

1. Consider an ensemble of atoms, all in the ground state except for one atom in the excited state. How does the initial photon emission rate depend on the atom number N ? (Assuming average inter-atomic separation is much smaller than the optical wavelength and a fully symmetric initial state)

A: The initial photon emission rate is proportional to N .

2. For the same situation as in 1.: What is the total number of photons emitted? Does it depend on N ?

A: single photon, no dependence on N .

3. For the same geometry as in 1. and 2., but all atoms in the ground state: How does the absorption probability for an incident photon depend on N ? Will the absorption of a single photon prepare the symmetric state assumed in questions 1. and 2.?

A: proportional to N . It will result in a symmetric state.

4. Superradiance requires the emission of photons to be in the same mode for all atoms involved. Give an example where atoms are not localized to a region smaller than the optical wavelength, but still show superradiance and explain why.

A: There are many, as long as the emission is into a single mode and the coherence time is sufficiently long (such as emitting into the same cavity mode, or atoms in an elongated shape, e.g. a cigar-shaped BEC)

5. Suppose we live in a 1D world (on a line) and we trap an array of atoms along this direction, where adjacent atoms have random separations which are larger than the optical wavelength. The atoms are in a symmetric state, with one excitation. The system will emit a photon, and due to the 1D feature the photon can only be emitted forward or backward. What is the rate for emission of the photon when Γ is the rate for a single atom?

- $N * \Gamma$, fully superradiant effect. In one direction, the emission of all atoms can be in phase. One can say that the phase for each atom compensates for the propagation phase.