


**Journal Articles, Submitted**


**Meeting Papers, Presented**

Chapter 2. Signal Transformation and Information Representation

Meeting Papers, Published


Meeting Papers, Submitted
