In recent years, the mathematics of fractal geometry has generated much excitement within the engineering community among those seeking broad new and more realistic classes of models for wide-ranging applications. This optimism has arisen out of the perspective that many natural and man-made phenomena around which we engineer our world are much better described through an inherently irregular “fractal” geometry than by the traditional regular Euclidean geometry. However, despite the apparent promise of fractal geometry in providing useful solutions to important engineering problems, progress in applying these models in such applications has been slower than expected. To a large degree, this has been due to the lack of an adequate set of convenient and efficient engineering-oriented mathematical tools for exploiting these ideas.

From this perspective, the recent emergence of powerful multiscale signal representations in general and wavelet basis representations in particular has been particularly timely. Indeed, out of this theory arise highly natural and extremely useful representations for a variety of important fractal phenomena. This book presents both the development of these new techniques as well as their application to a number of fundamental problems of interest to signal processing and communications engineers.

In particular, this book develops a unified, wavelet-based framework for efficiently synthesizing, analyzing, and processing several broad classes of fractal signals. For example, efficient and practical algorithms for solving some important problems of optimal estimation, detection and classification involving fractals are developed using this framework. As another example, novel and practical signal processing techniques for exploiting fractal signals
as information-bearing waveforms in efficient communication systems are
also developed.

In preparing this monograph, there has been an effort to make this
material as accessible as possible to graduate students and practicing profes-
sionals alike. In particular, no prior familiarity with either fractal geometry or
wavelets is assumed of the reader. In fact, Chapter 2 is a fully self-contained
primer on the relevant wavelet theory. However, to keep the treatment com-
 pact, the reader is assumed to possess a basic familiarity with continuous-
and discrete-time signals and systems, with stochastic processes, detection
and estimation theory, and with the geometry of linear vector spaces and
linear algebra. Wherever possible, concepts and intuition are emphasized
over mathematical rigor. Nevertheless, unavoidably some measure of that
ill-defined but important quantity “mathematical sophistication” is also
assumed of the reader.

As a final remark, it should be emphasized that no attempt has been
made to describe many of the exciting parallel developments taking place
within this active field of research. While I have tried whenever possible to
point out those developments most closely related to the material covered,
this monograph should not be interpreted as a comprehensive treatise. In
fact, rather than a retrospective on a mature topic, it is hoped that this book
will serve as a catalyst, stimulating further development in both the theory
and applications of the exciting, powerful, and increasingly important ideas
in this area.

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