

Timing performance of 30-nm-wide superconducting nanowire avalanche photodetectors

F. Najafi,^{1,a)} F. Marsili,^{1,a)} E. Dauler,² R. J. Molnar,² and K. K. Berggren^{1,b)}

¹Department of Electrical Engineering and Computer Science, Massachusetts Institute of Technology, 77 Massachusetts Avenue, Cambridge, Massachusetts 02139, USA

²Lincoln Laboratory, Massachusetts Institute of Technology, 244 Wood St., Lexington, Massachusetts 02420, USA

(Received 7 December 2011; accepted 19 March 2012; published online 12 April 2012)

We investigated the timing jitter of superconducting nanowire avalanche photodetectors (SNAPs, also referred to as cascade-switching superconducting single-photon detectors) based on 30-nm-wide nanowires. At bias currents (I_B) near the switching current, SNAPs showed sub-35-ps FWHM Gaussian jitter similar to standard 100-nm-wide superconducting nanowire single-photon detectors. At lower values of I_B , the instrument response function (IRF) of the detectors became wider, more asymmetric, and shifted to longer time delays. We could reproduce the experimentally observed IRF time-shift in simulations based on an electrothermal model and explain the effect with a simple physical picture. © 2012 American Institute of Physics. [<http://dx.doi.org/10.1063/1.3703588>]

Superconducting nanowire avalanche photodetectors (SNAPs, also referred to as cascade-switching superconducting single-photon detectors)¹ are based on a parallel-nanowire architecture (Figure 1(a)) that allows single-photon counting with higher signal-to-noise ratio (up to a factor of ~ 4 higher²) than superconducting nanowire single-photon detectors (SNSPDs)³ with the same nanowire width. Figure 1(b) shows the equivalent electrical circuit of a SNAP with 4 parallel sections (or 4-SNAP). All of the sections have nominally the same kinetic inductance (L_0) and are connected in series with an inductor (L_S) and in parallel with a readout resistor (R_{load}). If the bias current (I_B) of a N -SNAP is higher than the avalanche threshold current (I_{AV}) of the device, when one section switches to the normal state after absorbing a photon (initiating section), it diverts its current to the remaining $N-1$ sections (secondary sections), driving them normal (we call this process an avalanche). Therefore, a current $\sim N$ times higher than the current through an individual section is diverted to the read-out.²

The physical origin of the photodetection delay and timing jitter of detectors based on superconducting nanowires remains unclear over 10 years after the introduction of these detectors. Zhang *et al.*⁴ studied the photodetection delay of 130-nm-wide nanowires as a function of power and hypothesized that the observed 70-ps decrease of photodetection delay between the single-photon and multi-photon regimes might be due to reduced gap suppression time in the multi-photon regime. O'Connor *et al.*⁵ studied the local dependence of the photodetection delay and timing jitter (190–205 ps) along 100-nm-wide nanowires and concluded that narrower nanowire sections have lower delay and jitter. However, significantly lower jitter values (~ 30 ps (Ref. 6) to ~ 60 ps (Ref. 7)) have been repeatedly

reported for 100-nm-wide nanowires. Another study of jitter as a function of wavelength⁸ found no dependence in the range 1–2 μm . Along with the dependence on nanowire width, incident optical power, and photon energy, bias-current-dependence may provide decisive insight into the physical origin of photodetection delay and jitter. However, jitter measurements as a function of I_B , which have not been reported so far, have been hampered by decreasing signal-to-noise ratio (SNR, which makes the jitter induced by the electrical noise of the set-up dominant over the jitter of the device) and exponentially decreasing detection efficiency (which makes the acquisition time of the instrument response function significantly longer⁹) with decreasing I_B . We recently found a way to overcome these obstacles: We employed SNAPs to read out 20- and 30-nm-wide nanowires.² The detection efficiency at 1550 nm wavelength was 17–20% and showed only a weak bias-current-dependence ($< 5\%$ relative variation) in the bias range $I_{AV} < I_B < I_{SW}$, where I_{SW} is the SNAP switching current.² Taking advantage of the possibility of efficiently detecting single photons over the entire SNAP bias range with high SNR (> 3 , as defined in Ref. 2), we studied the timing performance of 30-nm-wide 2-, 3-, and 4-SNAPs as a function of the bias current. Our results suggest that the gap suppression time, which would be expected to be strongly dependent on the bias current, has little if any effect on the most-likely photodetection delay when the detectors are operating in single-photon regime.

We measured the instrument response function (IRF) of 10 devices with active areas ranging from 0.8 to 2.1 μm^2 (see Ref. 2 for details on the fabrication process). Our main finding is that, although at bias currents near I_{SW} , the IRF of SNAPs had a Gaussian shape with sub-35-ps full width at half maximum (FWHM), at lower values of I_B the IRF became wider, more asymmetric, and shifted to longer time delays. We could simulate the experimentally observed IRF time-shift (but not the observed asymmetry) by using an electrothermal model.¹⁰

^{a)}F. Najafi and F. Marsili contributed equally to this work.

^{b)}Author to whom correspondence should be addressed. Electronic mail: berggren@mit.edu.

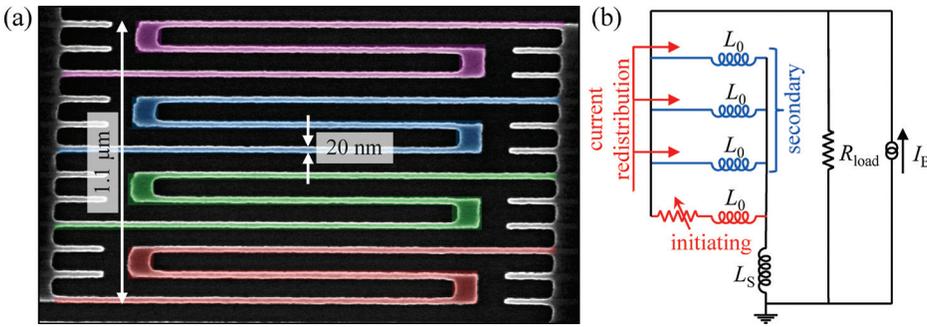


FIG. 1. (a) Colorized scanning electron microscope (SEM) image of a 4-SNAP resist (hydrogen silsesquioxane) mask on NbN with each section colored differently. (b) Equivalent electrical circuit of a 4-SNAP. The arrows pointing at the secondary sections represent the current redistributed from the initiating section to the secondary sections after the initiating section switches to the normal state.

To illuminate the detectors, we used a mode-locked, sub-ps-pulse-width laser emitting at ~ 1550 nm wavelength with 77 MHz repetition rate. The laser output was split into two single-mode optical fibers that we coupled to the detector under test and to a low-jitter fast photodiode (pulse rise time < 35 ps). The signals from the SNAP and from the fast photodiode were sent to a 6-GHz-bandwidth, 40-GSample/s oscilloscope, which we used to measure the IRF. We verified that the SNAPs were operating in the single-photon regime by setting the power level of the incident light within a range in which the detector photoresponse counts increased linearly with incident power (as in Ref. 2).

Figure 2(a) schematically represents the moments of the photodetection process most relevant to our discussion: (1) t_0 : A sub-ps laser pulse is emitted; (2) t_{FPD} : The rising edge of the photoresponse pulse of the fast photodiode crosses the oscilloscope trigger level set to 50% of the average pulse peak value; (3) t_{HSN} : A photon is absorbed in the nanowire and it starts a resistive state formation process (hotspot nucleation, HSN); (4) t_{ξ} : The first resistive slab of length ξ (the coherence length of NbN (Ref. 10)) is formed across the width of the initiating section; (5) t_{SNAP} : The rising edge of the SNAP photoresponse pulse crosses the oscilloscope trigger level set to 50% of the average pulse peak value (which depends on I_B); and (6) $t_{95\%}$: The SNAP photoresponse pulse crosses the oscilloscope trigger level set to 95% of the average pulse peak value. We defined the detector IRF as the histogram of the time delay t_D measured on the oscilloscope between the rising edges of the fast photodiode pulse (t_{FPD}) and of the SNAP pulse (t_{SNAP}), i.e., $t_D = t_{SNAP} - t_{FPD}$. The IRF histograms were calculated by using $\sim 6 \cdot 10^4$ time delay samples. The absolute value of t_D was set by the propagation times of the signals (laser pulse, fast-photodiode pulse, and SNAP pulse) through the optical and electrical paths of our set up, as illustrated by arrows in Figure 2(a). These I_B -independent delays were irrelevant to the problem. Therefore, for convenience, we added an offset¹¹ so that $t_D = 0$ s at the maximum of the IRF when the device under test was biased at $I_B = I_{SW}$.

Figure 2(b) shows the IRF of a 2-SNAP (normalized by its maximum value) at different bias currents. We observed two current-dependent effects in the IRF: (1) As I_B was increased, the time delay corresponding to the maximum of the IRF (we called this time delay “maximum-likelihood delay,” MLD) shifted towards shorter time delays and (2) as I_B was decreased, the IRF progressively transitioned from a Gaussian shape (when the detector was biased close to I_{SW})

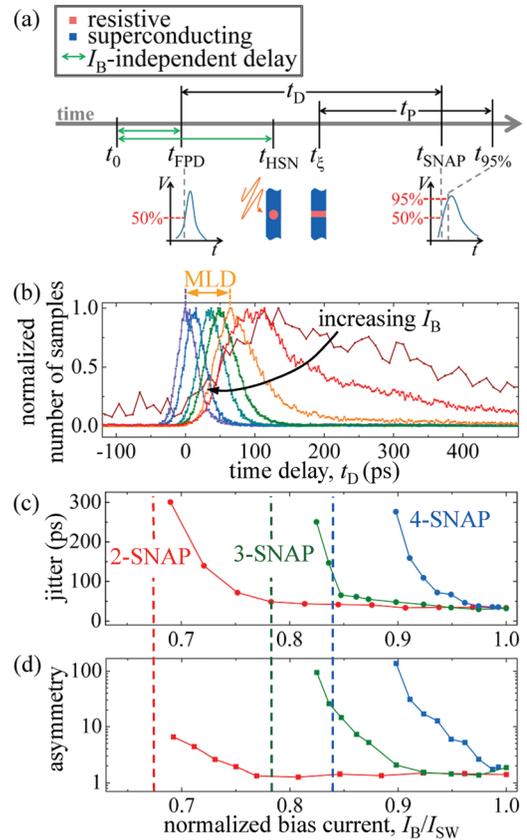


FIG. 2. (a) Schematic representation of instances during the photodetection process. A photon from an optical pulse emitted at t_0 is absorbed in the initiating section (t_{HSN}), generating a resistive slab along the width of the nanowire (t_{ξ}). After the avalanche, the SNAP bias current is diverted into the load, and an output voltage pulse forms across the load resistor. The arrival of this pulse can be detected once the rising edge of the SNAP pulse crosses the trigger level of the oscilloscope (t_{SNAP}). We measured the time delay between t_{SNAP} and a reference t_{FPD} , the instant at which the rising edge of the photodetection signal from a fast photodiode crossed the trigger level of the oscilloscope. The voltage (V) vs time (t) curves represent the oscilloscope traces of the fast photodiode (left hand side) and SNAP (right hand side) pulses. The dashed lines represent the 50% and 95% thresholds. (b) IRF (normalized by the maximum of each trace) of a 30-nm-wide 2-SNAP at bias currents: $I_B/I_{SW} = 1, 0.93, 0.85, 0.78, 0.73, 0.69,$ and 0.64 . The curved arrow indicates the direction of increasing I_B . The double-pointed arrow indicates the MLD at $I_B/I_{SW} = 0.73$. The MLD of the IRF was set to 0 s at $I_B/I_{SW} = 1$. (c) Jitter of a 2-, 3-, and 4-SNAP based on 30-nm-wide nanowires as a function of the normalized bias current (I_B/I_{SW}). The switching currents of the 2-, 3-, and 4-SNAP were $13.2 \mu\text{A}$, $17.9 \mu\text{A}$, and $27.8 \mu\text{A}$, respectively. The vertical dashed lines indicate the avalanche currents of the SNAPs.² The data for the jitter of 3- and 4-SNAPs biased below I_{AV} are not shown (see Ref. 12) as the devices were not operating as single-photon detectors (they were instead operating in arm-trigger regime as described in Ref. 2). (d) IRF asymmetry vs. I_B/I_{SW} for the same devices shown in panel (c).

to a broader and asymmetric shape, exhibiting a decaying tail which extended for several hundreds of picoseconds beyond the MLD.

Figure 2(c) shows the jitter of 2-, 3-, and 4-SNAPs, defined as the FWHM of the IRF, as a function of I_B/I_{SW} . The jitter of SNAPs showed a weak dependence on the bias current for I_B close to I_{SW} (e.g., for a 2-SNAP, the jitter increased from 35 ps at $I_B=0.97I_{SW}$ to 41 ps at $I_B=0.88I_{SW}$) but rapidly increased as I_B approached I_{AV} (by ~ 100 ps for a decrease in I_B of $0.1I_{SW}$). I_{AV} was determined from detection efficiency measurements, as reported in Ref. 2. We note that for I_B approaching I_{SW} , SNAPs showed the same jitter as standard SNSPDs (Ref. 6) (~ 33 ps), in contrast to previous reports of larger timing jitter of SNAPs.^{13,14}

Figure 2(d) shows the IRF asymmetry, defined as the ratio between the length of the IRF tails (experimentally defined as the time between 90% and 10% of the IRF maximum) after and before the MLD. Like the jitter, the asymmetry of SNAPs showed a weak dependence on the bias current at high I_B but rapidly increased as I_B approached I_{AV} .

The shift of the MLD to shorter delays with increasing I_B can be explained by considering the dependence of the electrothermal dynamics of the device on the bias current. Using the electrothermal model described in Ref. 10, we simulated the time evolution of the current diverted from the SNAP to the read out (I_{out}) after a HSN event occurred in the initiating section. Our model did not describe the formation and expansion of the photon-induced hotspot,^{15,16} so in our simulations, the absorption of a photon resulted in the immediate formation of a resistive ξ -long slab (ξ -slab), i.e., $t_\xi = t_{HSN}$.

We repeated the simulation at different values of I_B . Figure 3(a) shows the simulated current pulses from a 2-SNAP. We defined the detector peak delay t_P as $t_P = t_{95\%} - t_\xi$ and set t_ξ to 0 s in our simulations (see Ref. 12 for details on the choice of $t_{95\%}$ as reference). The observed increase of t_P with decreasing I_B can be easily understood. After the avalanche, the resistance $R(t)$ of the SNAP grows with time¹⁰ at a rate that monotonically increases with the dissipated power proportional to $R(t) \cdot I_B$ (Ref. 2) (Joule heating). At lower bias

currents, the dissipated power is smaller, resulting in a slower increase of $R(t)$. Hence, it takes longer for the diverted current I_{out} to reach its peak value. Figure 3(b) shows t_P (simulation) and the MLD (experiment) of a 2-SNAP as a function of I_B . As t_P and the MLD show a similar dependence on I_B , and recalling that our choice of origin of the MLD was arbitrary, we conclude that the MLD differs at most by a current-independent offset from t_P .

The absolute values of the MLD and of t_P were defined with respect to different moments in time (t_{FPD} for the MLD and t_ξ for t_P) and by using different thresholds on the SNAP photoresponse pulse (50% of the average pulse peak value for the MLD and 95% of the average pulse peak value for t_P , see Ref. 12). However, the current dependencies of the values of the MLD and t_P were similar across the entire bias-current range ($\sim 30\%$ of I_{SW}) of single-photon operation. From the comparison between the experimentally measured MLD values and the calculated t_P values, we conclude that, when neglecting the effect of jitter, the MLD dependence on current can be entirely accounted for by the bias dependence of the peak delay t_P . Therefore, time difference $t_\xi - t_{FPD}$ does not significantly contribute to the bias dependence of the MLD. Since the time difference $t_{HSN} - t_{FPD}$ does not depend on I_B by definition,¹⁷ we can conclude that $t_\xi - t_{HSN}$ does not appreciably affect the bias dependence of the MLD either. Therefore, the gap suppression time,⁴ which is known to be current-dependent,¹⁸ has negligible influence on the resistive-slab creation time, i.e., the time difference $t_\xi - t_{HSN}$.

Our simulations indicate that the increase of t_P with decreasing I_B may not be unique to the SNAP operation. We simulated the operation of a SNSPD after a HSN event for different bias currents (see Ref. 12) and found that t_P increases from 76 ps at $I_B = I_{SW}$ to 127 ps at $I_B = 0.64I_{SW}$. The physical process responsible for the abrupt increase in the width and asymmetry of the IRF of SNAPs as I_B approached I_{AV} remains unexplained. The timing jitter may be related to statistical variations occurring within the resistive slab creation time (between t_{HSN} and t_ξ), while the increase in the asymmetry with decreasing bias current may be due to the increase in the time required by the current

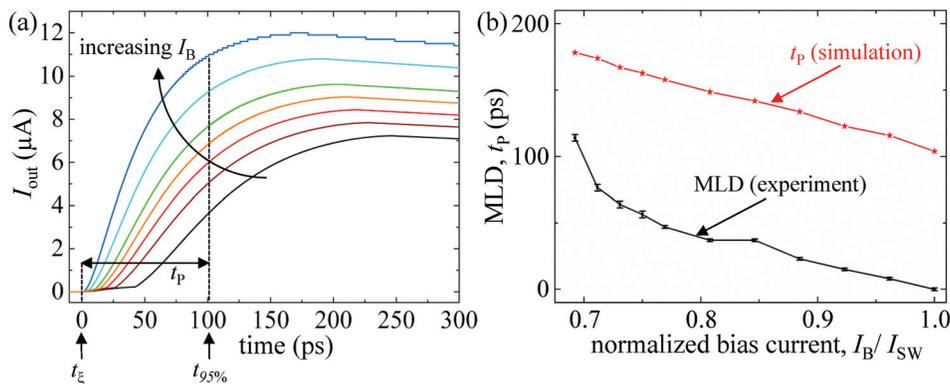


FIG. 3. (a) Simulated time evolution of the current diverted to the read out resistor ($R_{load} = 50 \Omega$) by a 2-SNAP after a resistive ξ -slab is formed in the initiating section (at time $t_\xi = 0$ s) for $I_B/I_{SW} = 0.96, 0.87, 0.81, 0.77, 0.73, 0.70$, and 0.66 . The kinetic inductance of each section of the 2-SNAP was $L_0 = 13$ nH and the series inductor was $L_S = 130$ nH, corresponding to the device of Figure 2(b). Arrows indicate the time at which the resistive ξ -slab is formed (t_ξ); the time at which I_{out} reaches 95% of its maximum ($t_{95\%}$) for $I_B/I_{SW} = 0.96$; the detector peak time for $I_B/I_{SW} = 0.96$ (t_P); and the direction of increasing I_B . (b) Experimental MLD vs I_B (squares) and simulated t_P vs I_B (stars) for the 2-SNAP of Figure 2(b). The error on the MLD values was assumed to be twice the bin size of the IRF histograms. The value of the MLD for the highest I_B was set to 0 s.

redistributed from the initiating section to suppress the superconducting gap in the secondary sections.

The central result of this paper is the experimental observation that as the bias current of SNAPs was decreased from the device switching current, the device IRF shifted to longer time delays and became more broad and asymmetric. While we were able to develop a model of the IRF time shift that closely described the experimental data, we could not explain the change in shape of the IRF as the bias current was varied.

The authors thank Andrew Kerman, Hyunil Byun, James Daley, Mark Mondol, and Professor Rajeev Ram for technical support. Detector fabrication and modeling was supported by the Center for Excitonics (Award # DE-SC0001088). Measurements and work at MIT Lincoln Laboratory were sponsored by the United States Air Force under Air Force Contract No. FA8721-05-C-0002. Opinions, interpretations, recommendations, and conclusions are those of the authors and are not necessarily endorsed by the United States Government. This work was completed while Professor K. K. Berggren was on sabbatical at Delft University of Technology, and supported by the Netherlands Organization for Scientific Research.

¹M. Ejmaes, R. Cristiano, O. Quaranta, S. Pagano, A. Gaggero, F. Mattioli, R. Leoni, B. Voronov, and G. Gol'tsman, *Appl. Phys. Lett.* **91**(26), 262509 (2007).

²F. Marsili, F. Najafi, E. Dauler, F. Bellei, X. L. Hu, M. Csete, R. J. Molnar, and K. K. Berggren, *Nano Lett.* **11**(5), 2048–2053 (2011).

³G. N. Gol'tsman, O. Okunev, G. Chulkova, A. Lipatov, A. Semenov, K. Smirnov, B. Voronov, A. Dzardanov, C. Williams, and R. Sobolewski, *Appl. Phys. Lett.* **79**(6), 705 (2001).

⁴J. Zhang, W. Słysz, A. Pearlman, A. Verevkin, R. Sobolewski, O. Okunev, G. Chulkova, and G. Gol'tsman, *Phys. Rev. B* **67**(13), 132508 (2003).

⁵J. A. O'Connor, M. G. Tanner, C. M. Natarajan, G. S. Buller, R. J. Warburton, S. Miki, Z. Wang, S. W. Nam, and R. H. Hadfield, *Appl. Phys. Lett.* **98**(20), 201116 (2011).

⁶E. A. Dauler, B. S. Robinson, A. J. Kerman, J. K. W. Yang, K. M. Rosfjord, V. Anant, B. Voronov, G. Gol'tsman, and K. K. Berggren, *IEEE Trans. Appl. Supercond.* **17**(2), 279–284 (2007).

⁷H. Takesue, S. W. Nam, Q. Zhang, R. H. Hadfield, T. Honjo, K. Tamaki, and Y. Yamamoto, *Nat. Photonics* **1**(6), 343–348 (2007).

⁸M. J. Stevens, R. H. Hadfield, T. Gerrits, T. S. Clement, R. P. Mirin, and S. W. Nam, *J. Mod. Opt.* **56**(2–3), 358–363 (2009).

⁹As the standard deviation of the number of events in a bin of a histogram is proportional to the square root of the total number of events in the histogram, a large number of photodetection delay samples have to be acquired in order to precisely characterize the timing performance of a detector. The time required to acquire a certain number of time delay samples increases with decreasing detection efficiency of the detector.

¹⁰F. Marsili, F. Najafi, C. Herder, and K. K. Berggren, *Appl. Phys. Lett.* **98**(9), 093507 (2011).

¹¹This offset ensures that the time delay corresponding to the maximum of the IRF is non-negative, while neglecting the effect of the lengths of the electrical and optical paths (mainly RF cables and optical fibers).

¹²See supplementary material at <http://dx.doi.org/10.1063/1.3703588> for IRF of SNAPs in arm-trigger regime, discussion of our definition of the MLD and of t_P , and bias-dependence of t_P for a SNSPD.

¹³M. Ejmaes, A. Casaburi, R. Cristiano, O. Quaranta, S. Marchetti, N. Martucciello, S. Pagano, A. Gaggero, F. Mattioli, R. Leoni, P. Cavalier, and J. C. Villégier, *Appl. Phys. Lett.* **95**(13), 132503 (2009).

¹⁴We attributed the discrepancy between our results and those of Ref. 13 to the fact that the data reported in Ref. 13 were obtained: (1) with 5-SNAPs, which we also studied without observing avalanche regime operation; (2) with 60-ps-wide laser pulses, resulting in a higher set-up jitter than in our measurements; and (3) by biasing the devices further away from I_{SW} than in our experiment.

¹⁵A. D. Semenov, G. N. Gol'tsman, and A. A. Korneev, *Physica C* **351**(4), 349–356 (2001).

¹⁶A. Semenov, A. Engel, H. W. Hübers, K. Il'in, and M. Siegel, *Eur. Phys. J. B* **47**(4), 495–501 (2005).

¹⁷The time difference $t_{HSN} - t_{FPD}$ was set by the propagation times of the signals through the optical and electrical paths of our set-up (see Figure 2(a)).

¹⁸M. Tinkham, *Introduction to Superconductivity* (McGraw-Hill, New York, 1996), Chap. XI.

Timing performance of 30-nm-wide superconducting nanowire avalanche photodetectors: Supplementary Material

F. Najafi^{1†}, F. Marsili^{1†}, E. Dauler², R. J. Molnar², K. K. Berggren^{1‡}

¹ *Department of Electrical Engineering and Computer Science, Massachusetts Institute of Technology, 77 Massachusetts Avenue, Cambridge, Massachusetts 02139, USA*

² *Lincoln Laboratory, Massachusetts Institute of Technology, 244 Wood St., Lexington, Massachusetts 02420, USA*

[†] *these authors contributed equally.*

[‡] *corresponding author: berggren@mit.edu.*

Table of Contents

Instrument response function of superconducting nanowire avalanche photodetectors in arm-trigger regime	2
Discussion of our definition of the maximum-likelihood delay and the peak delay	3
Bias-dependence of t_p for a superconducting nanowire single-photon detector	5
References.....	5

Instrument response function of superconducting nanowire avalanche photodetectors in arm-trigger regime

When biased below the avalanche current (I_{AV}), superconducting nanowire avalanche photodetectors with 3 and 4 parallel nanowires (3- and 4-SNAPs) operated in arm-trigger regime¹. In this regime the devices did not operate as single-photon detectors because more than one hotspot nucleation (HSN) event was necessary to trigger a detector pulse (2 HSN events for 3-SNAPs and 2 or 3 HSN events, depending on the bias current, for 4-SNAPs). Therefore, as the bias current (I_B) was decreased below I_{AV} , the devices transitioned from operating as 3-SNAPs (4-SNAPs) biased slightly above I_{AV} to operating as pseudo 2-SNAP (pseudo 3- or 2-SNAPs, depending on the bias current) biased close to the switching current (I_{SW}).

Figure SM 1a shows the instrument response function (IRF) of a 3-SNAP for I_B ranging from I_{SW} to $0.52I_{SW}$. The IRF became wider and more asymmetric as I_B was decreased from I_{SW} to $\sim 0.8I_{SW}$. For I_B slightly below $\sim 0.8I_{SW}$, the IRF abruptly changed shape and became approximately as narrow and symmetric as the IRF measured for $I_B \sim I_{SW}$. As I_B was decreased further, the IRF became again wider and more asymmetric. Figure SM 1b and c show a quantitative characterization of the shape of the IRF of 3- and 4-SNAPs in terms of its width (jitter) and asymmetry. The abrupt changes in the shape of the IRF as I_B was decreased can be explained with the arm-trigger-regime model, as discussed in Ref.¹.

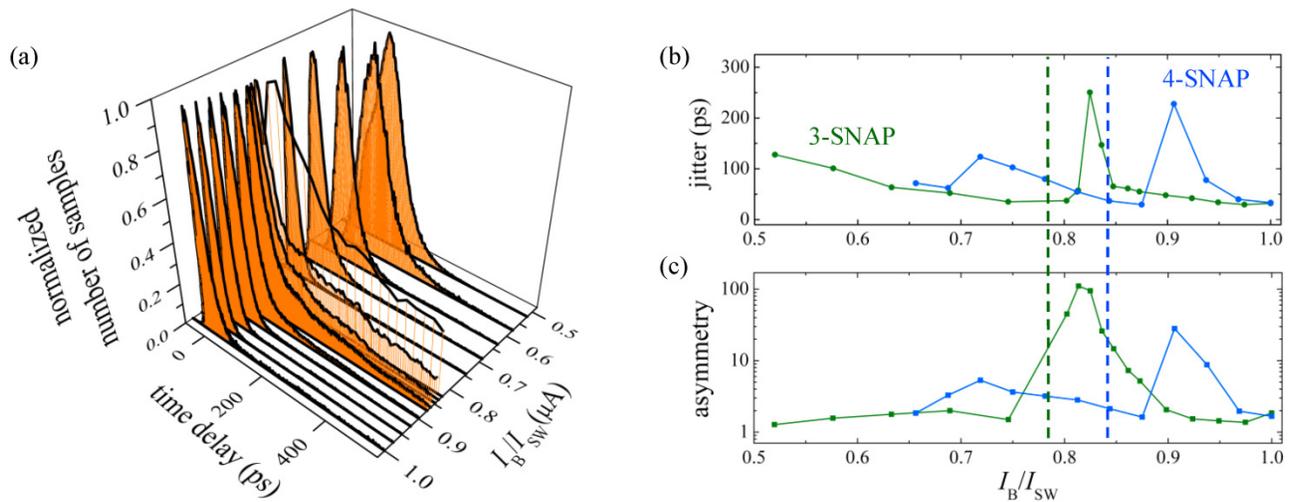


Figure SM 1. **a.** IRF (normalized by the maximum of each trace) of a 30-nm-wide 3-SNAP for I_B ranging from I_{SW} to $0.52I_{SW}$. **b, c.** Jitter (b, defined as the FWHM of the IRF) and IRF asymmetry (c) of a 30-nm-wide 3-SNAP (green, $I_{SW} = 17.9 \mu A$) and 4-SNAP (blue, $I_{SW} = 25.6 \mu A$). The IRF asymmetry was defined as the ratio between the IRF tails (experimentally defined as the time between 90% and 10% of the IRF maximum) before and after the maximum-likelihood delay.

Discussion of our definition of the maximum-likelihood delay and the peak delay

We adopted t_{SNAP} as a reference to measure the maximum-likelihood delay (MLD) to maximize the count rate (and then minimize the acquisition time) and to minimize the counts due to the electrical noise when measuring the IRF (“false counts”, see Ref. ¹).

We used low-noise 3-GHz-bandwidth amplifiers to read out the SNAPs. Therefore the rise time ² of the measured SNAP photoresponse pulse was limited by the bandwidth of our amplifiers. Figure SM 2 shows the measured averaged voltage pulse of a 2-SNAP at different bias currents. Due to the bandwidth limitation, we observed a bias-independent delay (~ 305 ps; see inset of **Error! Reference source not found.**) between the times at which the rising edge of the SNAP photoresponse pulse reached 50% and 95% of the peak value (t_{SNAP} and $t_{95\%}$). This constant offset between t_{SNAP} and $t_{95\%}$ allowed us to measure the current-dependent behavior of $t_{95\%}$ by measuring the current-dependent behavior of t_{SNAP} .

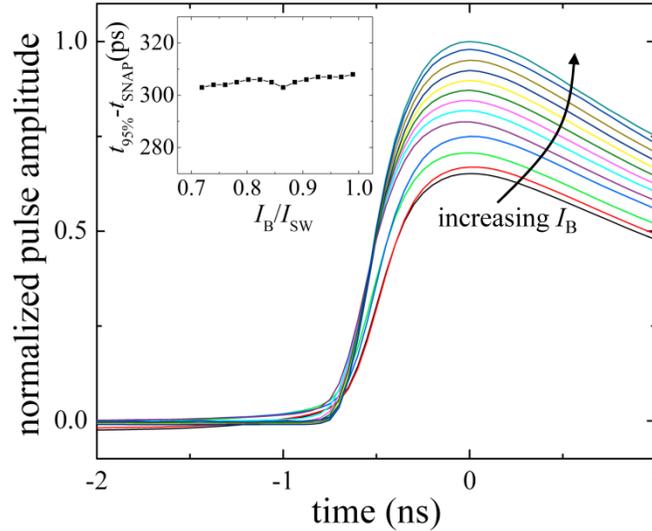


Figure SM 2. Measured voltage pulse (averaged over ~ 5000 traces; normalized to the pulse amplitude at $I_B=0.99I_{\text{SW}}$) of a 30-nm-wide 2-SNAP for I_B ranging from $0.99I_{\text{SW}}$ to $0.72I_{\text{SW}}$ by steps of $\sim 0.02I_{\text{SW}}$. The time at which the pulse reached its maximum value was set to 0 s. **inset.** Time delay between the 95%-of-maximum ($t_{95\%}$) and 50%-of-maximum transition (at t_{SNAP}) of the rising edge of the voltage pulse as a function of normalized bias current I_B/I_{SW} . The maximum variation of $t_{95\%}-t_{\text{SNAP}}$ for I_B ranging from $0.99I_{\text{SW}}$ to $0.72I_{\text{SW}}$ was 5ps.

Figure SM 3a shows the bias dependence of the MLD (experiment, black curve) and of the detector peak delay t_p (simulation, in color) extracted from the simulated SNAP pulses shown in Figure 3a by using different thresholds on the SNAP pulse as references: t_{max} (red curve), the instant at which the SNAP photoresponse pulse reaches its maximum; $t_{95\%}$ (orange curve), the instant at which the rising edge of the SNAP photoresponse pulse reaches 95% of the pulse peak value; and t_{SNAP} (green curve), the instant at which the rising edge of the SNAP photoresponse pulse reaches 50% of the pulse

peak value. Changing the reference threshold on the SNAP pulse did not significantly affect the bias dependence of t_p and then our conclusions.

We chose $t_{95\%}$ over t_{\max} because the pulses were flat around their maximum, so choosing t_{\max} as a time reference to calculate t_p introduced an uncertainty on the value of t_p of the order of tens of ps.

We chose $t_{95\%}$ over t_{SNAP} because, due to the limited bandwidth of our amplifiers ($\sim 3\text{GHz}$), the experimental rise time of the SNAP pulses ($\sim 300\text{ps}$, see Figure SM 2) was significantly larger than the rise time of the simulated pulses ($\sim 100\text{-}150\text{ps}$) shown in Figure 3a, so we expected the low-passed experimental pulses to be less distorted close to the slopeless maximum of the pulse than at 50% of the maximum. To further support our choice, we numerically filtered the simulated pulses shown in Figure 3a by using a low-pass filter with a 3-dB-cut-off frequency of 3 GHz and extracted $t_{95\%}$ and t_{SNAP} from the filtered pulses. Figure SM 3b shows the bias-dependence of $t_{95\%}$ and t_{SNAP} of the pulses shown in Figure 3a and of the filtered pulses. We added a different offset to each curve so that $t_{95\%}$ and t_{SNAP} would be zero at $I_B = I_{\text{SW}}$. While t_{SNAP} of the filtered pulses differed from t_{SNAP} of the pulses shown in Figure 3a by 13 ± 7 ps, $t_{95\%}$ of the filtered pulses differed from $t_{95\%}$ of the pulses shown in Figure 3a by 4 ± 4 ps, which confirmed that $t_{95\%}$ was a more suitable reference than t_{SNAP} to compare the results of our simulations (t_p) to the experimental results (the MLD).

Our choice of $t_{95\%}$ was further motivated by the experimental observation that the bandwidth-limited time difference $t_{95\%} - t_{\text{SNAP}}$ did not vary with I_B , as shown in Figure SM 2.

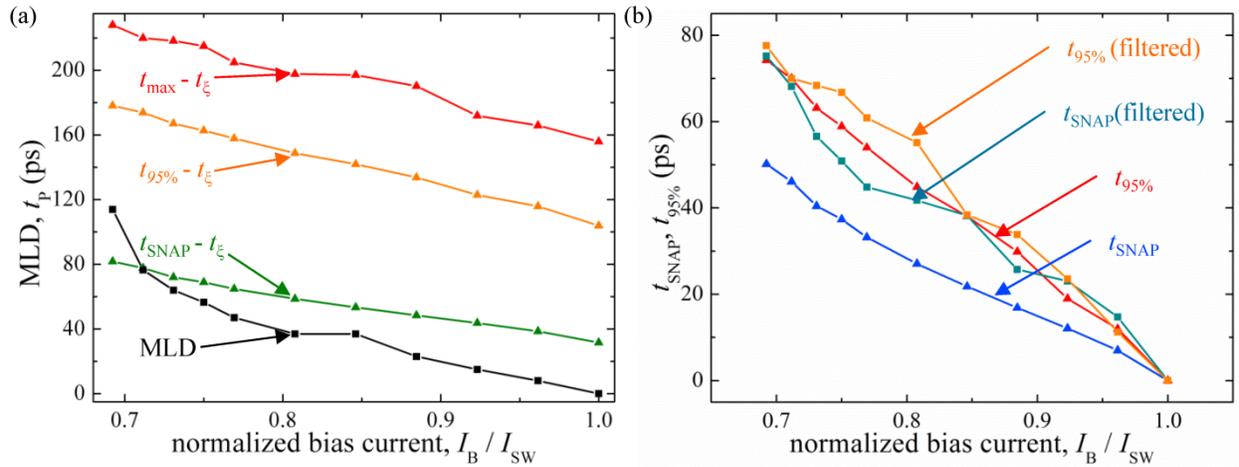


Figure SM 3. a. Experimental MLD vs I_B (black squares) and simulated t_p vs I_B (red, orange and green triangles) for the 2-SNAP of Figure 2b. The values of t_p were calculated by using different thresholds on the SNAP pulse as references: t_{\max} (red curve); $t_{95\%}$ (orange curve); and t_{SNAP} (green curve). **b.** $t_{95\%}$ and t_{SNAP} of the pulses shown in Figure 3a (triangles) and of the filtered pulses vs I_B (squares).

Bias-dependence of t_p for a superconducting nanowire single-photon detector

Figure SM 4a and b show the simulated time evolution after a HSN event (occurring at $t = t_\xi = 0$ s) of the current diverted from a superconducting nanowire single-photon detector (SNSPD) to the read out (I_{out} , see Figure SM 4a) and of the device resistance (R_{SNSPD} , see Figure SM 4b). We repeated the simulation at different values of I_B . Figure SM 4c shows $t_p = t_{95\%} - t_\xi$ for the SNSPD as a function of I_B .

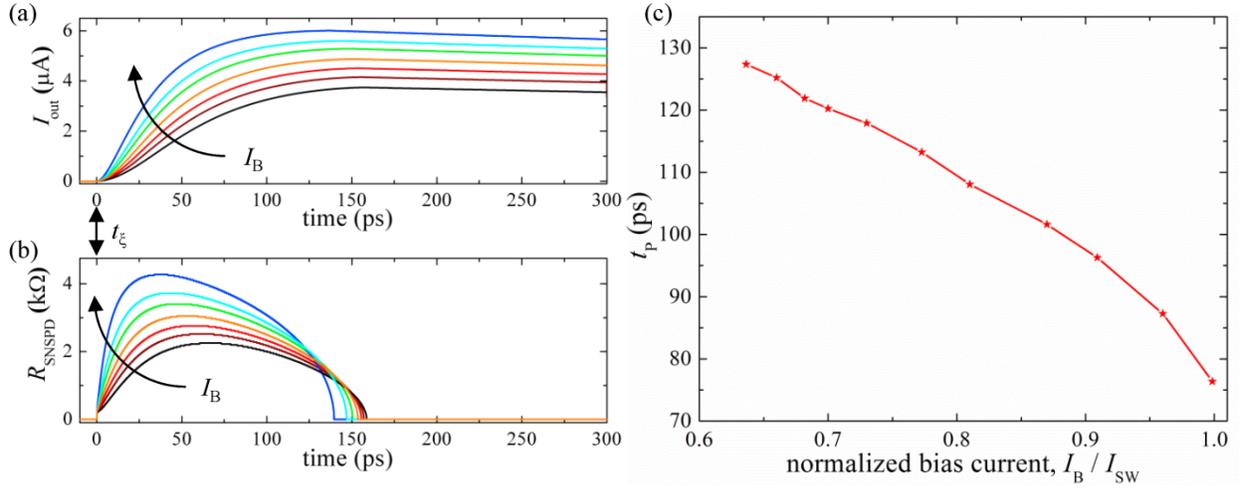


Figure SM 4. **a, b.** Simulated time evolution of I_{out} (a) and R_{SNSPD} (b) after a resistive ζ -slab is formed (at time $t_\xi = 0$ s) for an SNSPD biased at $I_B / I_{\text{SW}} = 0.96, 0.91, 0.81, 0.87, 0.81, 0.77, 0.68$. The SNSPD had the same kinetic inductance as the 2-SNAP of Figure 3, $L_{\text{SNSPD}} = 136.5$ nH. Black arrows indicate the time at which the resistive ζ -slab was formed (t_ξ) and the direction of increasing I_B . **c.** Simulated t_p vs I_B for the SNSPD of (a) and (b).

References

- ¹ F. Marsili, F. Najafi, E. Dauler, X. Hu, M. Csete, R. Molnar, and K. K. Berggren, *Nano Lett.* **11** (5), 2048 (2011).
- ² F. Marsili, F. Najafi, C. Herder, and K. K. Berggren, *Applied Physics Letters* **98** (9), 093507 (2011).